

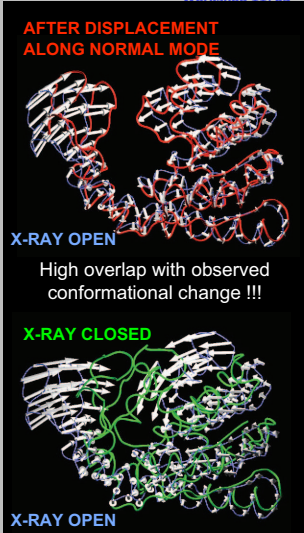
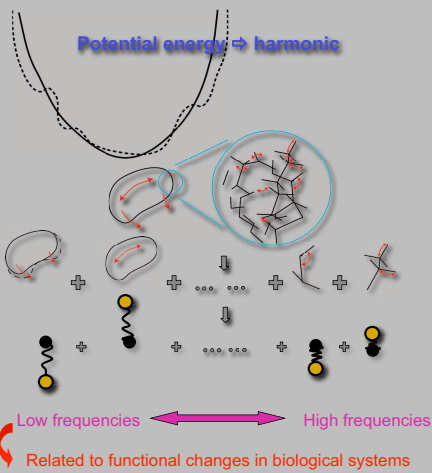
NMFF - Flexible fitting of atomic structures into EM maps

Charles L. Brooks III
(Florence Tama)



Elastic network normal mode analysis - a multi-resolution framework for exploration of large-scale conformational changes

Normal mode analysis



Technical Issues in Normal Mode Computations

$$U(r) \cong \frac{1}{2} \sum_y \frac{\partial^2 U}{\partial r_i \partial r_j} \bigg|_{r=r_0} (r_i - r_i^0)(r_j - r_j^0) \longrightarrow \frac{1}{2} \sum_n \omega_n^2 q_n^2$$

$$\mathbf{H} = \begin{pmatrix} \frac{\partial^2 U}{\partial r_i \partial r_j} \end{pmatrix}$$

Hessian: 2nd derivative of the potential

Eigenvalue problem

$$\mathbf{A}^T \mathbf{H} \mathbf{A} = \mathbf{L}$$

$$\mathbf{A} = (\mathbf{a}_1 \quad \mathbf{a}_2 \quad \dots)$$

$$\mathbf{L} = \begin{pmatrix} \omega_1^2 & & 0 \\ & \omega_2^2 & \\ 0 & & \ddots \end{pmatrix}$$

Eigenvector = normal mode

Eigenvalue = frequency

Technical Issues in Normal Mode Computations

$$U(r) \cong \frac{1}{2} \sum_y \frac{\partial^2 U}{\partial r_i \partial r_j} \bigg|_{r=r_0} (r_i - r_i^0)(r_j - r_j^0) \longrightarrow \frac{1}{2} \sum_n \omega_n^2 q_n^2$$

$$\mathbf{H} = \begin{pmatrix} \frac{\partial^2 U}{\partial r_i \partial r_j} \end{pmatrix}$$

Hessian: 2nd derivative of the potential

Problems with large biological systems

Minimization

Eigenvalue problem

$$\mathbf{A}^T \mathbf{H} \mathbf{A} = \mathbf{L}$$

Size of the system (3Nx3N)

$$\mathbf{A} = (\mathbf{a}_1 \quad \mathbf{a}_2 \quad \dots)$$

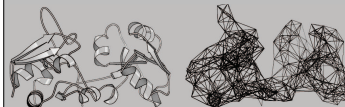
$$\mathbf{L} = \begin{pmatrix} \omega_1^2 & & 0 \\ & \omega_2^2 & \\ 0 & & \ddots \end{pmatrix}$$

