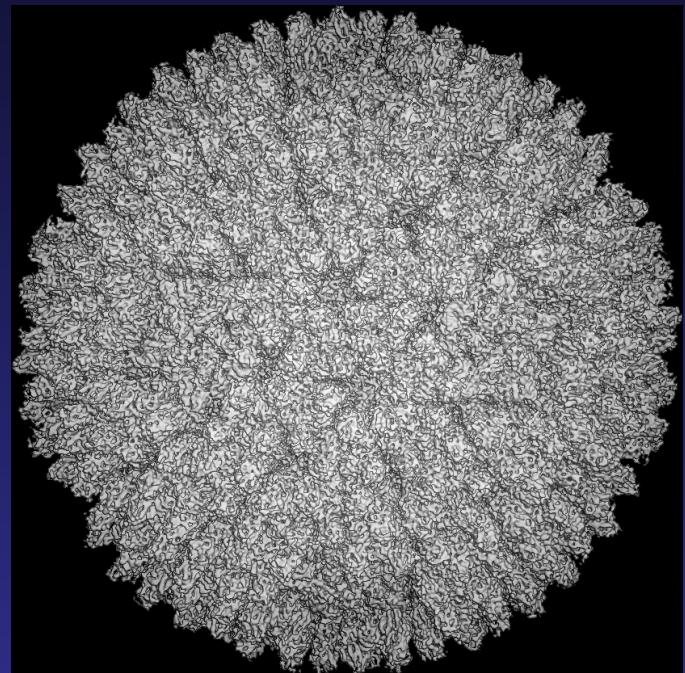
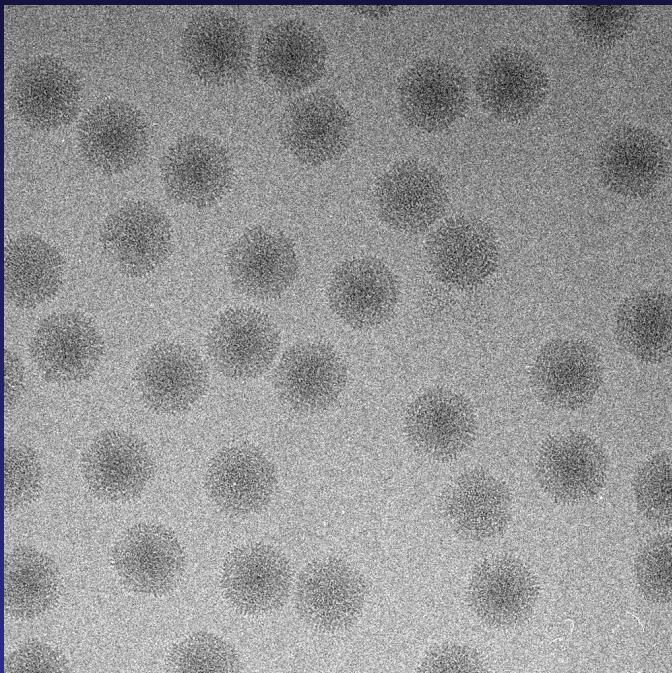


3D Reconstruction of Icosahedral Particles



3D Reconstruction of Icosahedral Particles

Outline

- Background

- References; examples; etc.

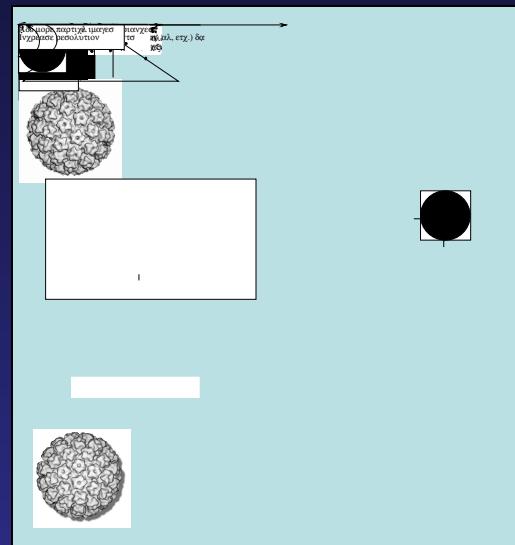
- Symmetry

- Icosahedral (532) point group symmetry
- Triangulation symmetry

- “Typical” procedure (flow chart)

- Digitization and boxing
- Image preprocessing / CTF estimation
- Initial particle orientation/origin search
- Orientation/origin refinement
- 3D reconstruction with CTF corrections
- Validation (resolution assessment)

- Current and future strategies



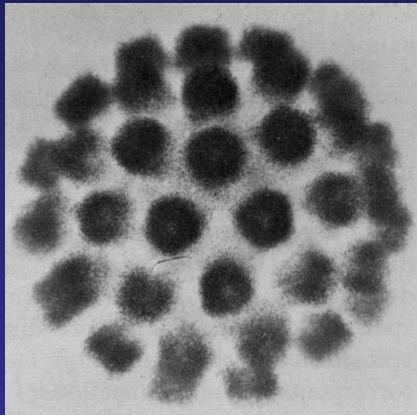
3D Reconstruction of Icosahedral Particles

REFERENCES

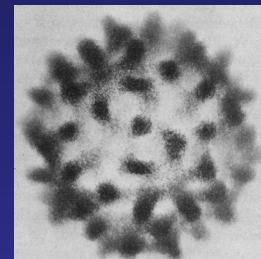
Crowther, R. A., Amos, L. A., Finch, J. T., DeRosier, D. J. and Klug, A. (1970) Three dimensional reconstructions of spherical viruses by Fourier synthesis from electron micrographs. *Nature* **226**:421-425

First 3D reconstructions of negatively-stained,
spherical viruses:

