

From x-ray crystallography to electron microscopy  
and back -- how best to exploit the continuum of  
structure-determination methods now available

Scripps EM course, November 14, 2007

What aspects of contemporary x-ray crystallography have made it a particularly powerful tool in structural biology?

- **Molecular replacement**: the body of pre-existing structural knowledge simplifies a new structure determination
- **Density modification**: elimination of noise by imposition of “reality criteria” in direct space
- **Refinement**: constraints enable you to incorporate chemical “reality criteria”

1. Phasing x-ray data from EM (TBSV; reovirus core)
2. Phasing electron diffraction data from coordinates derived from x-ray crystallography (aquaporin)
3. Docking an x-ray structure into an EM map (clathrin coat)
4. Lessons from x-ray crystallography for single-particle EM

# X-ray crystallographic structure determination

1. Experimental phases → map → (modified map) → build model

Experimental phases are poor; density modification is useful whenever possible.

Building rarely produces complete or fully correct model:  
model → refine → rephase → rebuild and extend model  
→ refine → (cycle)

2. MR phases → map and MR model → rebuild or extend model  
→ refine → (cycle)

Map is strongly biased, so it is *much* better to modify map based on solvent flattening or ncs, then continue with rebuilding and extending

Examples: phases from EM map  
as MR “model”, density modification  
from non-crystallographic symmetry  
(icosahedral: 5-fold in these two cases)

TBSV: negative stain, 30 Å (1974)

Reovirus: cryo, 30 Å (2000)

## Structure of Tomato Bushy Stunt Virus

### II.† Comparison of Results Obtained by Electron Microscopy and X-ray Diffraction

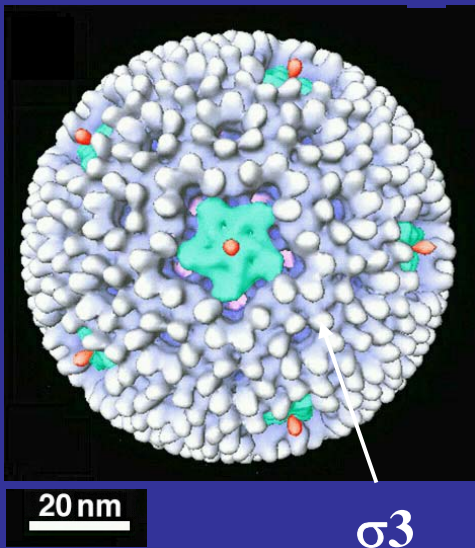
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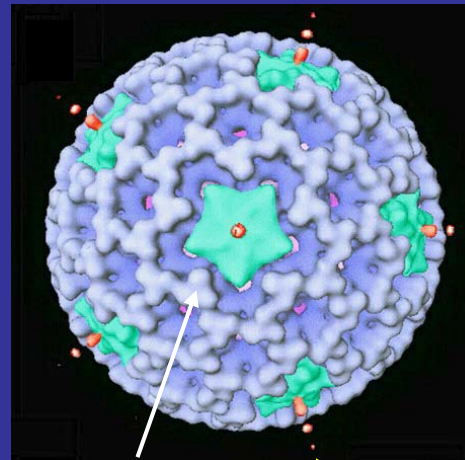
A three-dimensional reconstruction from electron micrographs of tomato bushy stunt virus has been used to determine X-ray phases to 28 Å resolution, by analogy with the single isomorphous replacement method of protein crystallography. An electron density map computed from X-ray amplitudes and these phases differs in two important respects from the electron micrograph reconstruction. The exclusion of stain from the 5-fold vertices, previously attributed to the presence of a minor protein, is shown to be an artifact of staining. The other difference involves positive staining of the RNA at the quasi-3-fold positions.



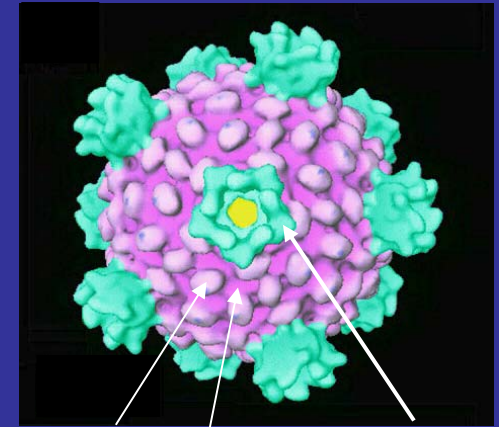
Protease



$\sigma 3$



$\sigma 1$   
 $\mu 1$



**Virion**

**ISVP**

infectious or  
intermediate  
subviral particle

**Core**

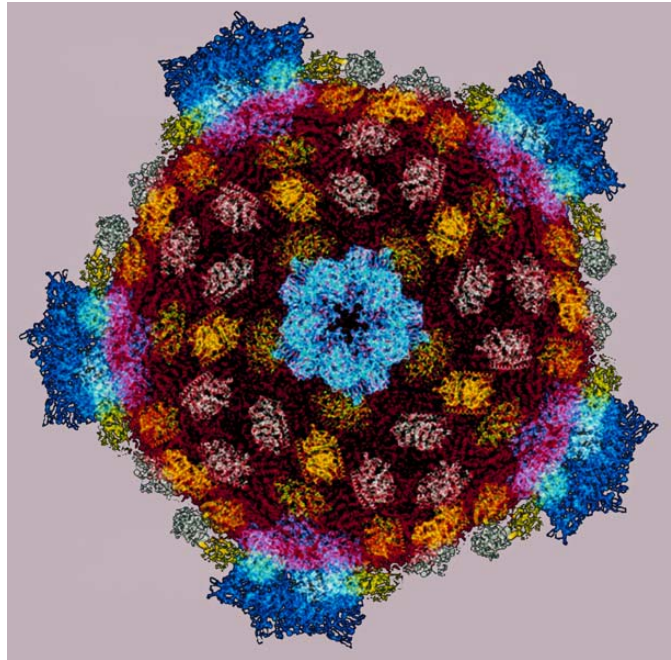
Dryden, Baker *et al.* (1993).