Eigenvector = normal mode

Eigenvalue = frequency

Elastic network normal mode analysis

Minimization => Tirion Potential (*)



$$E(r_a, r_b) = \frac{C}{2} (|r_{a,b}| - |r_{a,b}^0|)^2$$

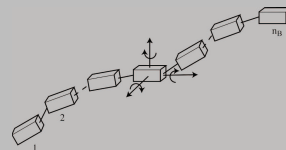
Hookean potential

- > No minimization
- > Coarse grained model => C α atoms

$$E_p = \sum_{a,b} E(r_a, r_b) \begin{cases} 1 \rightarrow r_{a,b}^0 \leq R_{cut} \\ 0 \rightarrow r_{a,b}^0 \geq R_{cut} \end{cases}$$

Cutoff for network elastic bonds

Diagonalization of Hessian => RTB (Rotation Translation Blocks) method (**)



- block = 1 or several residues treated as rigid body
- rotation + translation of block => new basis
- expression of Hessian in this new basis
- Diagonalization of a matrix $6n_b * 6n_b$

* Tirion MM (1996) *Phys Rev Lett.* **77**, 1905-1908

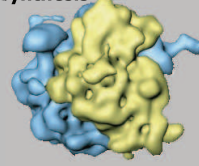
** Tama et al. (2000) *Proteins*

Elastic network normal mode analysis

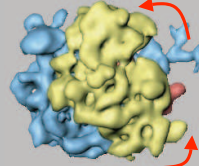
- Determining the constants for ENNMA
 - $R_{cut} \rightarrow 2^{nd}$ minimum in (pseudo)atom - atom(pseudo) distribution function
 - 4.5 Å heavy atoms, 7-8 Å $C\alpha-C\alpha$, 10-12 Å P-P (DNA/RNA), 10-12 Å $C\alpha-P$ (protein-na)
 - Can be as large as 15-25 Å for really coarse-grained models
 - Level of RT-block coarsening
 - Varies depending on system
 - Residue for proteins (aa), 1-5 (or more) for $C\alpha/P$ in small complexes, larger, e.g., 1 per protein, in large structures like viruses

Large-scale conformational changes

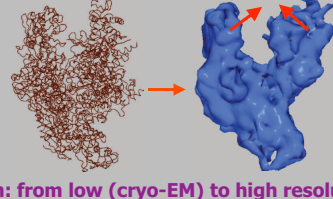
Ribosome: protein synthesis



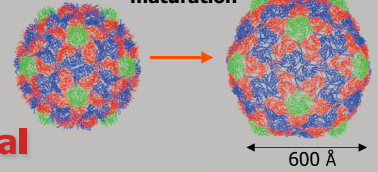
Functional motions



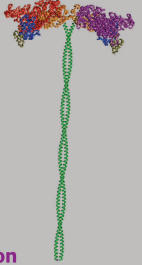
RNA polymerase: transcription



Virus maturation



Mycosin II inhibition



> Time scale (> ms)

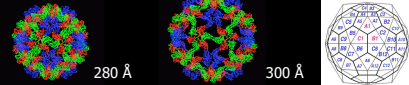
> Structural information: from low (cryo-EM) to high resolution

Exploring macromolecular machines with ENNMA - virus capsids

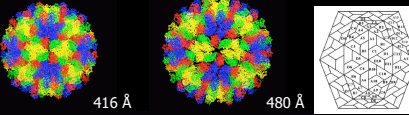
Tama & Brooks, *JMB*, (2002); *ibid* (2005).

Exploring large-scale conformational changes in virus maturation

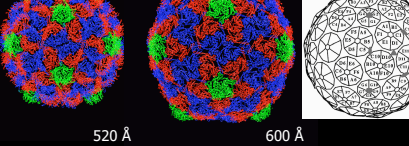
CCMV T=3



NoV T=4



HK 97 T=7



> Large conformational changes observed for several viruses

> Icosahedral symmetry

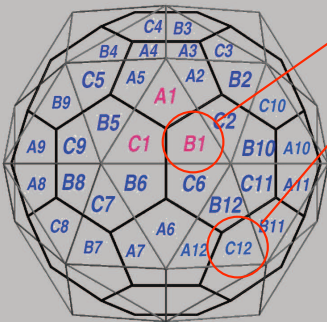
> Normal mode analysis

- well reproduces conformational change of a small virus CCMV

- do different motions characterize dynamics of viruses with different quasi-equivalent symmetries?
<http://viperdb.scripps.edu>

