Negative Stain Image of "2D-Crystal"

Electron Crystallography of Two-Dimensional Crystals

The Basics

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To grasp the basic ideas underlying electron crystallographic image processing, all we need to ask is: how can we describe a periodic array without using the actual picture itself?



The regularity of the crystal "lattice" is reflected in a "repeat" in the OD-pattern.



However: the repeats are not precisely the same due to noise, low-dose conditions, and irregularities in the lattice (= lattice disorder). Nevertheless, the periodic nature of the OD-pattern begins to provide clues how these data structure can be exploited.



2D-crystals present us with the easiest approach towards structure because the Fourier Theorem states that any periodic function can be described as the sum of a series of sinusoidal functions of wavelengths that are integral fractions of a single basic wavelength λ .

$$\begin{split} f(x) &= \frac{C_0}{2} + C_1 \cos(\frac{2\pi x}{\lambda} + \alpha_1) + C_2 \cos(\frac{2\pi x}{\lambda/2} + \alpha_2) + \dots \\ C_n \cos(\frac{2\pi x}{\lambda/n} + \alpha_n) \end{split}$$
 Or short

 $f(x) = \frac{C_0}{2} + \sum_{n=1}^{n=\infty} C_n \cos(\frac{2\pi x}{\lambda/n} + \alpha_n) \qquad \begin{array}{c} C_n \text{ Amplitude} \\ n \text{ Order} \\ \alpha_n \text{ Phase} \end{array}$

In other words: the FT of a 2D-crystal will be discrete and if we know the "recipe" for building one single unit cell of the periodic array (e.g. the grey part of the function shown above), then we know the structure of the entire crystal.



In principle: the Fourier components and their summation to obtain a real space picture of an object is very similar to making Lasagna....



To prove the point



cryoEM picture of a gap junction 2Dcrystal (periodic object) deposited on continuous carbon support film (aperiodic object)

Spots at regular spacings: diffraction maxima arising from crystal. Alternating pattern of bright and dark regions. This is a combination of two things. (1) the aperiodic carbon film causes diffraction at all angles, and (2) the oscillation in intensities **a)** b) is the manifestation of the CTF of the objective lens (not all diffracted waves are transmitted with the same fidelity)

Calculated FT of the image. What do you see? And what is causing it?









enlarged area of FT

circular maskholes applied (FT has now non-zero values only within maskholes

Digital Filtering of Fourier Transform



Autocorrelation Map

Part of Crosscorrelation Map



Note that the shape of the central peak in the autocorrelation map is very similar to the shape of the cross-correlation peaks.

Digital Filtering of Fourier Transform





Crosscorrelation Maps

Now that the data extend to well beyond 10Å, correction for the CTF





deviation from expected lattice position [Å] X20 (not to scale) with respect to chosen reference

becomes critically important.

height of cross correlation-peaks indicates how similar each unit cell is to the chosen reference

The simulated curves are for 3000 and 6000Å of underfocus respectively, an accelerating voltage of 200keV (λ =0.025Å) and

demonstrate how the CTF would look like in the FT of the image. Circles represent [sin $\Phi(\alpha)$] =0 Frequencies where $[\sin \Phi(\alpha)] < 0$ contribute with reversed contrast to

the image. Therefore, the phases

of reflections in these regions need

a C_s=2mm

These lower two panels

Effect of "Lattice Unbending"



Left: data were retrieved from a calculated FT of an untreated raw image. In this case, the data are not statistically significant beyond ~15Å resolution.



Right: after correction for translational lattice disorder, the same image provides data out to ~7Å resolution.

Plot symbols indicate the goodness of each reflection. Reflections marked by a "1" have a signal-to-noise ratio of at least 8.



Basic Image Processing of 2D-Crystals





REAL SPACE

RECIPROCAL SPACE









What happened!! Did I take a bad image/picture?

Looking at a couple of unit cells together explains everything......



The answer is: **by shifting the phases**. Remember, a movement in real space correlates to a phase shift in reciprocal space



The molecules contoured in green are shifted by 1/2 unit cell (=180 degree shift applied to the (1,0) reflection) with respect to the molecules contoured in magenta



Projection Density Map and some of the Corresponding Structure Factors



Real space map obtained by Fourier summation

1.0	<u>(H,K,L)</u>	amp	phase	FOM
1	100	2566	180	99.5
	110	12424	180	99.9
	120	777	180	99.5
	130	1123	0	99.7
	140	208	0	73.9
	150	605	0	99.0
	160	670	180	99.2
	170	250	180	99.6
	180	350	0	94.3
	190	77	180	59.8
	1 10 0	140	0	13.3
	200	9265	180	99.9
	210	1971	0	99.8
	And so for	orth		

The presence of symmetry requires the contents of the unit cell to be positioned such that the crystallographic related molecules have the correct spatial relation with respect to the symmetry axes.....take p6 for instance.....



0 Twofold axis

△ Threefold axis

 \bigcirc Sixfold axis

Remember, p6 symmetry has not been imposed here...but the more pressing issue is how do we get from the p1 map we have to a distribution of densities that looks like above?





Example for a Lattice Line



This figure shows the variation of phase (top panel) and amplitude (bottom) of the (2,5)-reflection of a gapjunction 2D-crystal as function of z*.

The amplitudes were obtained from the calculated image transforms. In contrast to the phase information, image derived amplitudes are very **noisy** mostly because the image is modulated by the contrast transfer function of the objective lens (see page showing the calculated FT of an image). The effect of the CTF on amplitudes cannot be fully corrected, but, on the other hand does not really matter that much because it is the phases that determine the structure.

Concept of Lattice Lines and Principle of Sampling their Data



Taken from: Amos, Henderson and Unwin (1982), Prog. Biophys Molec Biol 39:183-231



3D-Map of a Gap-Junction Intercellular Channel

Shown are a surface representation at ~7.5Å resolution A total of ~42,000 channel molecules were crystallographically averaged to obtain this structure.

THE END