Fitting high resolution structures into low resolution EM maps

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Fitting Processes

1. Map scaling
2. Symmetry constraints
3. Fitting criteria
   a. fit of atoms into density
   b. avoiding negative density
   c. steric hindrance, inter atomic clashes
   d. restraints imposed by known structural features
4. Combining different criteria
   a. normalization of each measurement
5. The search process
   a. rotational search
   b. multi-dimensional "climb" or least squares
6. Verification
   a. hand of map
   b. subunit contacts
7. Problems
   a. symmetry missmatches
   b. unknown structural components
   c. uninterpreted density

Map Scaling

Minimize $\Sigma [\rho_1(x_1,y_1,z_1) - (a + b\, \rho_2(x_2,y_2,z_2))]^2$

where ρ_1 is the reference map (e.g. X-ray virus map)

and ρ_2 is the map of interest (e.g. virus plus ligand complex)

And $x_1 = x_2 + \delta x_2$, $y_1 = y_2 + \delta y_2$, $z_1 = z_2 + \delta z_2$
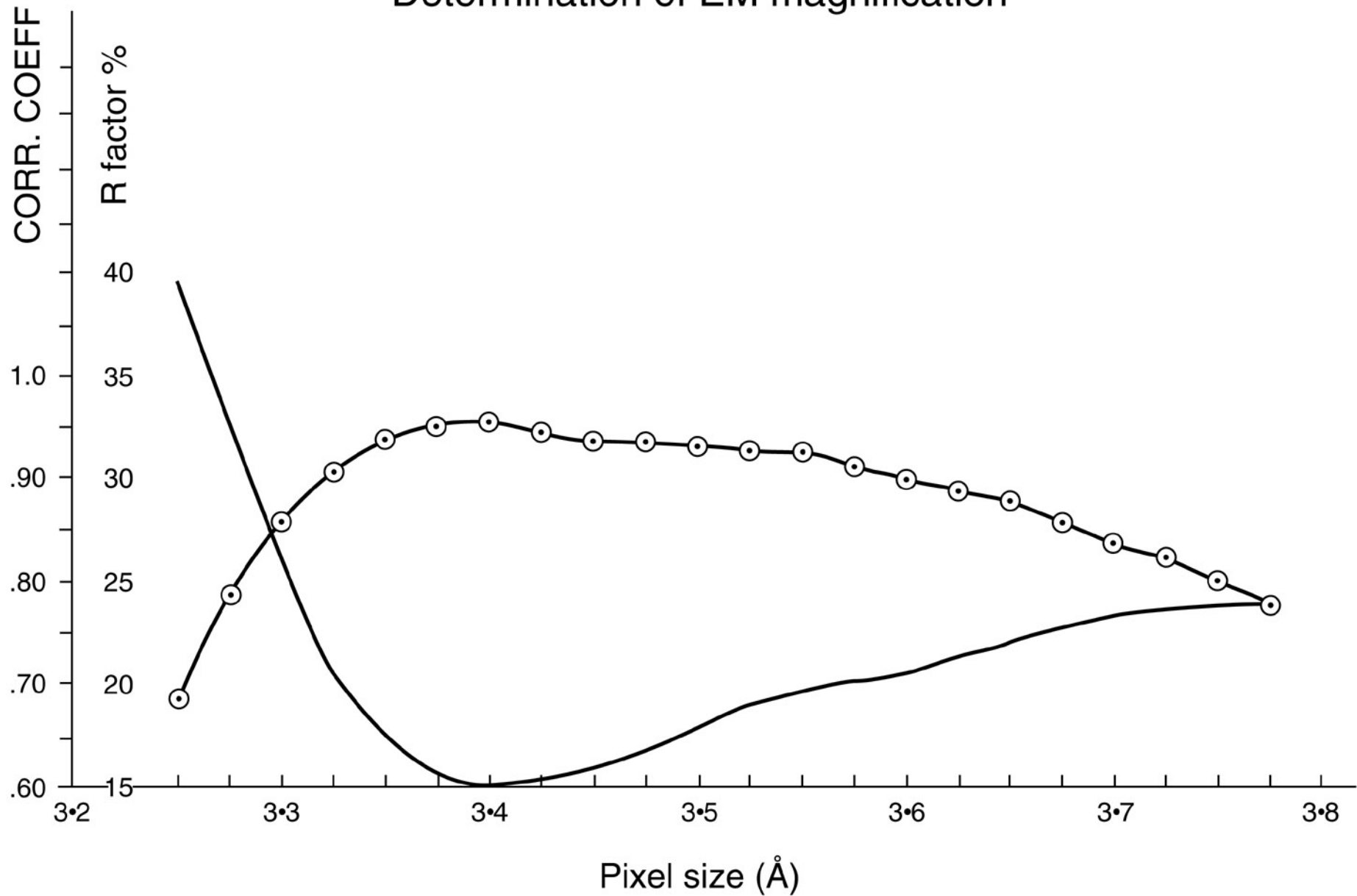
Requiring interpolation for determinin ρ_2