Normal mode analysis applied to viruses

Coarse grained model: $C\alpha$ atoms + RTB method \rightarrow one protein = one block



Rotation + Translation of blocks \Rightarrow new basis

Projection of the Hessian

Diagonalization of matrix

T=3 \Rightarrow 1080 x 1080

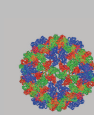
T=4 \Rightarrow 1440 x 1440

T=7 \Rightarrow 2520 x 2520

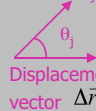
T=13 \Rightarrow 5040 x 5040

How well is the conformational change described?

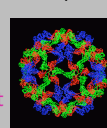
Native



Normal Mode a_j



Procapsid



$$\text{overlap}_j = \frac{a_j \cdot \Delta r}{|\Delta r| |a_j|}$$

$\sum \text{overlap}^2$

> Represents 95% of the conformational change

> CCMV and native NoV \Rightarrow one predominant mode accounts for more than 90% of the conformational change.

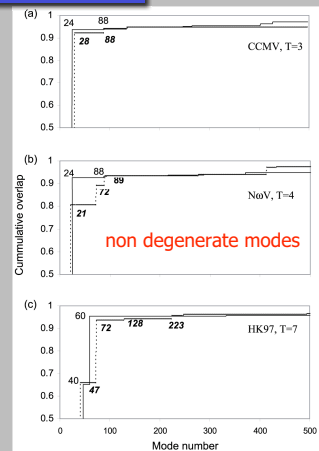
> HK97 \Rightarrow first mode only 65%.

> First mode is well conserved between the two states

Overlap CCMV \Rightarrow 0.99

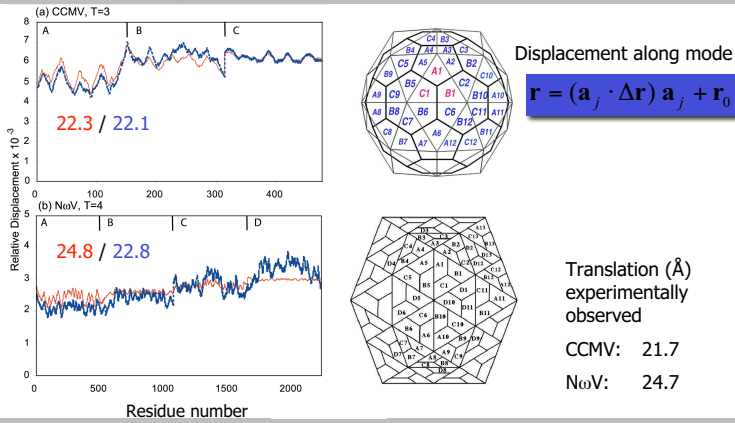
NoV \Rightarrow 0.91

HK97 \Rightarrow 0.97



Nature of the low-frequency normal modes T=3/T=4

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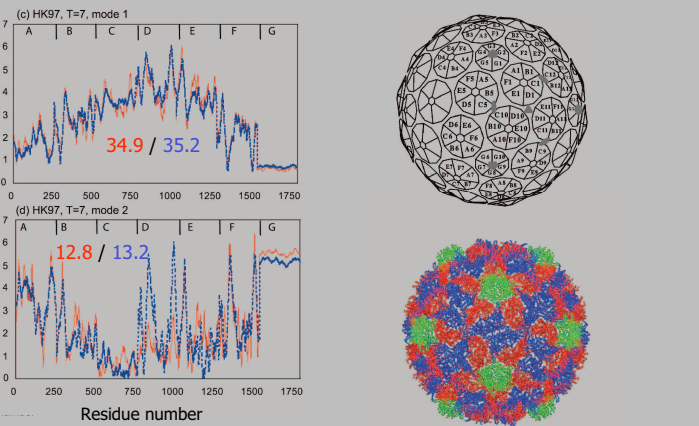