Human wart virus



Tomato bushy stunt



500 Å

3D Reconstruction of Icosahedral Particles

REFERENCES

Crowther, R. A., DeRosier, D. J. and Klug, A. (1970) The reconstruction of a three-dimensional structure from projections and its application to electron microscopy. *Proc. Roy. Soc. Lond. A* **317**:319-340

Crowther, R. A. (1971) Procedures for three-dimensional reconstruction of spherical viruses by Fourier synthesis from electron micrographs. *Phil. Trans. R. Soc. Lond. B.* **261**:221-230

General principles of 3DR method

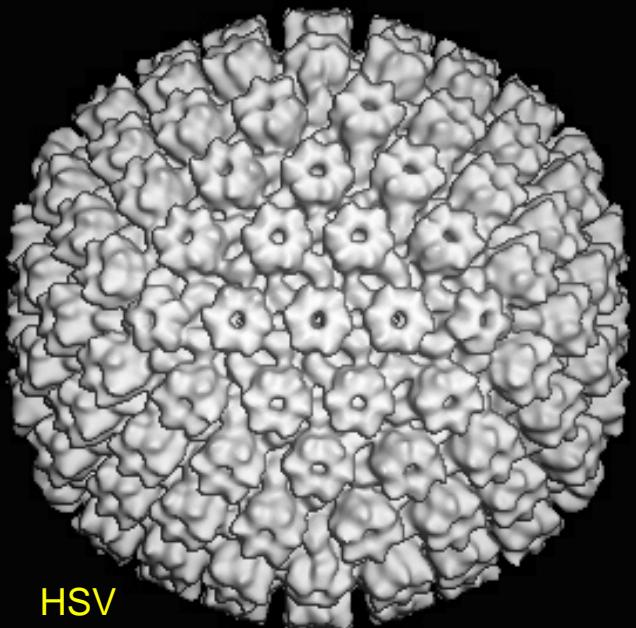
- Fourier-Bessel mathematics
- Common lines

3D Reconstruction of Icosahedral Particles

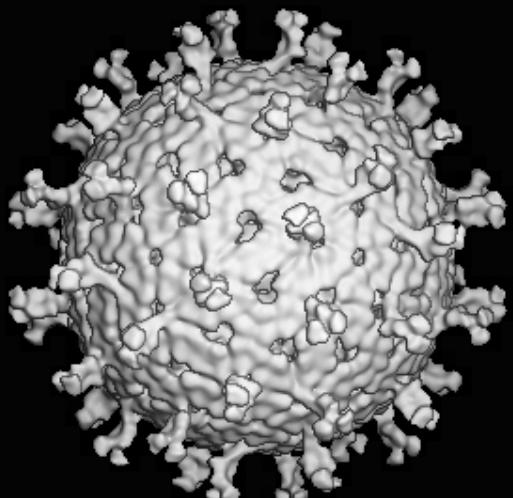
REFERENCES

- Reference list available as handout
- For die-hards:

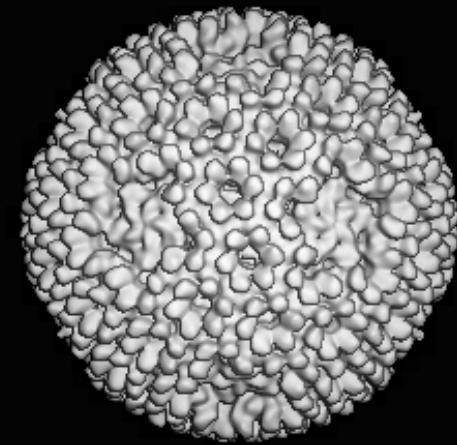
Baker, T. S., N. H. Olson, and S. D. Fuller (1999) Adding the third dimension to virus life cycles: Three-Dimensional reconstruction of icosahedral viruses from cryo-electron micrographs. *Microbiol. Molec. Biol. Reviews* **63**:862-922