Or maximize the correlation C, where

$C = [\Sigma(\langle\rho_1\rangle - \rho_1)(\langle\rho_2\rangle - \rho_2)] / [\Sigma(\langle\rho_1\rangle - \rho_1)^2].[\Sigma(\langle\rho_2\rangle - \rho_2)^2]$

Comparison of the PV1:CD155 EM map with the PV1 X-ray map:

Shell radius (Å)	108 - 120	120 - 132	132 - 144	144 - 156
Number of Pixels*	3,918	22,203	17,914	3,424
Correlation Coefficient[†]	0.1881	0.2662	0.9105	0.9860

Determination of EM magnification

Symmetry Constraints

Let the atomic positions of a model be given by (X,Y,Z), or, in vector notation, by $\mathbf{X}$, in an orthogonal coordinate system.
Let the origin of the model (defined by its center of mass) be at $\mathbf{S}$.
Let the rotation matrix required to place the model into the "reference" EM density be $[E]$, Then

$$\mathbf{X'} = [E]\mathbf{X} + \mathbf{d},$$

where $\mathbf{X'}$ are the coordinates of the model atoms in the EM map and $\mathbf{d}$ is a translation vector.

Let $\mathbf{S'}$ be the approximate target position in the EM map for placement of the model's origin. Then

$$\mathbf{S'} = [E]\mathbf{S} + \mathbf{d}$$

and, hence,

$$\mathbf{d} = \mathbf{S'} - [E]\mathbf{S}$$

or

$$\mathbf{X'} = [E](\mathbf{X} - \mathbf{S}) + \mathbf{S'} .$$

Let the reference molecule be reproduced by
M "crystallographic" and T "NCS" symmetry operations
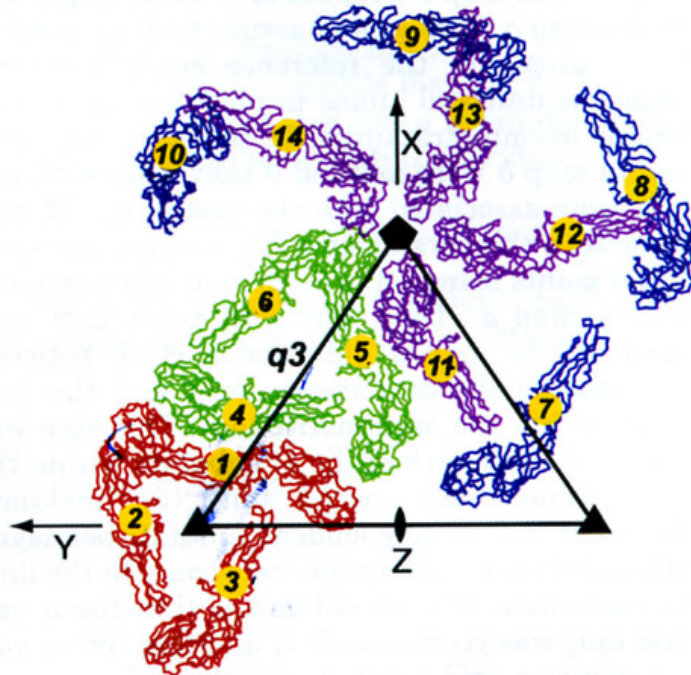given by $[R_m]$ ($m = 1, M$ and $t=1, T$). Thus

$$\mathbf{X''} = [R_{m,t}]\mathbf{X'}$$

And hence using

$$\mathbf{X'} = [E](\mathbf{X} - \mathbf{S}) + \mathbf{S'}$$

It follows that

$$\mathbf{X''} = [R_{m,t}]([E](\mathbf{X} - \mathbf{S}) + \mathbf{S'})$$

Sindbis Virus
M=60 icosahedral operators
T = 4 quasi symmetry NCS
operators

Fitting criteria

a. fit over N atoms into density

$$sumf = 100.\sum_{T} (\sum_{N} \rho(X'') / TN\rho_{norm}$$

   where ρ_{norm} is either the maximum or rms density

b. The number of atoms (N′) in negative density, expressed as a %

$$-den = 100.\sum_{T} (N') / TN$$

c. The number of atoms (N″) that approach atoms in another molecule to within 3.4A, expressed as a %.