Lowest frequency mode captures the overall translation of the asymmetric unit

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Nature of the low-frequency normal modes: HK97

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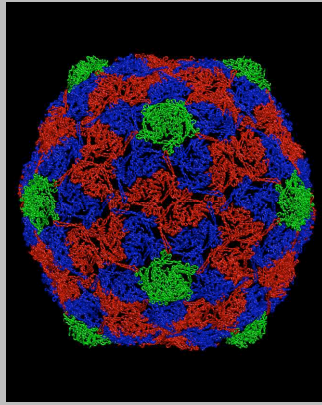
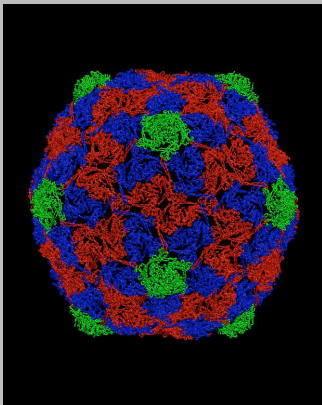
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HK97

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Prohead II: Mode 1

Head II: Mode 2



Necessary to achieve the shape transition

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Summary - virus dynamics

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- HK97: a pair of low frequency normal modes is necessary to produce the non-uniform conformational transition
- NoV and CCMV: one normal mode provides the nearly uniform overall translation associated with the conformational transition
- capsid shell is not mechanically uniform, especially for viruses of higher complexity such as T=7 and T=13 viruses
- pentameric units display higher flexibility

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"Practical" tools for structural biology based on ENNMA

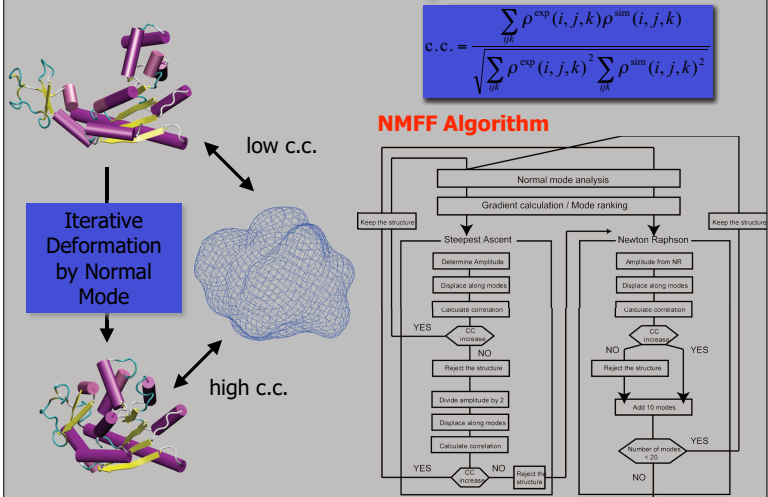
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- By exploiting the low-dimensionality of the space required to achieve functionally relevant spatial reorganization we can develop lower-resolution structure refinement/fitting methodologies
- Normal Mode Flexible Fitting for flexibly fitting atomic models into low resolution structural data from cryo-EM

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Normal Mode Flexible Fitting