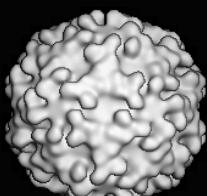
HSV



Rotavirus



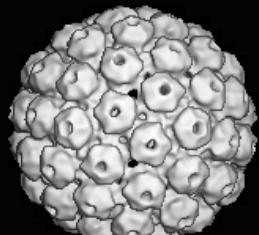
Reovirus



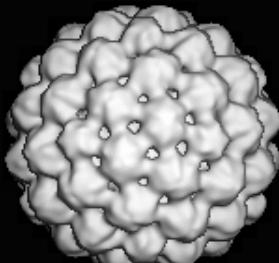
NoV



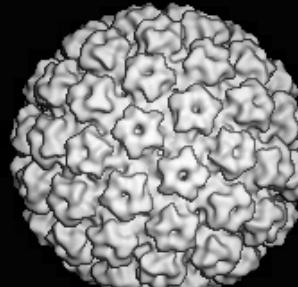
LA-1



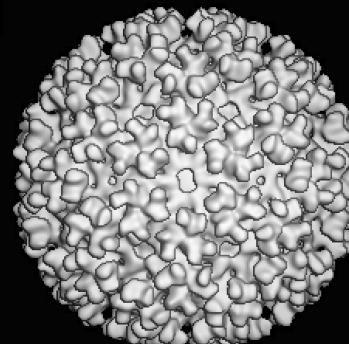
Polyoma



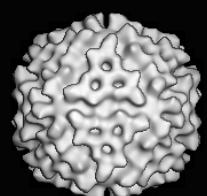
CaMV



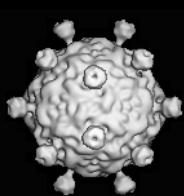
HPV



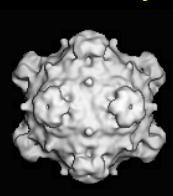
Ross River



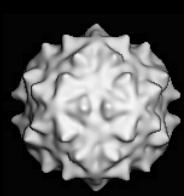
N β V



SpV-4



ϕ X174



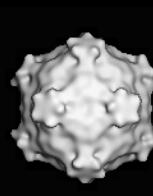
FHV



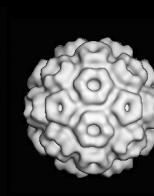
HRV-14



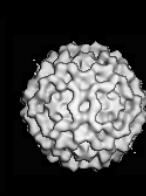
Polio



CPMV

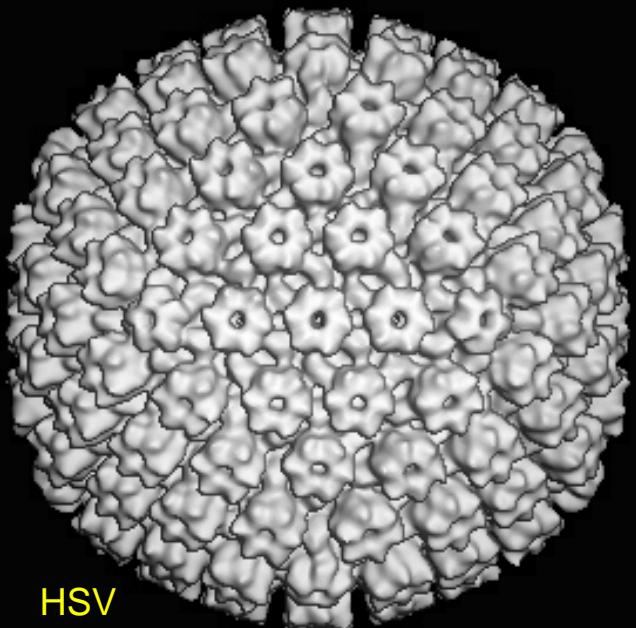


CCMV

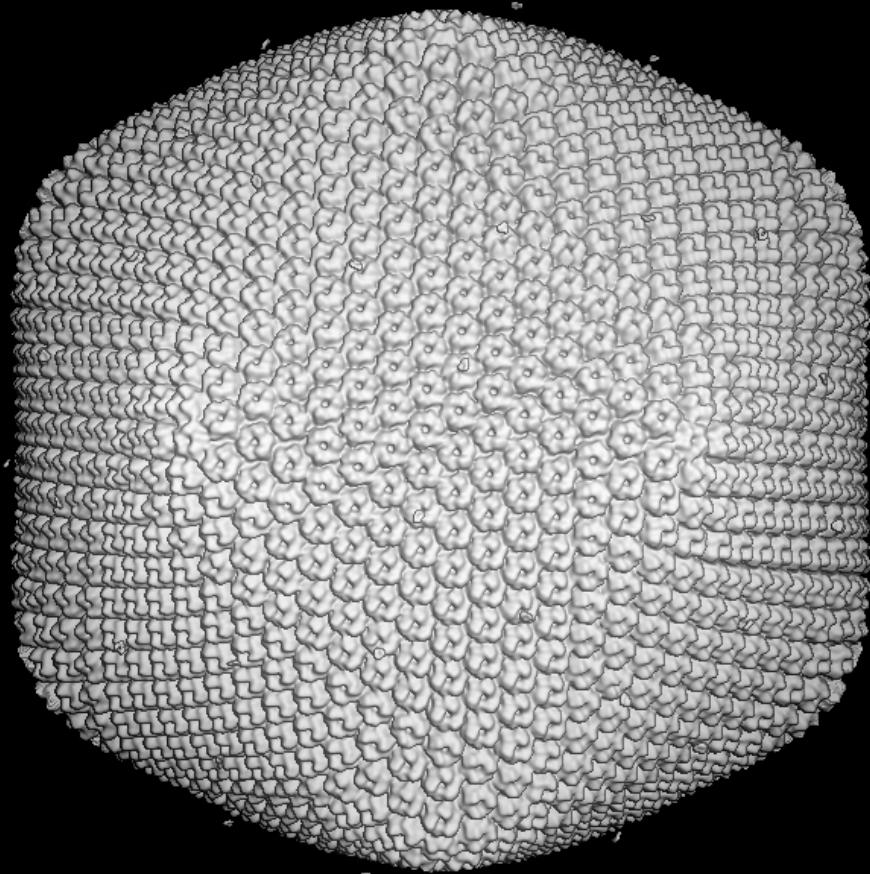


B19

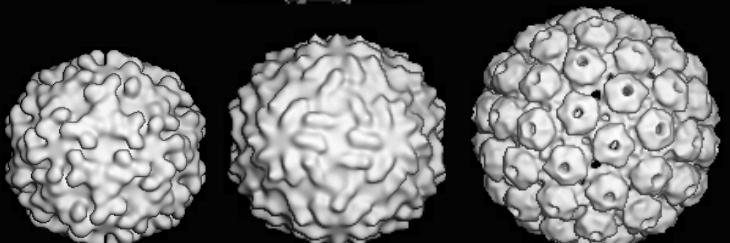
500 Å



HSV