$$clash = 100.\sum_{T} (N'') / TN$$

d. The average or rms distance between L specific fixed points (R_i) in the map and specific atoms on the molecule (X''_i) (e.g. Carbohydrate moities in the map and corresponding aas).

$$avgdist = \sum_{L} |(R_i - X''_i)| / L$$

Fitting the E1
protein
of Sindbis virus :
Using carbohydrate
sites as restraints

W.Zhang et al, J.Virol, 2002, 76, 11645-11658

Use of Restraints

1. Minimizing the distance between recognizable features in the cryoEM map and the associated atomic Group of the molecule being fitted

2. Restraining the molecule being placed in a map to use a specific contact region to other parts of the structure

3. Keeping a short distance between the C-end of one domain and the N-end of the next, independently fitted, domain.

Combining different criteria

$$R_{crit} = \Sigma \, \omega_i s_i \left[(\nu_i - <\nu_i>) / \sigma(\nu_i) \right] / \Sigma \omega_i$$

Where ν_i is the value of the ith criterion,

$<\nu_i>$ is the standard deviation of ν_i taken over a set of randomly oriented molecular fits into the density,

ω_i is the weight (usually 1.0) to be placed on the given criterion and

s_i is +1.0 if the criterion is to be maximized (e.g. *sumf*) or -1.0 if the criterion is to be minimized (e.g. *–den*, *clash*

Fitting the E1 protein of Sindbis virus. The top 25 best fit converge to only 4 different fits on refinement

a. Values of criteria

Fit No	R_{crit}	sumf	clash	-den	avgdist Å
13	0.98	39.3	0.5	9.2	21.9
10	0.81	37.3	2.2	10.1	20.5
14	0.26	36.3	3.7	11.9	21.2
25	-2.37	39.2	17.5	10.1	28.7

b. Criteria expressed as the number of σ above mean

Fit No	R_{crit}	sumf	clash	-den	avgdist
13	0.98	2.38	0.19	1.52	0.93
10	0.81	1.40	-1.35	1.18	1.48
14	0.26	0.48	-2.78	0.42	1.22
25	-2.37	2.32	-23.10	1.15	-1.67

The search process

2. Explore all unique values of the three Eulerian angles that define the [E] rotation matrix, using fairly large angular intervals

$$0 \le \theta_1 < 2\pi; \qquad 0 \le \theta_2 \le \pi, \qquad 0 \le \theta_3 < 2\pi$$

2. Rank according to sumf

3. Use results for determining the mean and standard deviation (σ) for each criterion required to calculate R_{crit}.

4. Refine the top n (e.g. 100) best fits by a six dimensional "climb" on R_{crit}, using fine angular and positional intervals.

5. Eliminate all but one of closely similar fits, leaving only distinctly different fits.

Note: fitting more than one rigid body at a time can be done sequentially and refined by least squares

Refine using "Climb"
R_{crit} values at end of climb

Refining the placement of the E1 glycoprotein
Into Sindbis virus cryoEM density

param	$\xi - \Delta\xi$	ξ	$\xi + \Delta\xi$	ξ	$\Delta\xi$
θ_1	1.016	1.029	1.022	357.0	0.25
θ_2	1.008	1.029	1.026	40.5	0.25
θ_3	1.021	1.029	1.021	193.5	0.25
x	0.996	1.029	1.011	23.9	0.50
y	1.028	1.029	0.990	68.3	0.50
z	0.963	1.029	1.015	284.5	0.50

The E glycoprotein dimer of flaviviruses : Sequential fitting into the mature dengue EM map

TBEV: F. Rey et al Nature, 1995, 375, 291-298
Dengue: Y. Modis et al PNAS, 2003, 100, 6986-6991