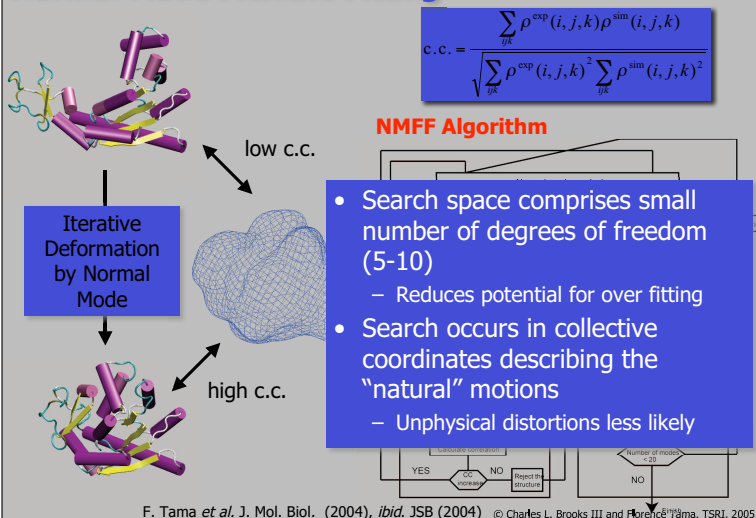
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F. Tama et al. J. Mol. Biol. (2004), *ibid.* JSB (2004) © Charles L. Brooks III and Florence Tama, TSRI, 2005

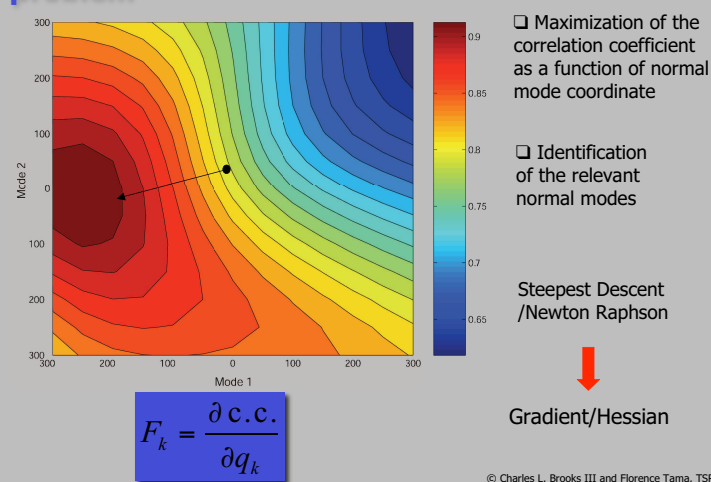
Normal Mode Flexible Fitting

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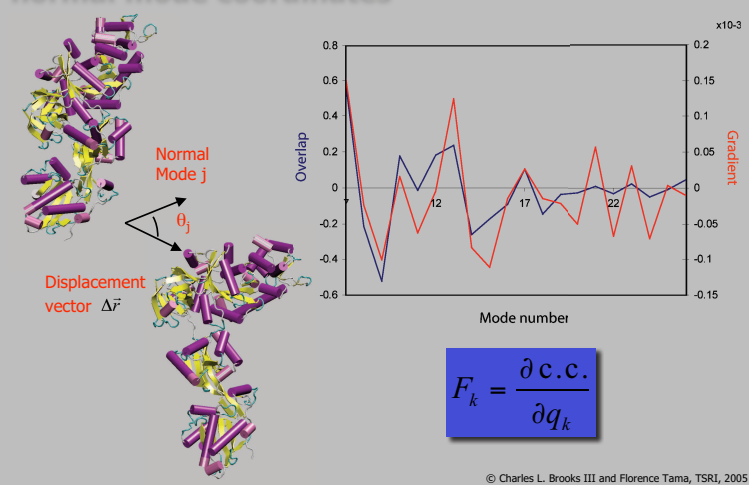
Correlation coefficient: Maximization problem

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Derivative of correlation coefficient by normal mode coordinates