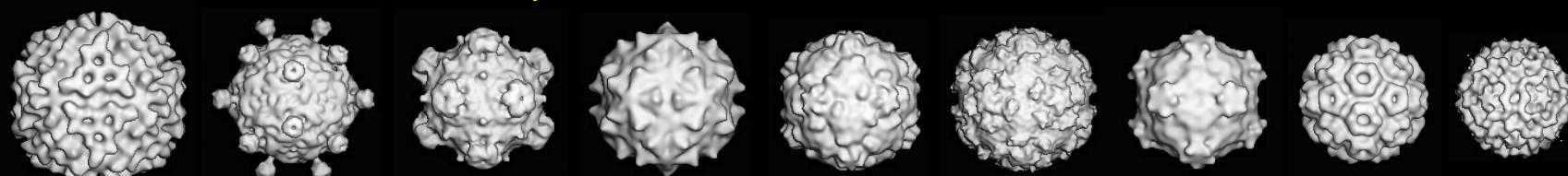
PBCV-1



N ω V

LA-1

Polyoma



N β V

SpV-4

ϕ X174

FHV

HRV-14

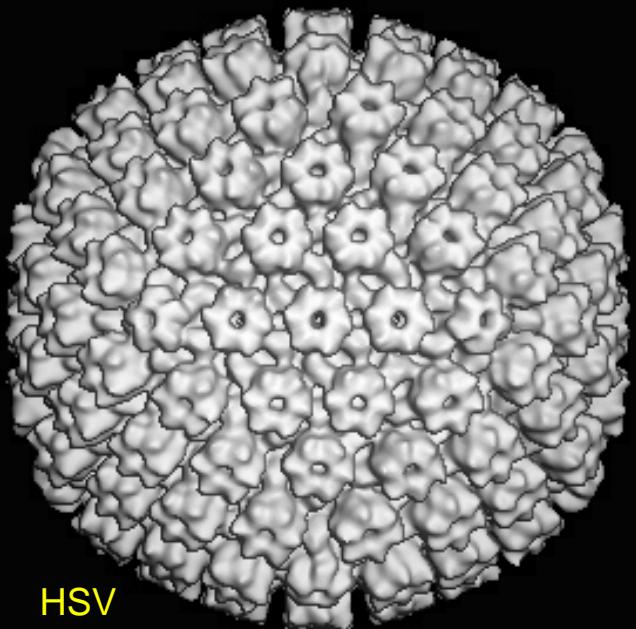
Polio

CPMV

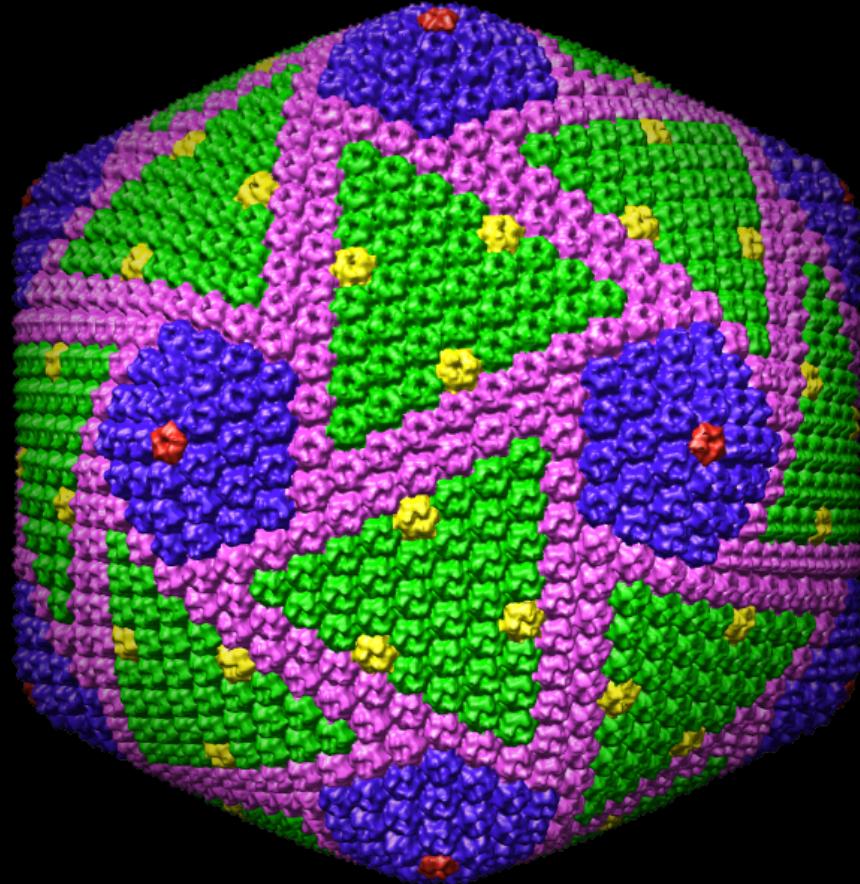
CCMV

B19

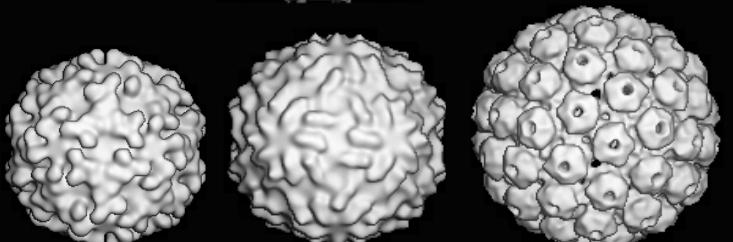
500 Å



HSV



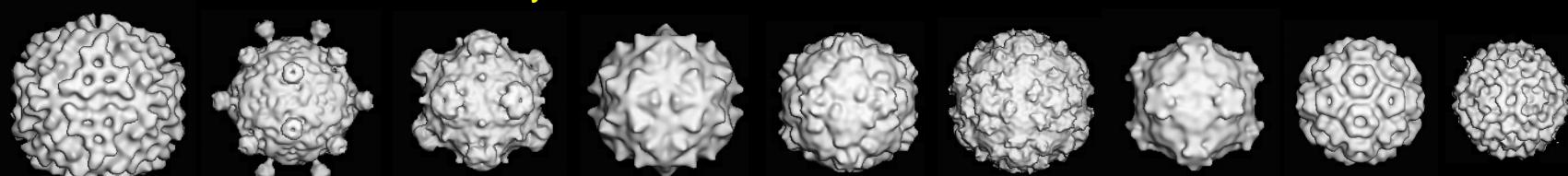
PBCV-1



NoV

LA-1

Polyoma



N β V

SpV-4

ϕ X174

FHV

HRV-14

Polio

CPMV

CCMV

B19

500 Å

3D Reconstruction of Icosahedral Particles

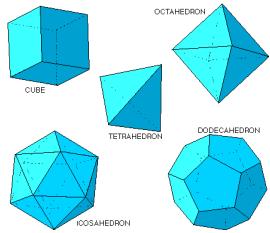
Outline

- Background
 - References; examples; etc.
- Symmetry
 - Icosahedral (532) point group symmetry
 - Triangulation symmetry
- “Typical” procedure (flow chart)
 - Digitization and boxing
 - Image preprocessing / CTF estimation
 - Initial particle orientation/origin search
 - Orientation/origin refinement
 - 3D reconstruction with CTF corrections