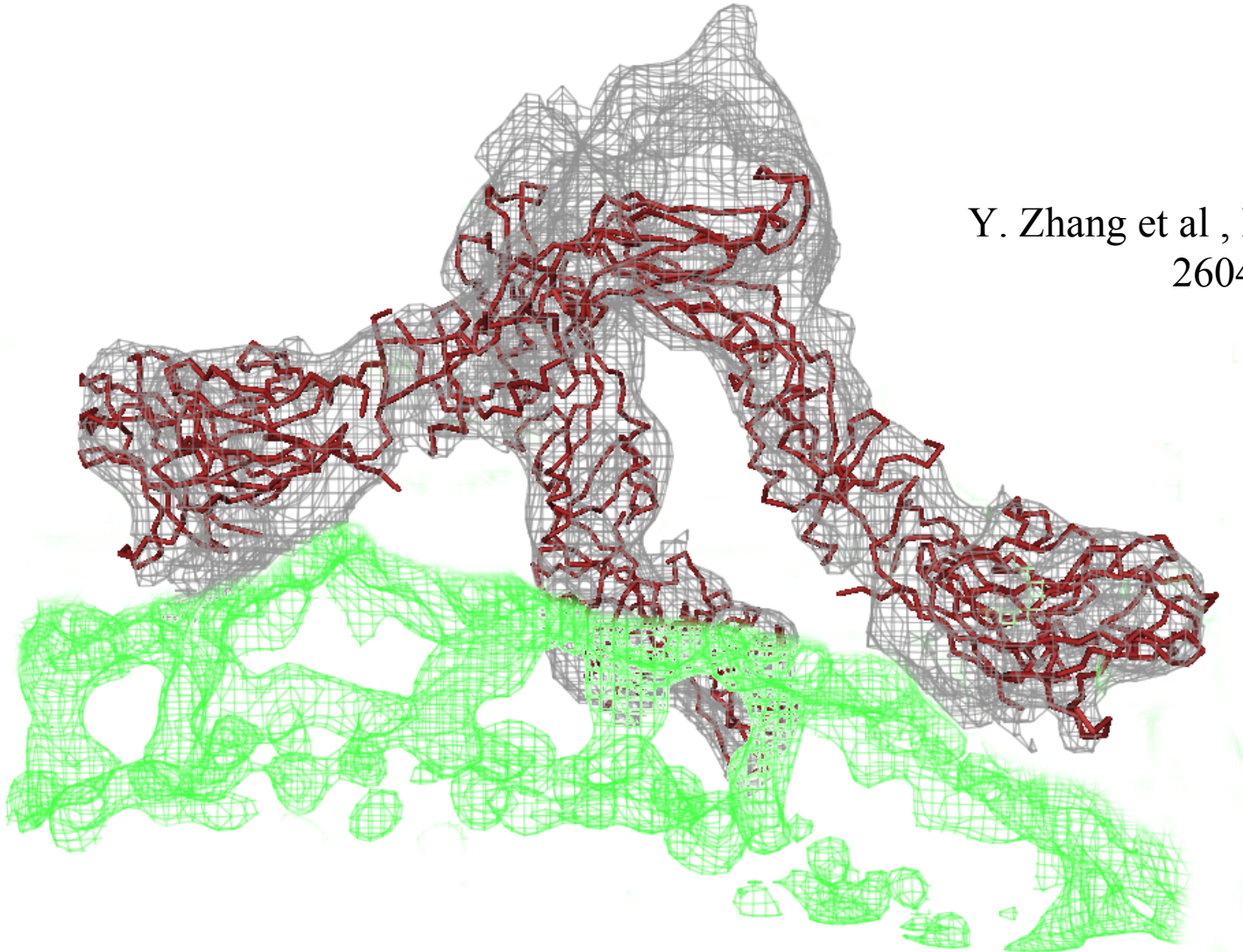   Y. Zhang et al, Structure 2004, 22, 2604-2613

The E glcoprotein monomer of flaviviruses :
Sequential fitting into the immature dengue virus map