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Flexible fitting results

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Initial structure	Atoms included	Resolution (Å)	Final RMSD (Å)		
			Lactoferrin	EF2	Ca ²⁺ -ATPase
RMSD fitted structure	All atoms	10	0.8 (1.4)	1.8 (2.1)	4.3 (4.9)
	All atoms	20	1.1 (1.5)	2.1 (2.3)	5.0 (5.6)
	All atoms	30	1.4 (1.9)	2.6 (3.1)	5.0 (5.5)
Situs rigid body*	C α atoms	10	1.0	1.8	5.1
	C α atoms	20	1.3	2.2	4.7
	C α atoms	30	1.8	2.8	5.4
Original RMSD (Å)	All atoms	10	0.9 (1.4)	2.1 (2.3)	4.5 (5.0)
	All atoms	20	1.0 (1.5)	2.2 (2.4)	4.9 (5.5)
	All atoms	30	1.4 (1.8)	2.9 (3.0)	5.2 (5.7)
Original RMSD (Å)	C α atoms	10	1.2	1.9	4.8
	C α atoms	20	1.4	2.2	4.7
	C α atoms	30	2.0	2.6	5.2
Original RMSD (Å)			6.5	14.6	14.4

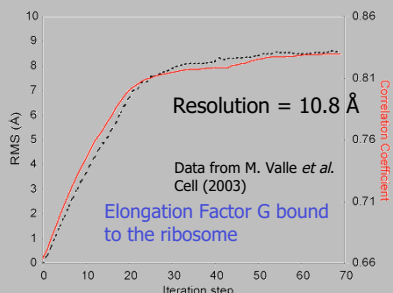
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Simple example flexible refinement

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<http://mmtsb/scrpps.edu/software/nmff.html>

Flexible refinement of atomic structures into low-resolution EM maps using elastic network normal modes



F. Tama *et al.*, J. Struct. Biol. (2004)

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Examples of NMFF refinement in model building and interpretation of structural data

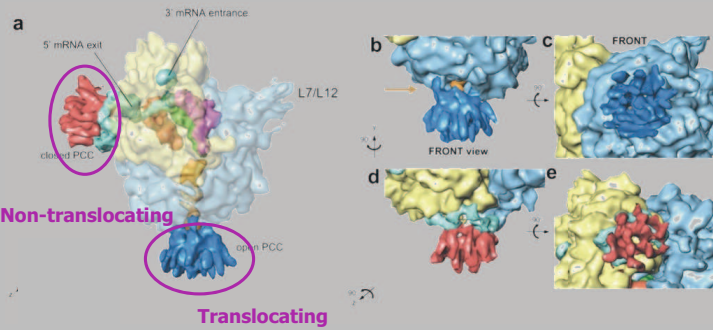
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E-coli protein conducting channel bound to a translating ribosome

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Structure at ~ 12 Å resolution



Dimeric structures

K. Mitra, C. Scaffitzel, T. Shaikh, F. Tama, S. Jenni, CL. Brooks III, N. Ban and J. Frank. *Nature* (2005)

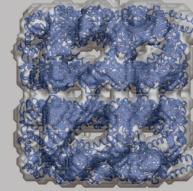
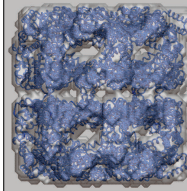
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13 Å structure of a chaperonin GroEL-protein substrate complex

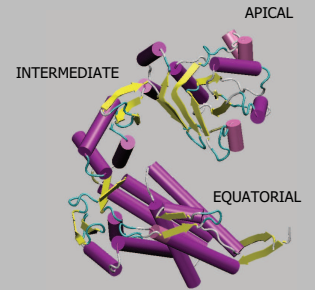
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GroEL - substrate free (map at 12Å)

GroEL with bound E coli glutamine synthetase (GS) (map 13Å)



Conformational difference



Fitting performed from 10EL using NMFF with 7-fold symmetry imposed.