 - Validation (resolution assessment)
- Current and future strategies

3D Reconstruction of Icosahedral Particles

Symmetry

- 1. Icosahedral (532) point group symmetry
- 2. Triangulation symmetry

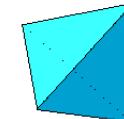


Regular Polyhedra

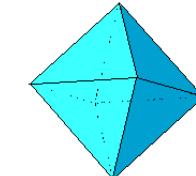
(Platonic Solids)

There are just five platonic solids:

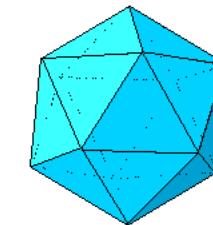
From **equilateral triangles** you can make:
with 3 faces at each vertex, a **tetrahedron**



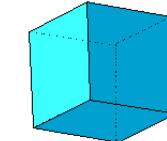
with 4 faces at each vertex, an **octahedron**



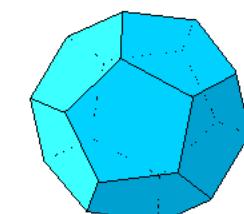
with 5 faces at each vertex, an **icosahedron**



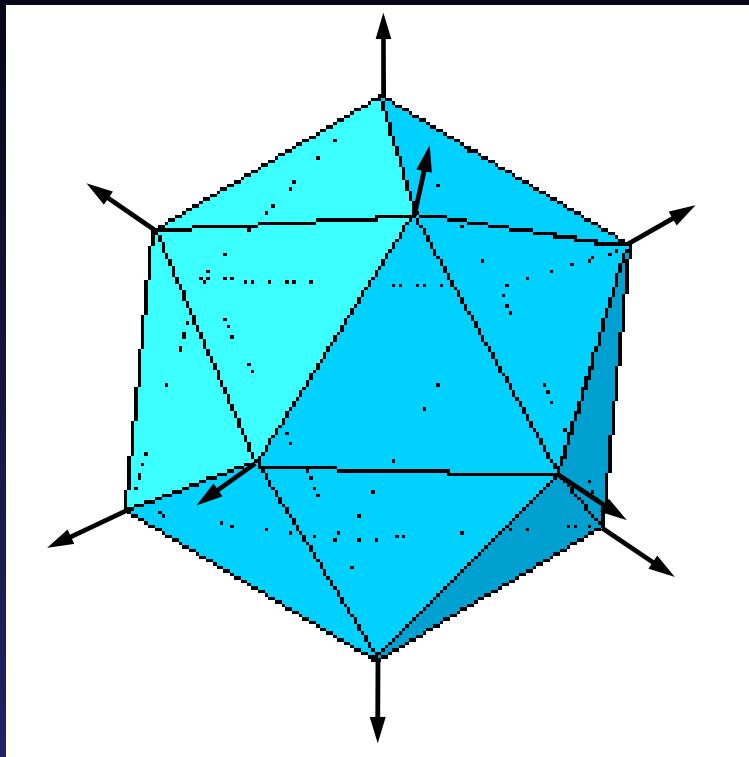
From **squares** you can make:
with 3 faces at each vertex, a **cube**