Y. Zhang et al , EMBO J 2003, 22, 2604-2613

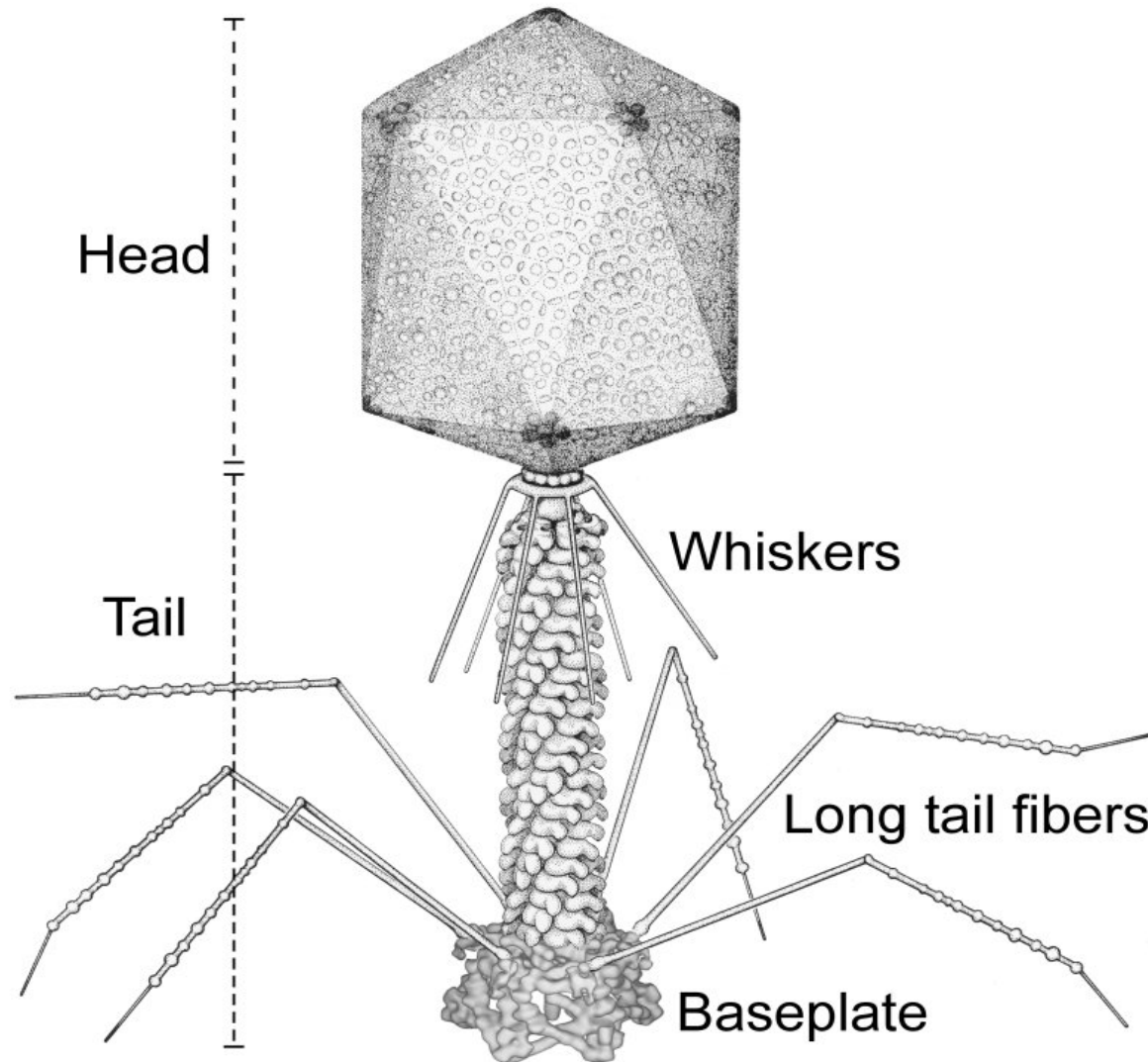# Sequential fitting of E monomer into the immature Dengue cryoEM map

Results are independent of order of fitting

MOL	sumf DI	sumf DII	sumf DIII	x	y	z	θ1	θ2	θ3
A 1st	50.8	55.8	42.3	32.0	-7.7	220.9	15.0	61.0	349.2
A 2nd	49.7	56.4	44.0	31.0	-6.7	221.4	11.0	61.5	345.0
A 3rd	50.9	56.0	40.5	31.5	-6.7	220.4	10.8	61.5	355.2
B 1st	48.4	57.6	42.9	72.1	8.2	210.6	38.0	64.5	162.5
B 2nd	49.8	57.4	41.8	71.6	8.2	210.6	34.8	63.5	164.8
B 3rd	49.7	57.4	41.9	72.1	7.7	210.6	37.5	64.0	163.5
C 1st	48.9	54.7	42.1	10.5	48.3	217.0	19.8	58.0	240.2
C 2nd	49.2	53.1	41.3	9.0	47.8	217.0	22.0	58.5	238.5
C 3rd	49.5	54.9	42.8	10.0	48.3	217.0	18.2	57.0	241,8

Validation

1. Is the hand consistent with each fitted protein?
2. Are distances between atoms in the interface reasonable?
3. Are the type of residues in the contact region appropriate? Look for:
    hydrophobic versus hydrophobic
    charge complimentarity
4. Have all the higher density regions been interpreted?
5. Do unexpected results make chemical sense?