Some residues move by ~ 7Å in the apical domain

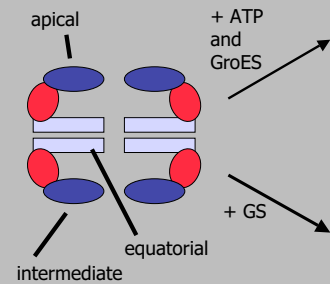
S. Falke, F. Tama, CL. Brooks III, EP. Gogol and MT. Fisher. *J. Mol. Biol.* (2005)

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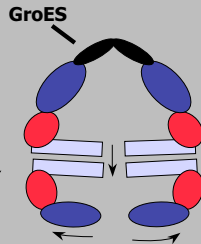
GroEL-GroES-ADP versus GroEL-GS

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GroEL



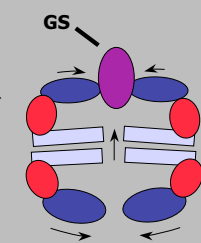
+ ATP and GroES



GroEL-GroES-ADP

- equatorial domains maintain contact => the movements in cis lead to movements of the opposite trans apical domain.

+ GS



GroEL-GS

- equatorial domains maintain contact
- movements opposite those observed with GroEL-ES

Binding of GS imparts dramatic effects on the opposite ring

S. Falke, F. Tama, CL. Brooks III, EP. Gogol and MT. Fisher. *J. Mol. Biol.* (2005)

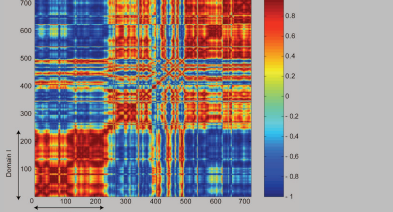
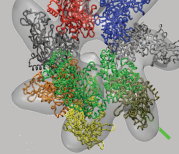
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Anthrax toxic complex

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Initial fit

Protective Antigen heptamer



F. Tama, G. Ren, S.H. Leppla, CL. Brooks III and A.K. Mitra to be submitted

Structure obtained with NMFF

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Red Clover Necrotic Mosaic Virus

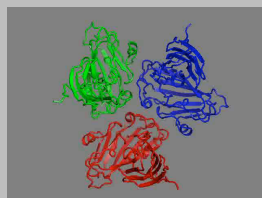
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Homology model



Fitting

Native to EDTA treated virions



Extraction of ions alters the conformation of the capsid that generates channel through which the genomic RNA is likely to be released

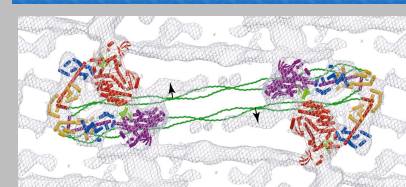
M. B. Sherman, R. H. Guenther, F. Tama, C. L. Brooks, A. M. Mikhailov, E. V. Orlova, T. S. Baker, and S. A. Lommel. *Submitted to Mol Cell.*

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Refinement of HMM

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Transition between active and inhibited myosin



F. Tama, M. Feig, J. Liu, CL. Brooks III, KA. Taylor *J. Mol. Biol.* (2005)

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Flexible Fitting - Summary

- Uses small number of collective (functionally relevant) independent coordinates to optimize cc
 - Minimizes problems of over-fitting
- Can be used at multiple levels of coarse-graining for optimal model to accommodate data
 - Multi-resolution through RTB as well as pseudo-atomic elastic networks
- Employs symmetry to permit symmetric assemblies to be modeled from asymmetric unit
- Free and available at:

<http://mmtsb.scripps.edu/nmff.html>

Summary

- Elastic network normal mode analysis provides a multi-resolution approach for exploring functional reorganization of biological assemblies
 - Nature exploits the overall all shape of her biological machines to provide robustness in functional reorganization
- NMFF can be used in conjunction with known atomic level structures and lower resolution data to explore functional rearrangements of biological assemblies as observed by cryo-EM and related low resolution methods

Acknowledgments

Florence Tama (U of AZ), Michael Feig (MSU), Osamu Miyashita (U of AZ), Jack Johnson, Vijay Reddy, Joachim Frank (HHMI), Alok Mitra (Auckland), Mark Fisher (KU), Ed Gogel (UM-KC), Tim Baker (UCSD)