From **pentagons** you can make:
with 3 faces at each vertex, a **dodecahedron**

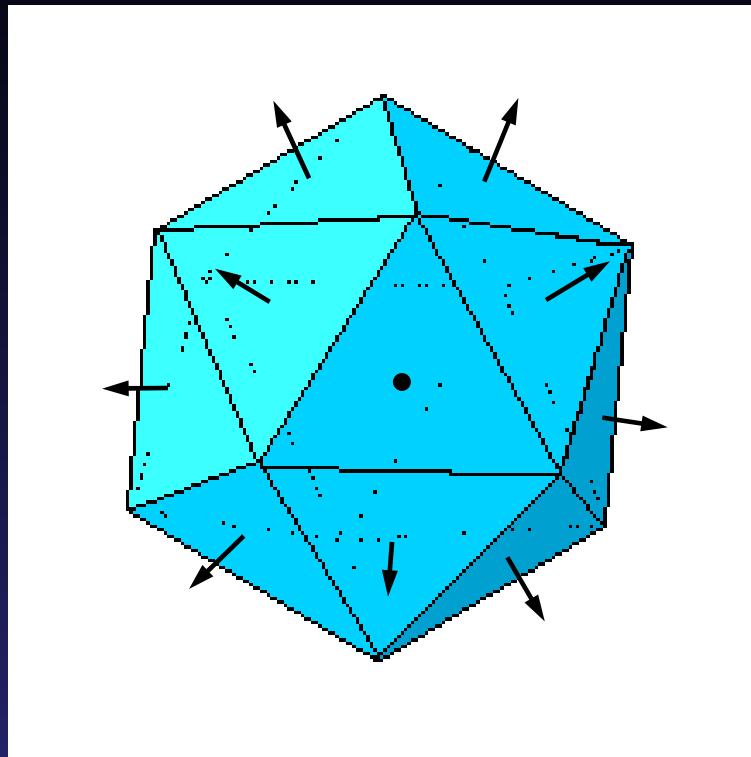


Icosahedral (532) Point Group Symmetry



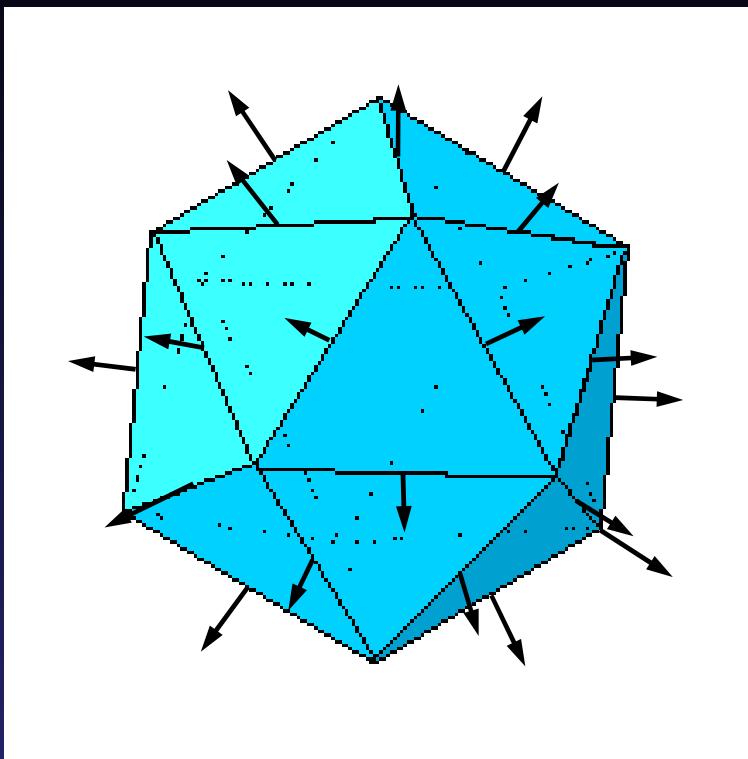
12 vertices (5-fold)

Icosahedral (532) Point Group Symmetry



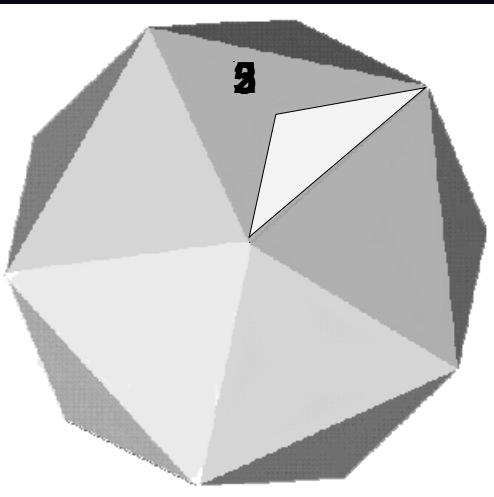
12 vertices (5-fold)
20 faces (3-fold)

Icosahedral (532) Point Group Symmetry

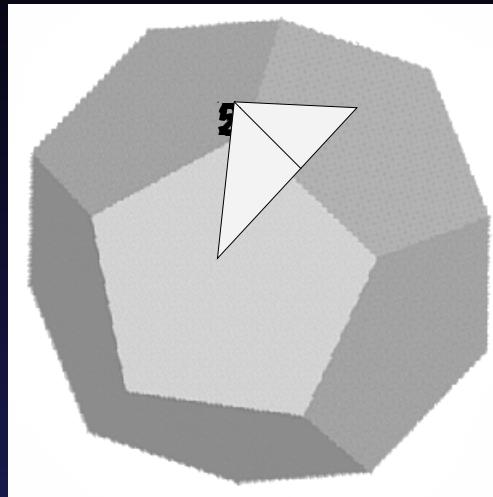


12 vertices (5-fold)
20 faces (3-fold)
30 edges (2-fold)

Icosahedron



Dodecahedron



Different shapes, but both have 532 symmetry

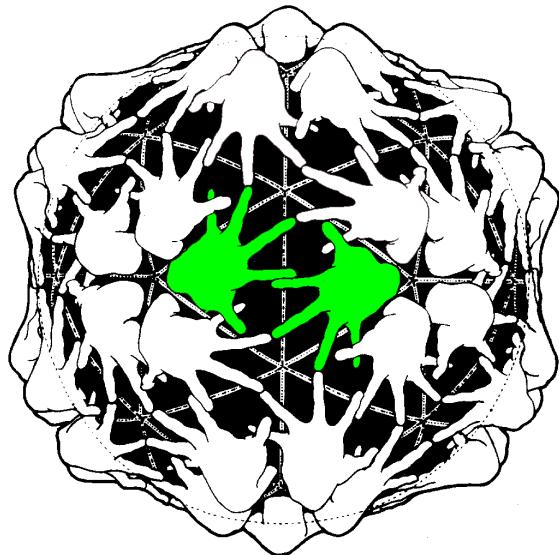
12 vertices, 20 faces, 30 edges
(6 5-folds, 10 3-folds, 15 2-folds)