Validation: Consistent hand verification of the cryoEM map
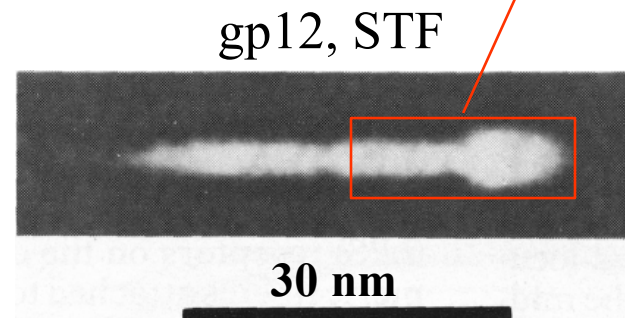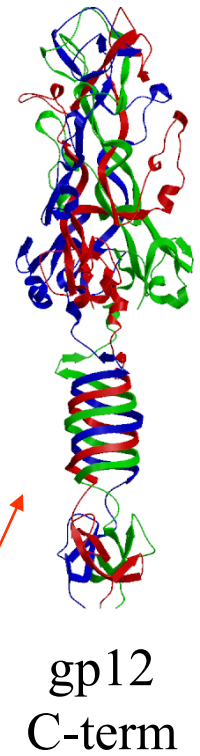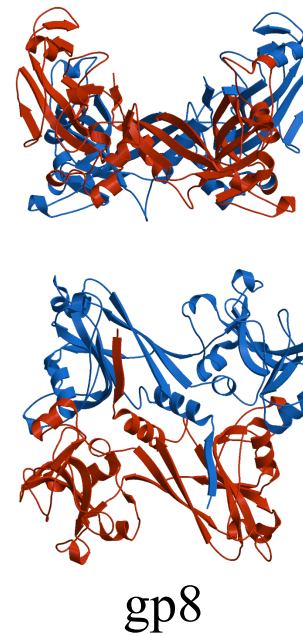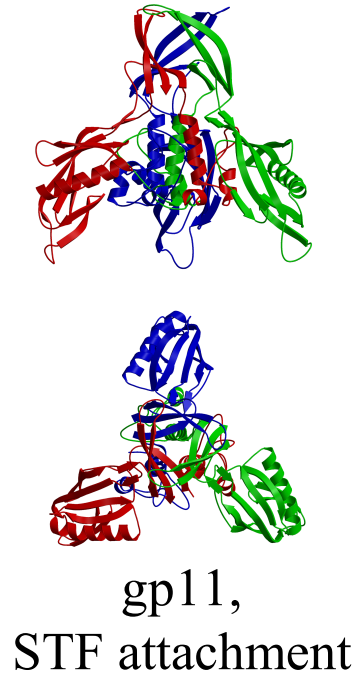# using T4 phage baseplate proteins

Hexagonal conformation (tube-baseplates)

- Initial model – hexagonal prism connected to a tube

- Sixfold symmetry

- 945 particles used in the reconstruction

- Defoci 1.5 – 3.5 μm

- 12 Å resolution

Some crystal structures of the baseplate proteins

gp27
trimer

gp5
OB fold
domain

gp5
Lysozyme
domain

gp5
B−helix
domain

gp5-gp27

gp9,
LTF
attachment

gp11,
STF attachment

gp8

gp12, STF

30 nm

gp12
C-term

19

48 54
6 25 53
9
27   8
5   7
              10
26?   11   12

T4 Hand determination: Un-normalized correlation coefficients

Baseplate protein	Correct hand	Incorrect hand
gp8	1.1	0.7
gp11	0.9	0.7
gp10	1.2	0.7
gp12	1.1	1.0

Validation : Interactions of the E1 and E2 Sindbis virus glycoproteins

E2 unknown structure difference density

E1: known structure was fitted and used to zero out the EM density

Transmembrane region

Validation: Has all of the significant density been interpreted?
Original analysis of Dengue Virus Map at 26Å resolution