# Crystals of reovirus cores

F432,  $a = 1255 \text{ \AA}$

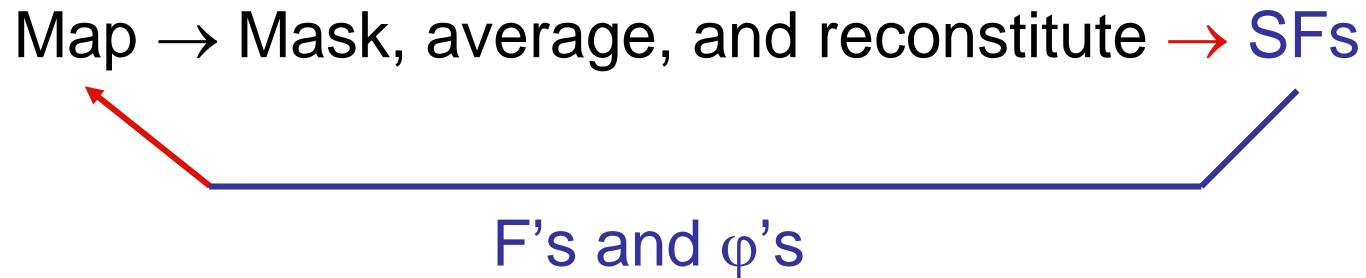
Initial phases to  $30 \text{ \AA}$  from modified EM density

Phase extension by averaging



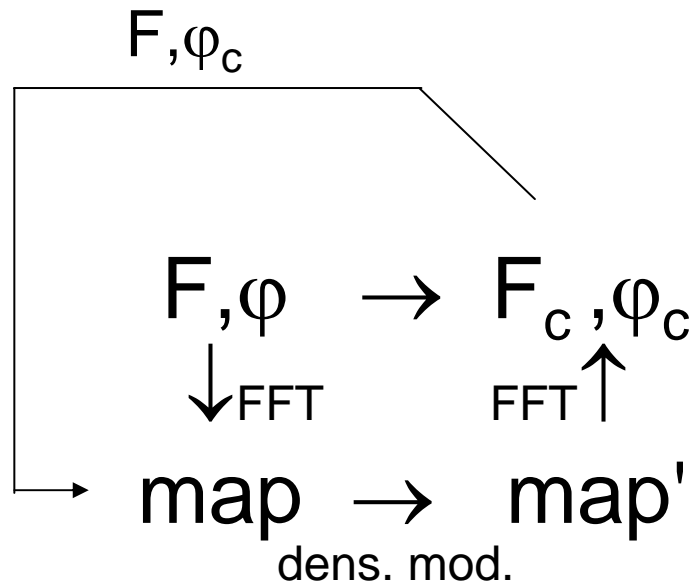


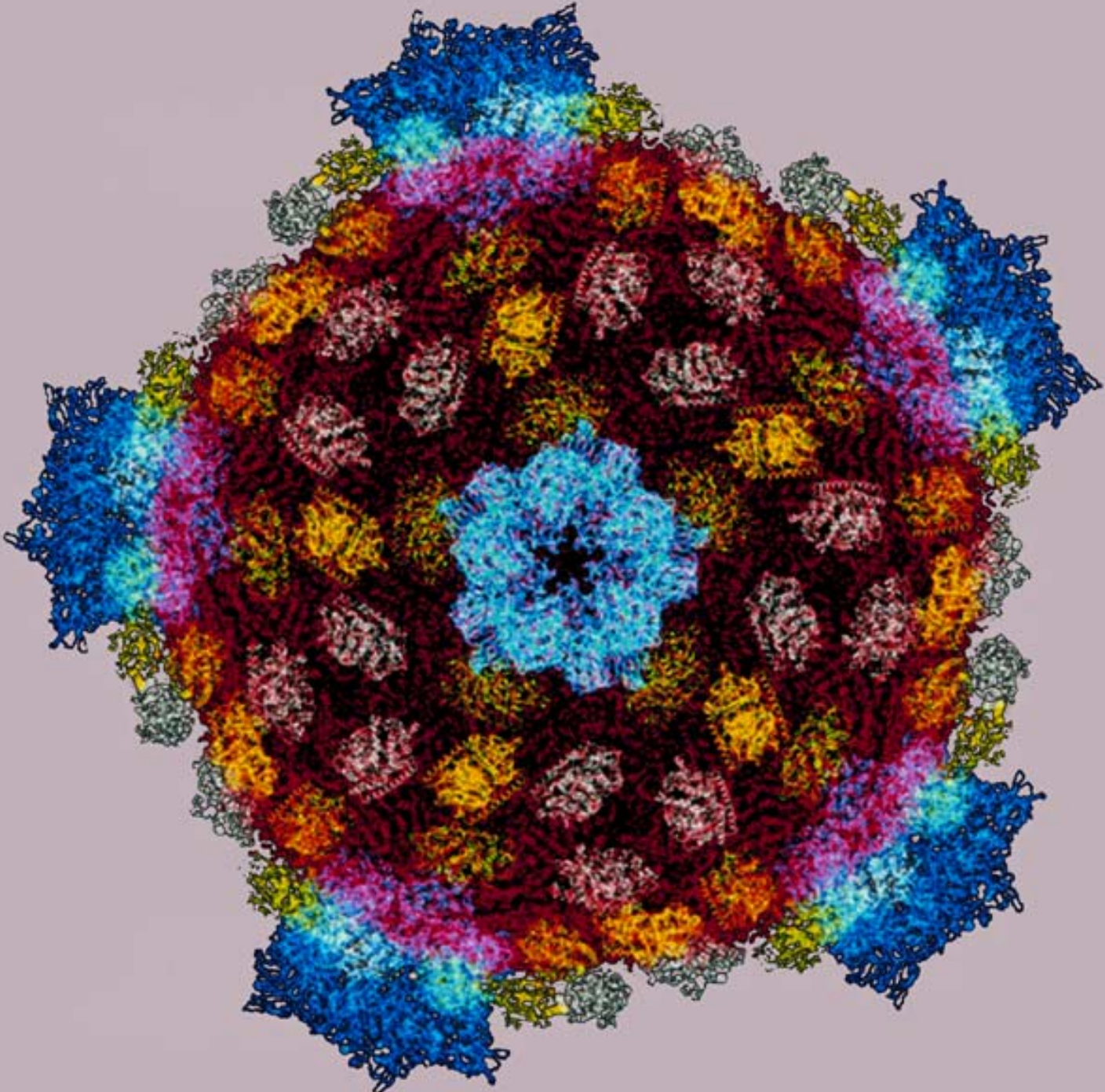
## Averaging as basis for phase extension in x-ray crystallography