20 vertices, 12 faces, 30 edges
(10 3-folds, 6 5-folds, 15 2-folds)

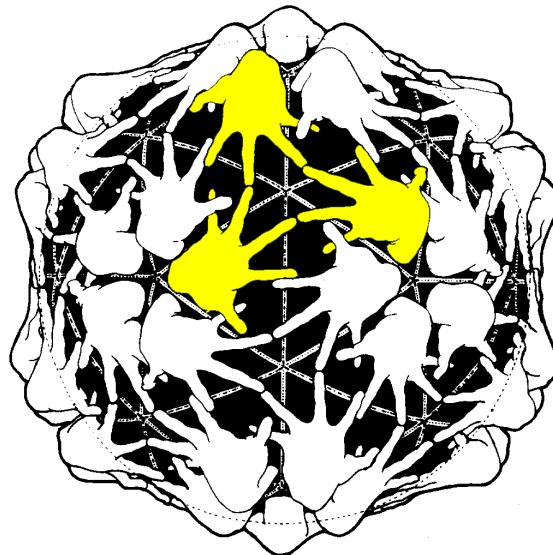
Asymmetric unit is 1/60th of whole object

Object consists of 60 identical ‘subunits’ arranged with icosahedral symmetry

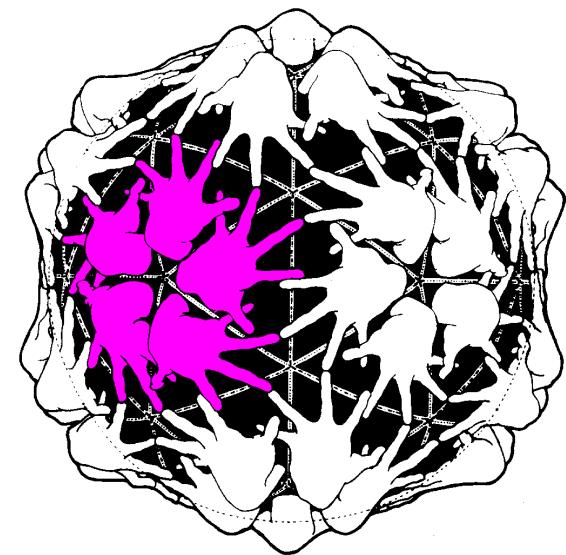
Icosahedral (532) Point Group Symmetry



30 dimers



20 trimers



12 pentamers

3D Reconstruction of Icosahedral Particles

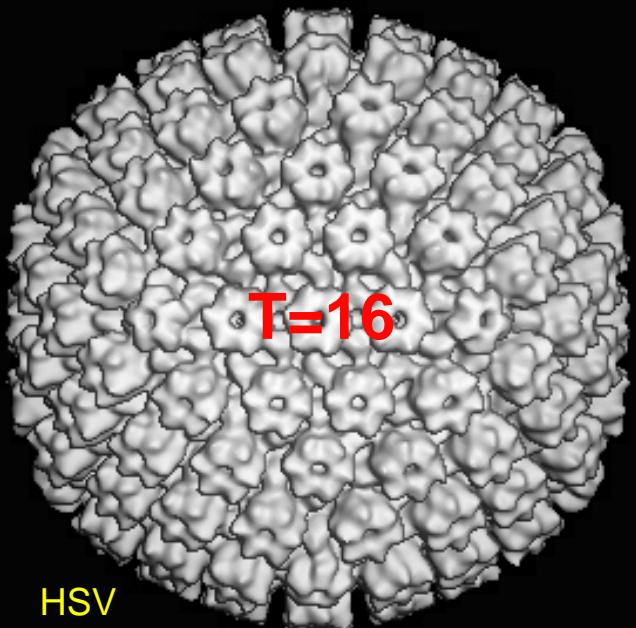
Symmetry

- 1. Icosahedral (532) point group symmetry
- 2. Triangulation symmetry

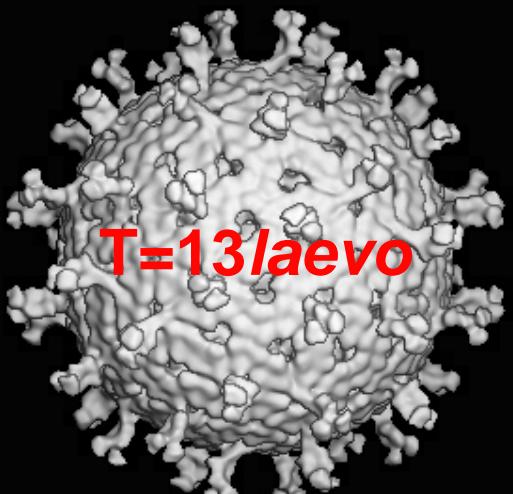
Purely mathematical concept (concerns lattices)

Real objects (e.g. viruses) with 532 symmetry often consist of multiples of 60 ‘subunits’

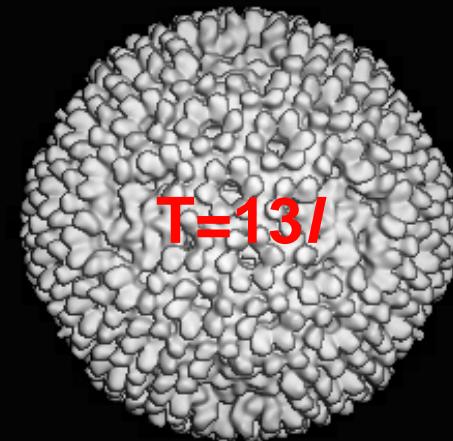
‘Subunits’ arranged such that additional, local or pseudo-symmetries exist