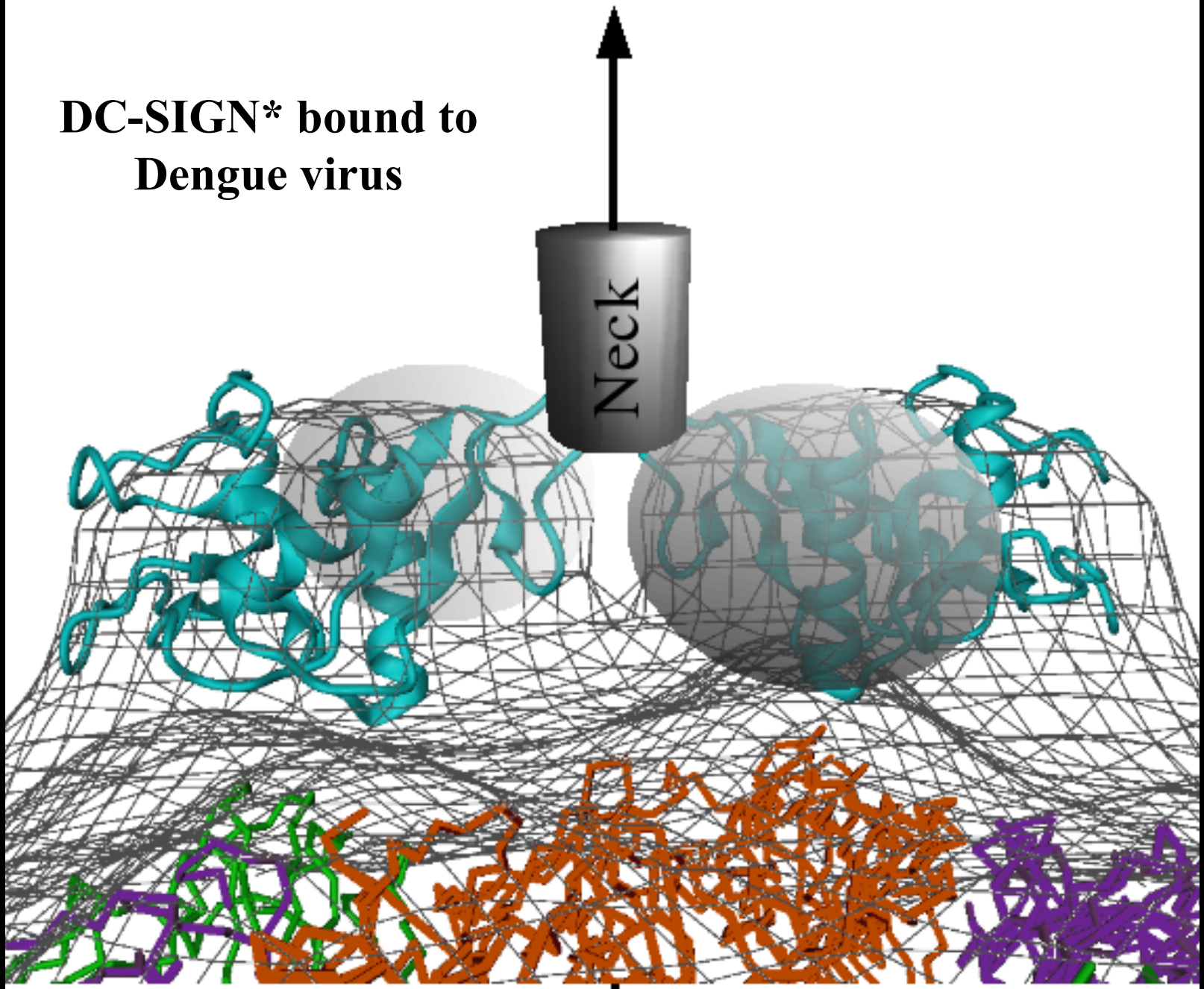| height	ratio1	ratio2
-7		147.0
-6		59.6
-5	129.8	21.7
-4	38.9	12.5
-3	17.9	4.9
-2	11.6	3.5
-1	6.6	1.9
0	5.1	2.7
1	3.4	0.8
2	2.7	0.5
3	2.4	0.3
4	1.8	0.2
5	2.0	0.1
6	1.8	0.1
7	1.9	0.0
8	0.9	0.0
9	2.0	0.0
10	2.3	0.0

Ratio=unused/used pixels
(between radii 230 & 250Å)
Ratio1: after fitting dimer on i2
Ratio2 : after fitting dimer on i2 and q2