Works because true a.u. is smaller than crystallographic a.u., transform is effectively oversampled

# Non-cryst. symmetry averaging and solvent flattening





## Aquaporin-0 (AQP0):

Molecular replacement with MOLREP, monomer as model  
Must refine unit cell (grid search)

Refinement with CNS

1. Rigid body with unit-cell variation
2. Simulated annealing; rebuild from 2Fo-Fc with solvent flipping maps and SA omit maps to correct

Gonen et al, 2004

# Aquaporin-0

(AQP0).

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Two-dimensional crystals	
Layer group	p422
Unit cell (Å)	$a = b = 65.5$
Thickness (assumed) (Å)	160
Electron diffraction	
Number of patterns merged	286 (0°, 11; 20°, 43; 45°, 107; 60°, 87; 70°, 38)
Resolution limit for merging (Å)	1.7
$R_{\text{Friedel}}$ (%)	14.25
$R_{\text{merge}}$ (%)	16.60
Observed amplitudes to 1.9 Å	126,980
Unique reflections	22,293
Maximum tilt angle (°)	71.3
Fourier space sampled	80.0% (70.5% at 2.0-1.9 Å)
Multiplicity	5.7 (2.5 at 2.0-1.9 Å)
Crystallographic refinement (5.0-1.9 Å)	
Resolution limit for refinement (Å)	1.9
Crystallographic $R$ factor (%)	25.81
Free $R$ factor (%)	29.93
Reflections in working/test set	14,600/1,580
Non-hydrogen protein atoms	1,784
Non-hydrogen lipid atoms	348
Solvent molecules	76
Average protein $B$ factor (Å <sup>2</sup> )	48.4
Ramachandran plot (%)	97.5; 2.5; 0 (allowed; generous; disallowed)

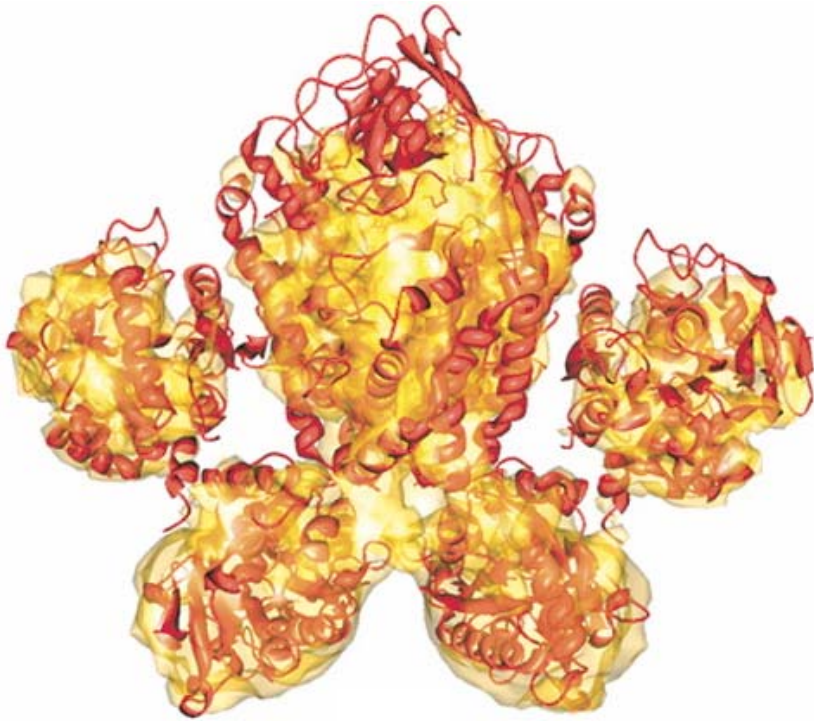
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Docking a model from x-ray crystallography  
(or NMR) into a cryoEM density

Two key resolution barriers:  $\sim 8-9 \text{ \AA}$  and  $\sim 4 \text{ \AA}$

Rigid-body refinement vs. more flexible refinement

# Transferrin/TfReceptor



  
90°



Cheng et al (2004) Cell 116:565-576.

## Molecular replacement:

1. Can a molecular model work as an initial reference for single-particle alignment, with appropriate filtering of spatial frequencies?
2. How can we best exploit molecular replacement in 2-D crystallography?