Asn 67

Asn 153

Validation: Chemical Reasonableness
Receptor recognition by Dengue virus
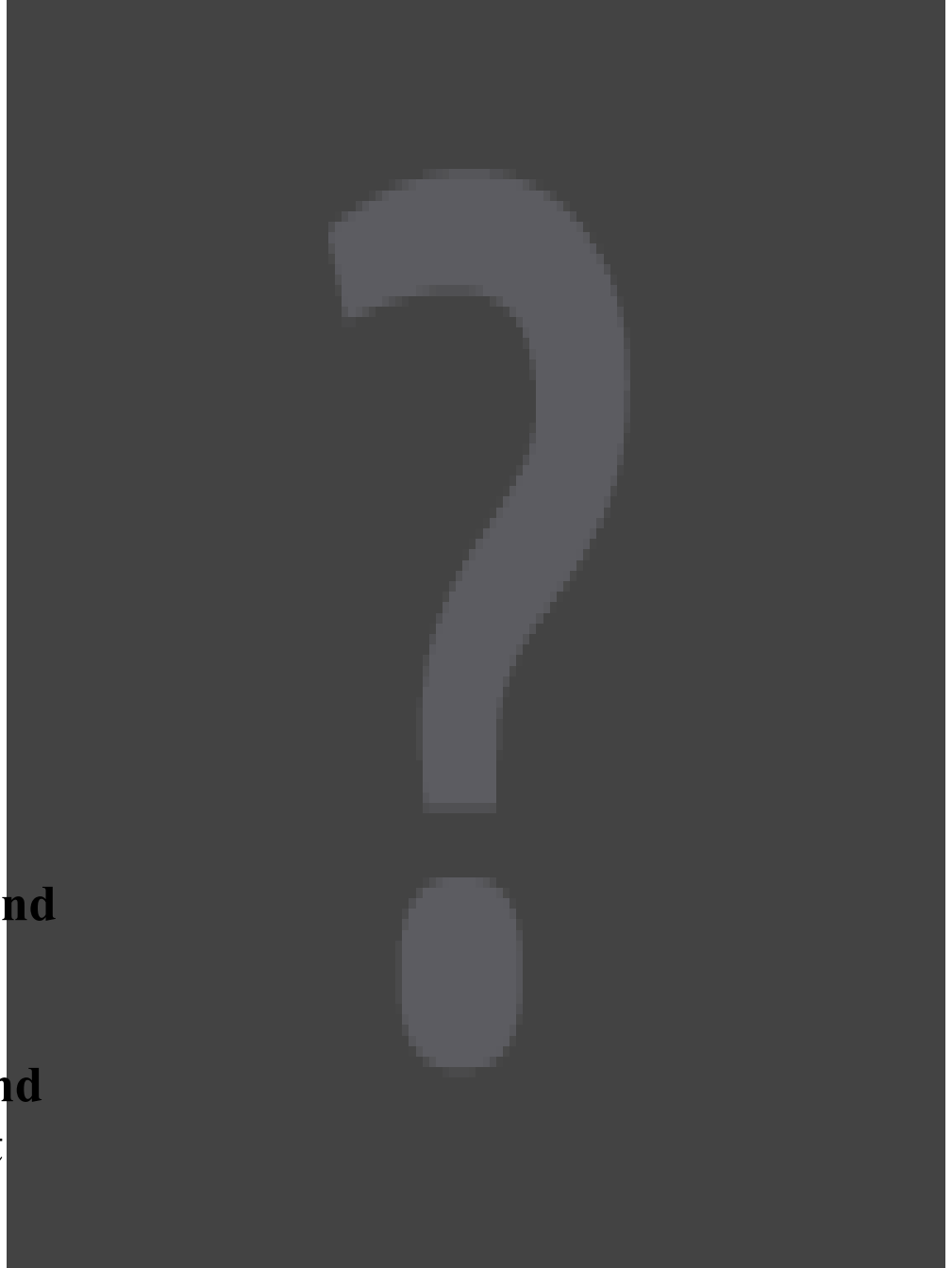
DC-SIGN* bound to Dengue virus

Neck

Other problems:
1. Symmetry missmatches
2. Envelope of proteins whose structure is unknown

1. T4 phage 5-fold head symmetry, 6-fold tail symmetry

2. Yellow are the HOC molecules found by using a HOC$^-$ mutant

3. White are the SOC molecules found by using a HOC$^-$ SOC$^-$ mutant

Fokine et al, PNAS, 2004, **101**:6003-6008\

Relevant references

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Navaza et al, Acta Cryst 2002, **D58**, 1820-1825.

Roseman et al, Acat Cryst 2000, **D56**, 1332-1340.

Rossmann et al, J. Struct Biol. 2001, **136**, 190-200.

Volkmann et al, J. Sruct Biol. 1999, **125**, 176-184.

Wriggers et al., Structure 2001, **9**, 779-788,

Wriggers et al, J. Struct Biol 1999, 125, 185-189.

Acknowledgements