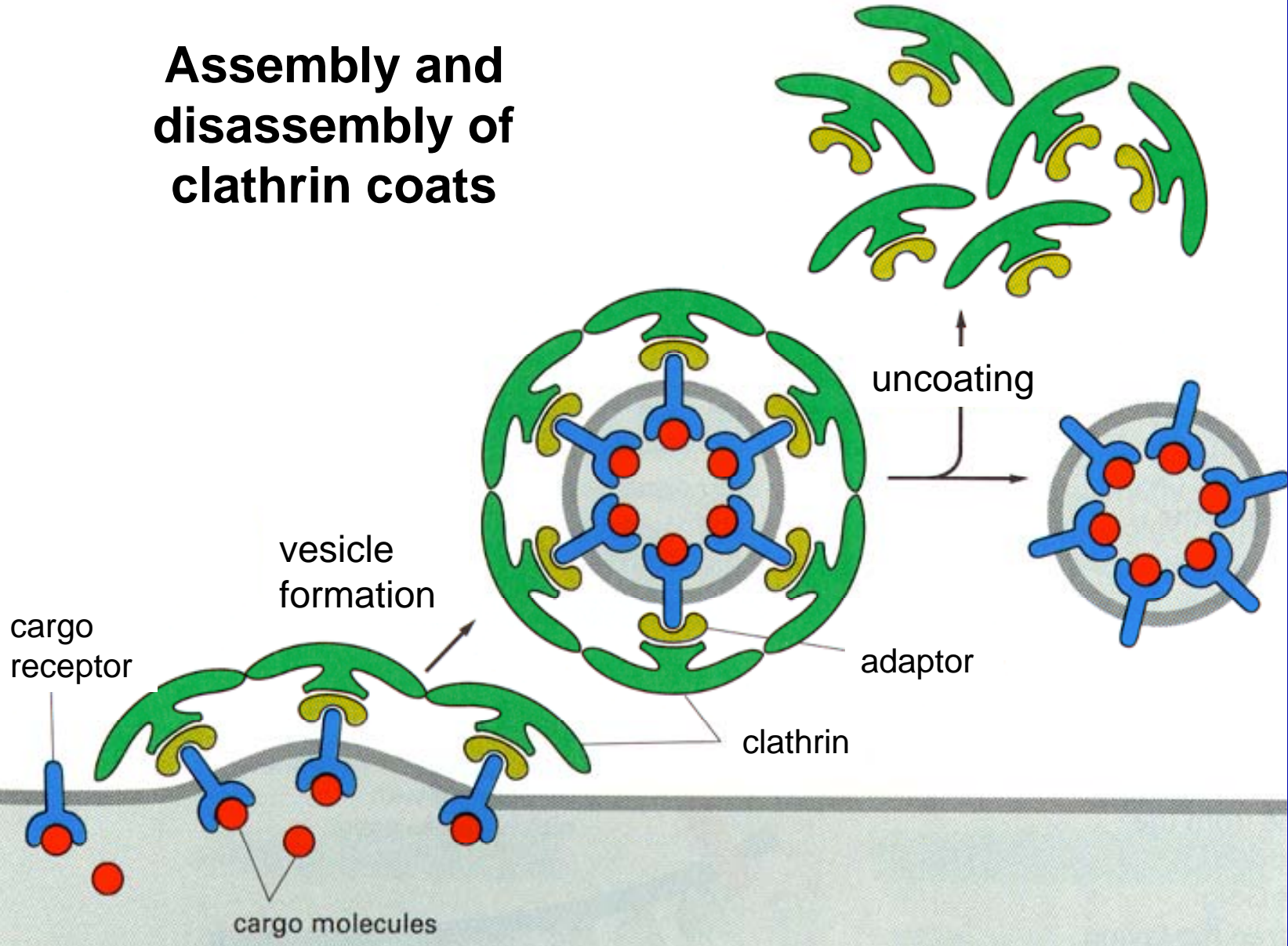


# Clathrin coat

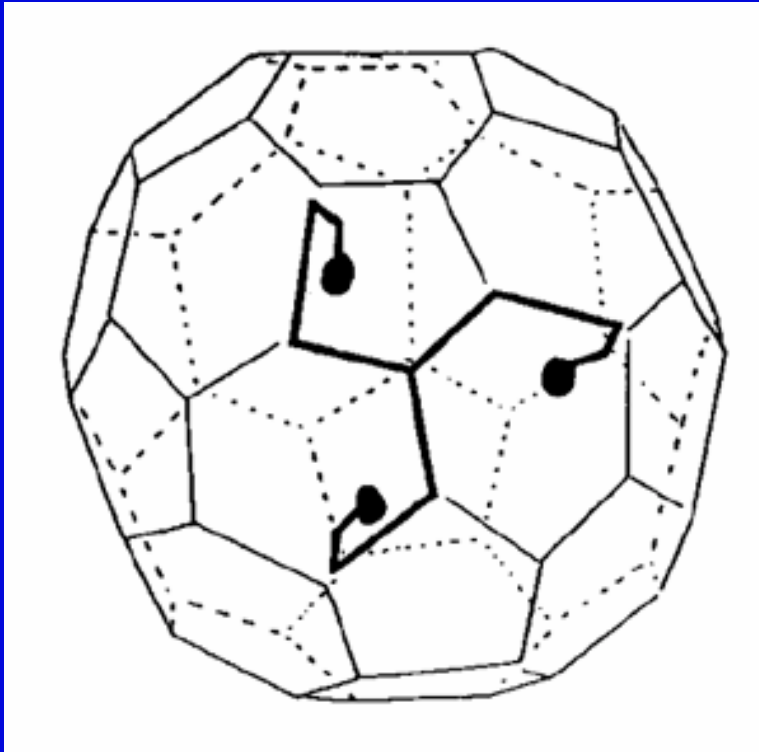
1. Density modification
2. ncs symmetry averaging

Fotin et al, 2004

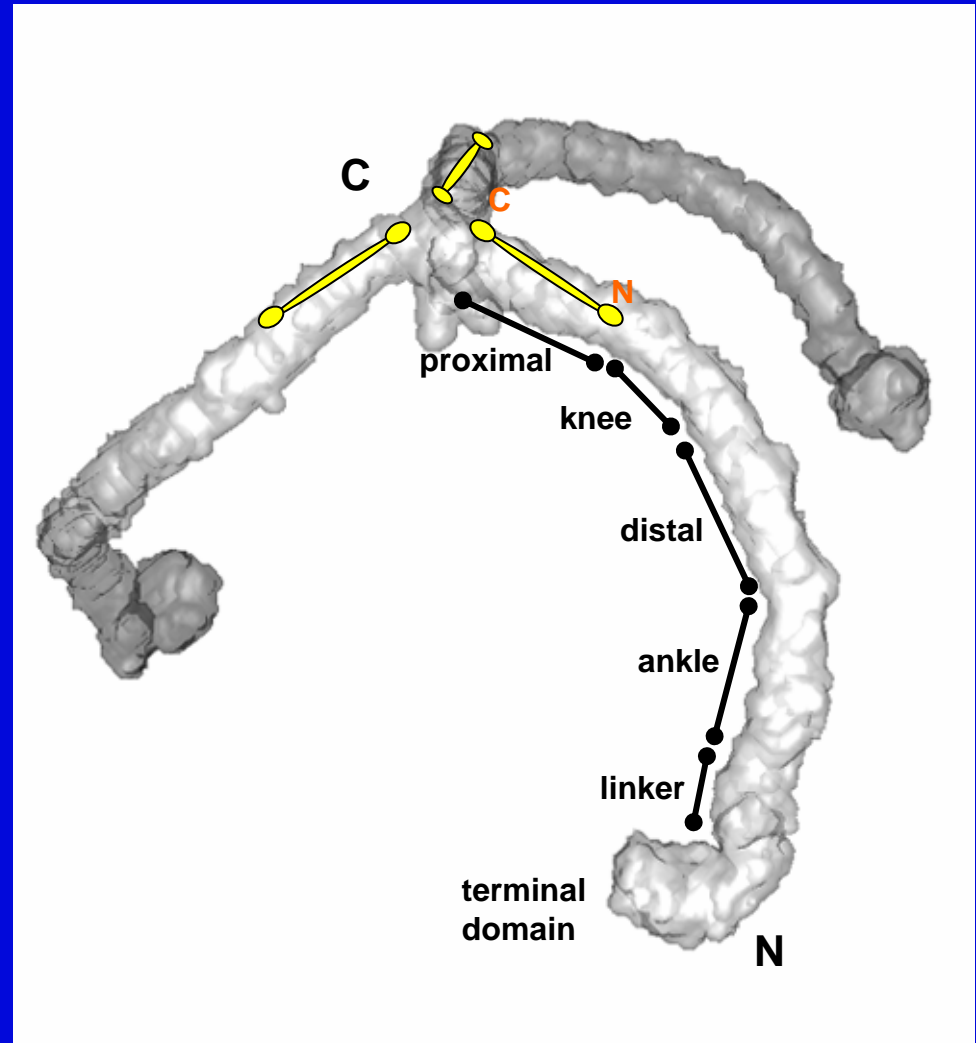
# Assembly and disassembly of clathrin coats



# Anatomy of a clathrin coat



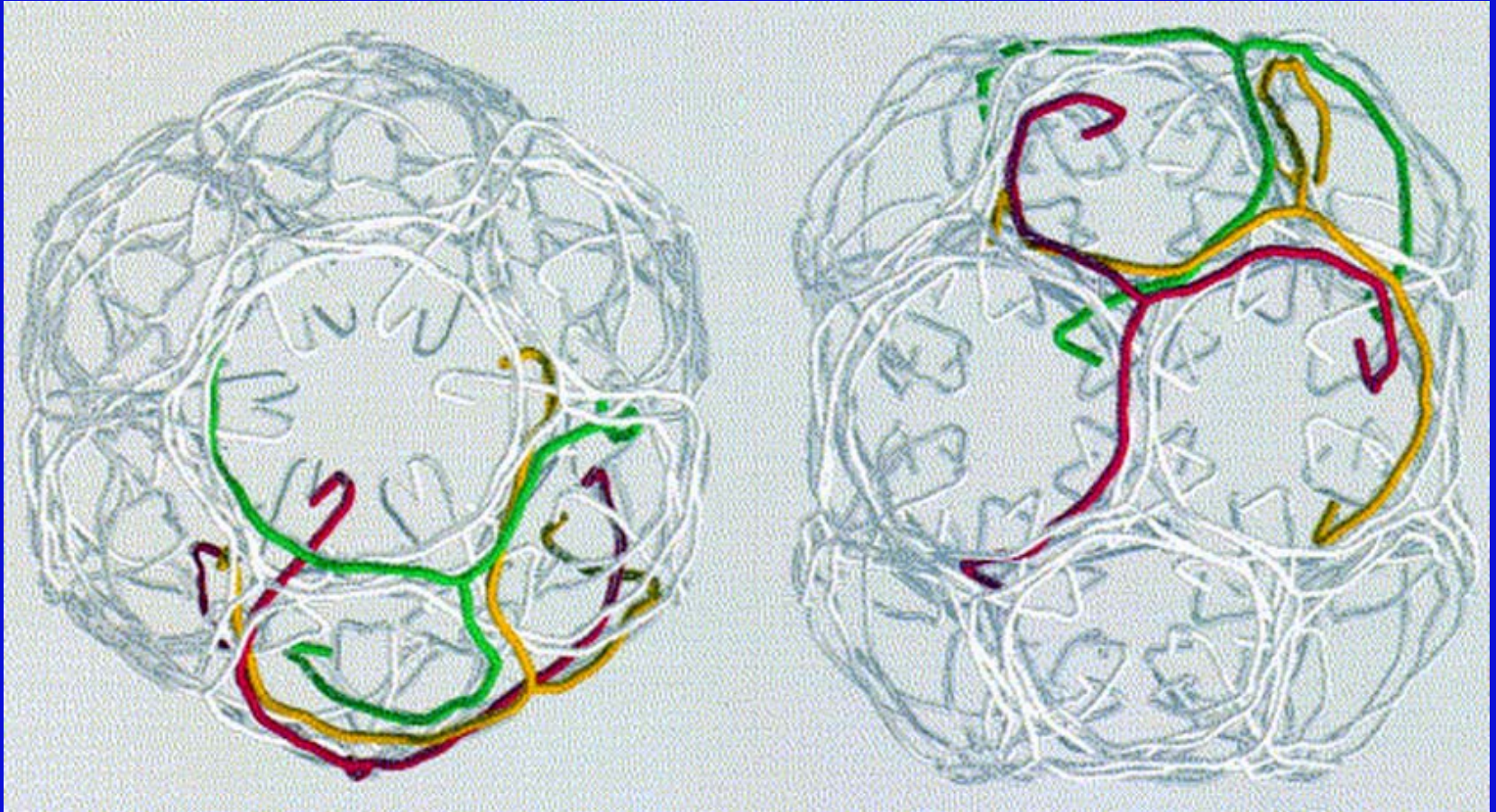
Clathrin lattice



Triskelion = 3 x (Heavy Chain + Light Chain)

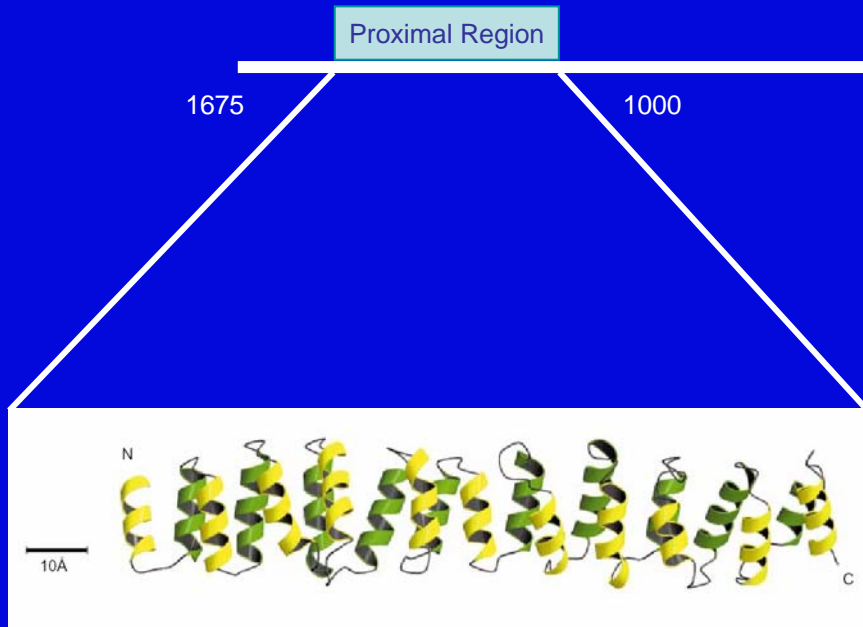
QuickTime™ and a  
Cinepak decompressor  
are needed to see this picture.

## D6 barrel

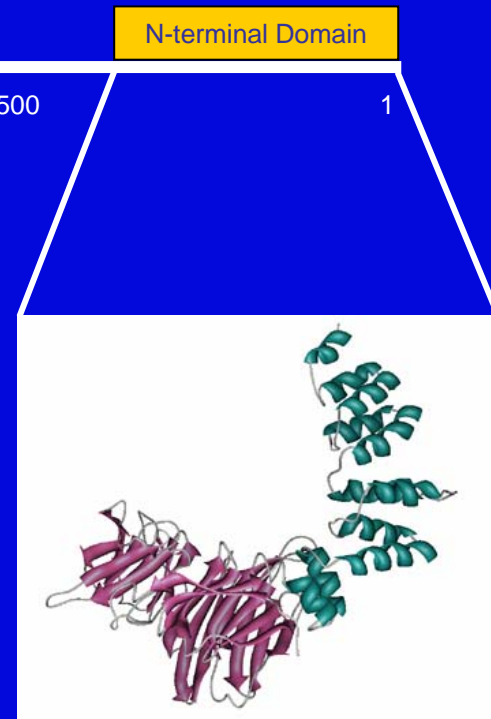


Musacchio, Smith, Grigorieff,  
Pearse, Kirchhausen

# X-ray structure of clathrin fragments



Ybe et al, 1999



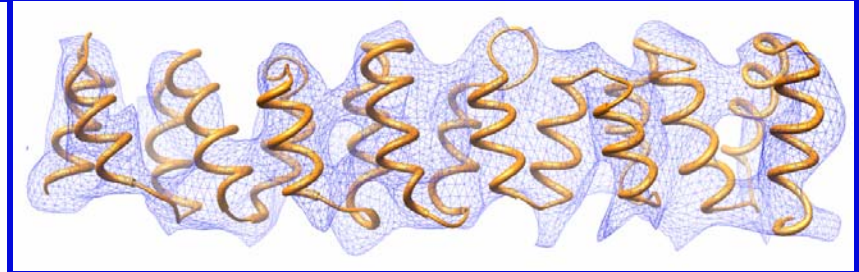
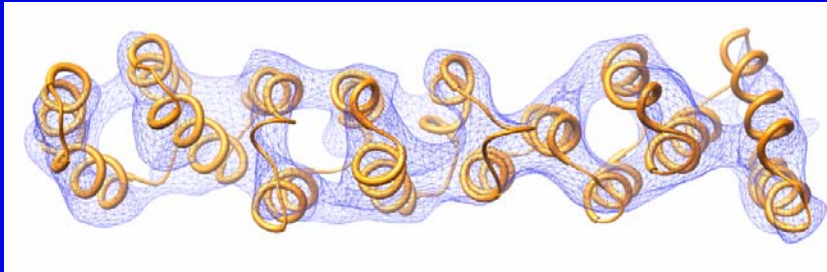
terHaar et al, 1998

# Comparison of EM and X-ray densities at 7.9 Å

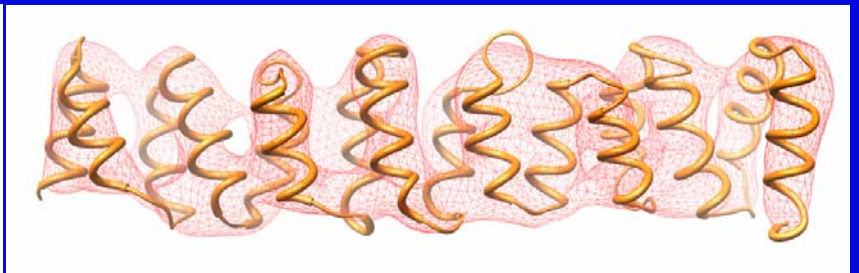
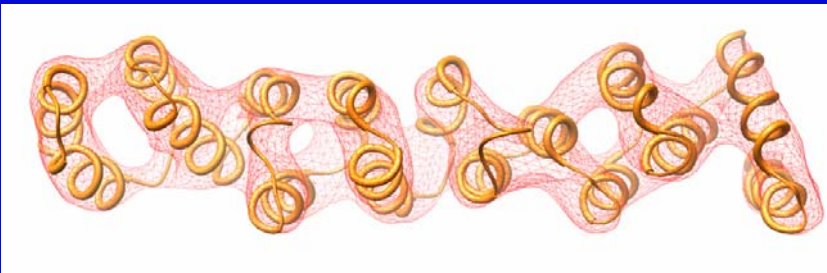
Top View

Side View

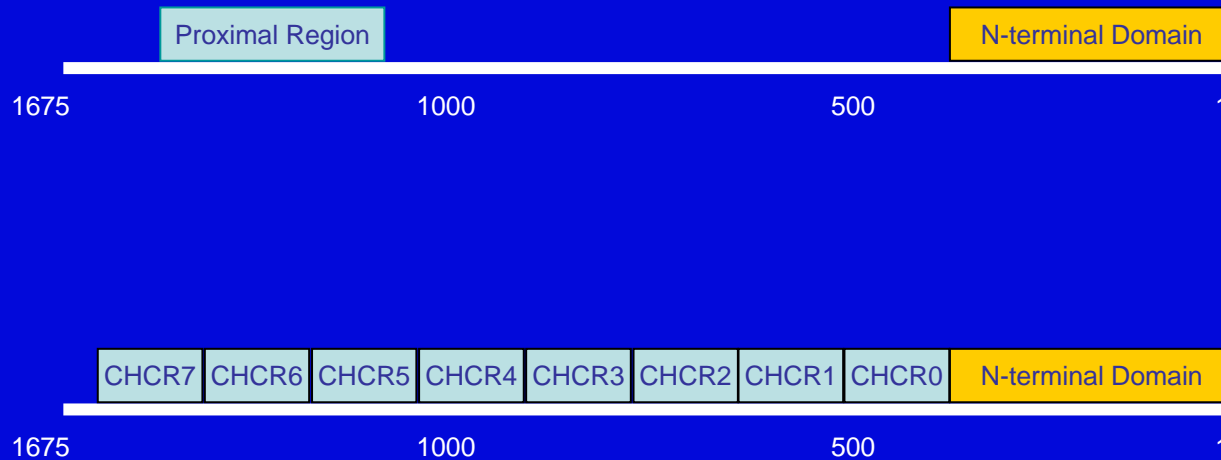
EM



X-ray

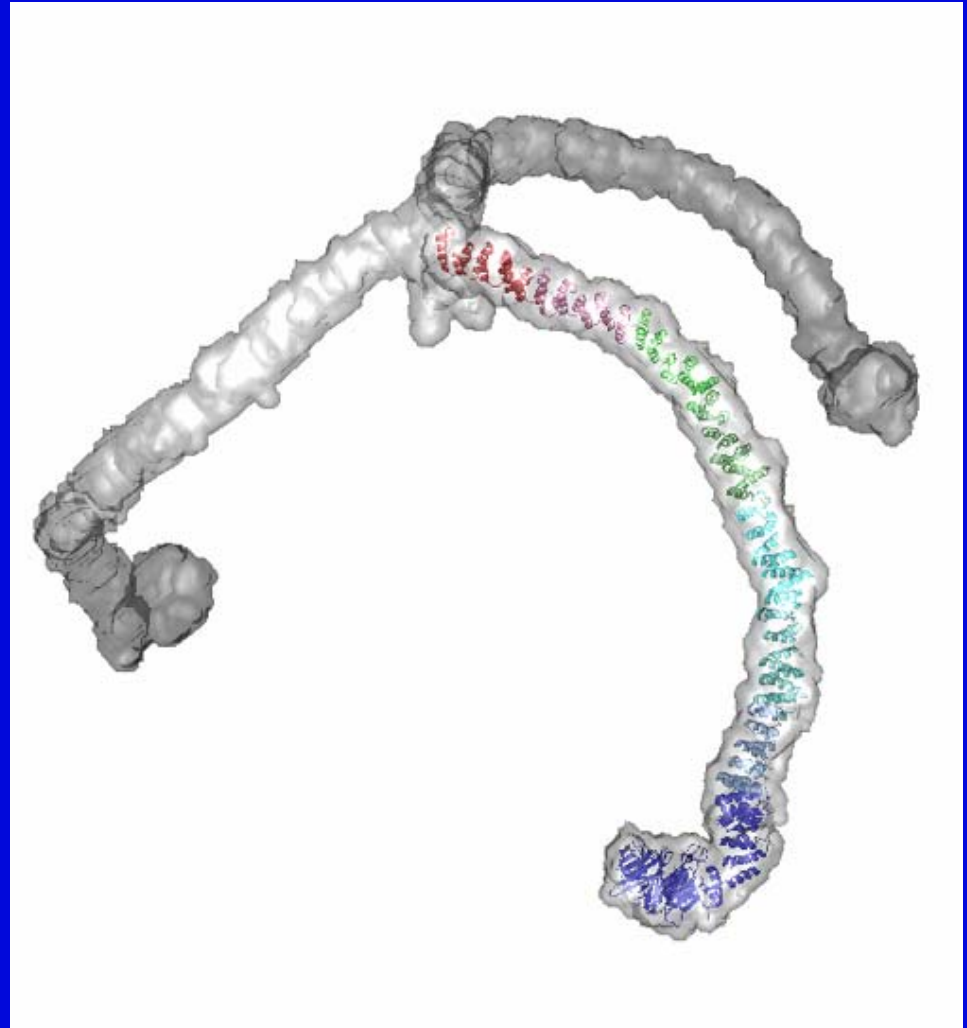
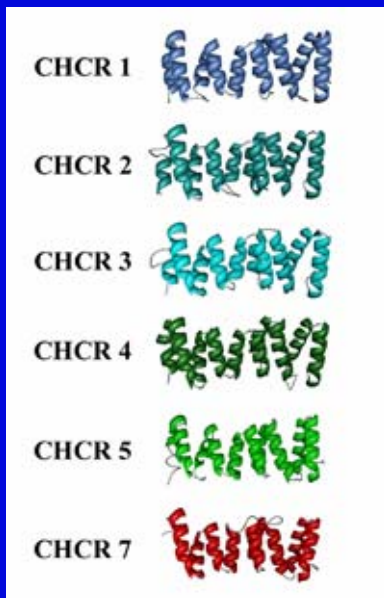
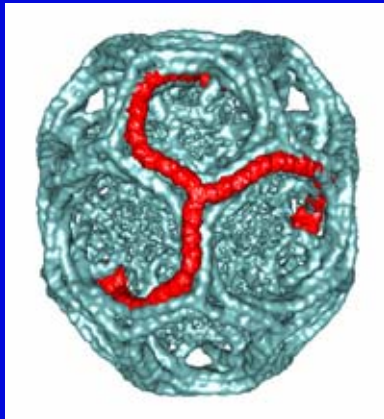
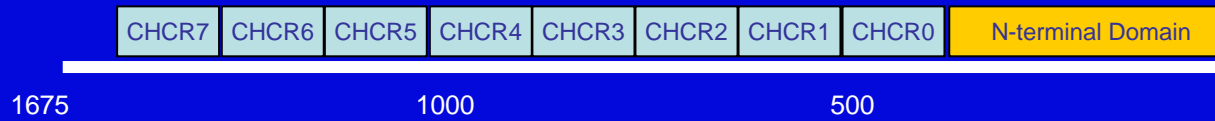


# Clathrin CHCR domain organization





# Modeling structure of the whole leg





Two questions:

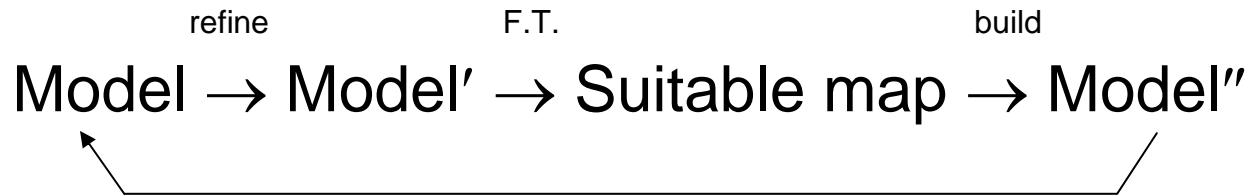
1. Can we improve a reconstruction by use of a model built into the density as reference?
2. Can we refine a model against the observed data (projected images)?

In crystallography, measured amplitudes are, by experimental arrangement, coming from an averaged structure.

In single-particle EM, measured projections contain unique “noise” that will disturb estimate of projection parameters

X-ray: observations are amplitudes; refine model parameters against these observations, using chemistry as a constraint.

If the model is incomplete, use refinement to improve phases, get better map, extend model.



Refinement minimizes:

$$R = \frac{\sum ||F_i^{\text{calc}}(h;x) - F_i^{\text{obs}}(h)||^2}{\sum |F_i^{\text{obs}}(h)|^2}$$

EM: observations are projections; what parameters should be refined?

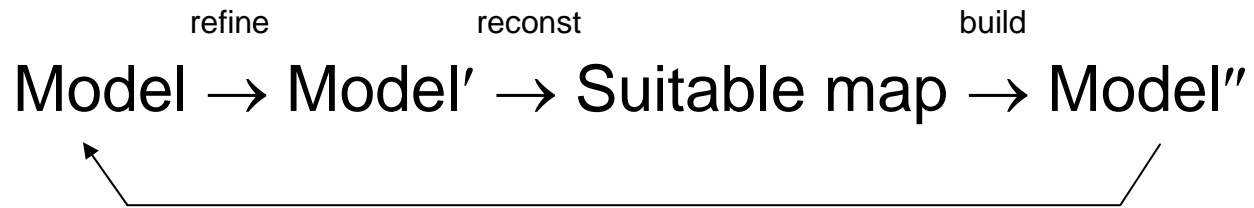
Do we have enough power to refine against the following agreement factor?

$$R = \frac{\sum |\sigma_i^{\text{calc}}(\mathbf{u}, \mathbf{v}; \mathbf{x}, \theta_i) - \sigma_i^{\text{obs}}(\mathbf{u}, \mathbf{v})|^2}{\sum |\sigma_i^{\text{obs}}(\mathbf{u}, \mathbf{v})|^2}$$

where  $\sigma_i^{\text{calc}}$  is the calculated projection, as a function of  $\mathbf{x}$ , the model coordinates (and B's), and of  $\theta_i$ , the orientation and origin of the  $i^{\text{th}}$  projection

If not, what is a suitable compromise?

Would hope to have the following cycle:



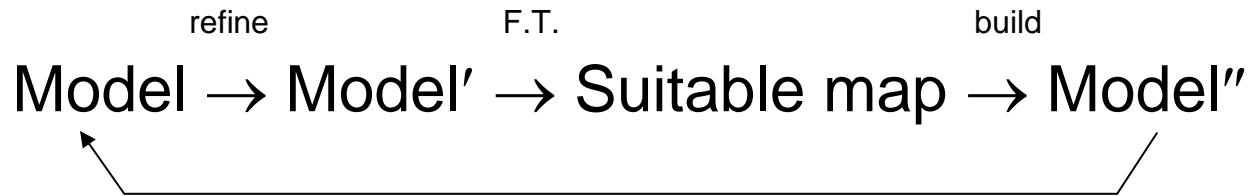
Karin Reinisch  
Tamir Gonen  
Yifan Cheng  
Piotr Sliz  
Alex Fotin

Tom Walz  
Niko Grigorieff  
  
Tom Kirchhausen  
  
David DeRosier



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