HSV



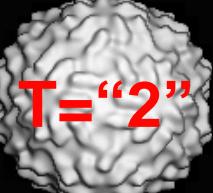
Rotavirus



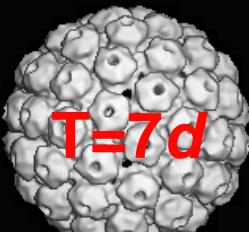
Reovirus



N ω V



LA-1



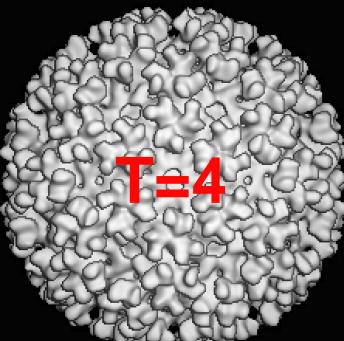
Polyoma



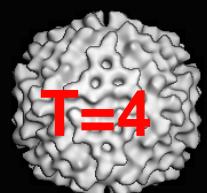
CaMV



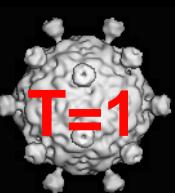
HPV



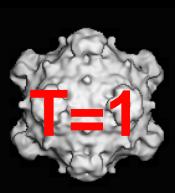
Ross River



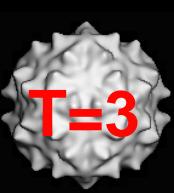
N β V



SpV-4



ϕX174



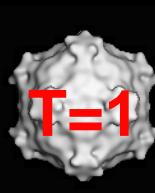
FHV



HRV-14



Polio



CPMV

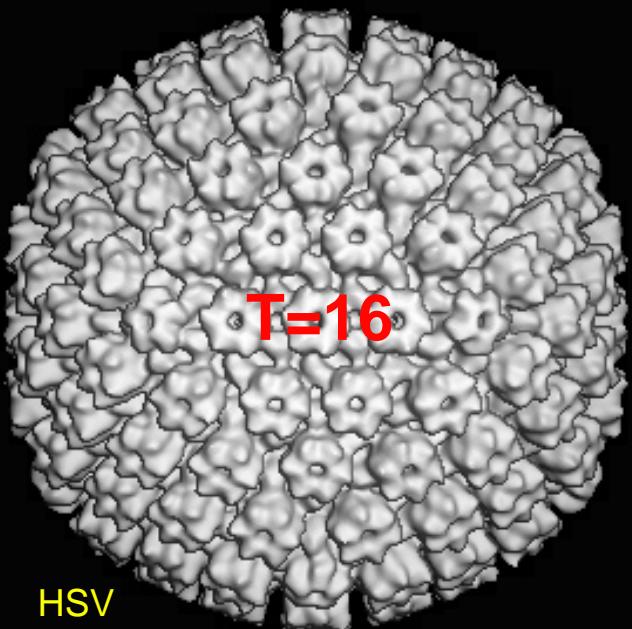


CCMV

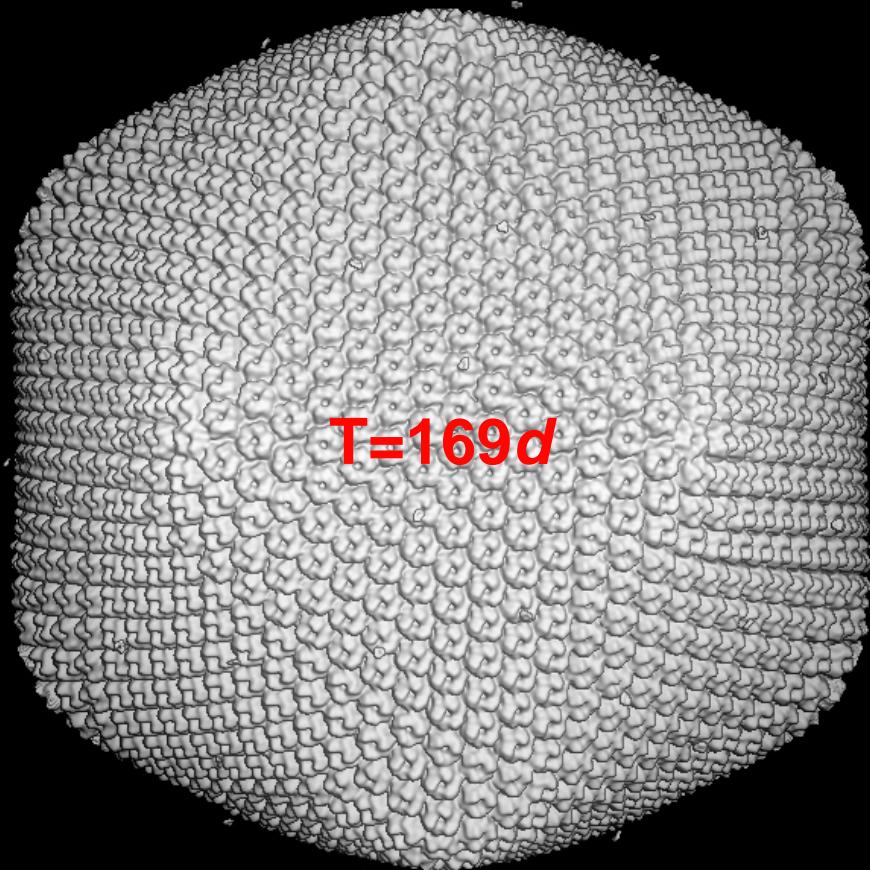


B19

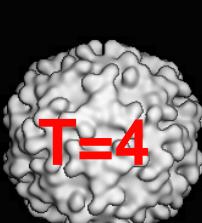
500 Å



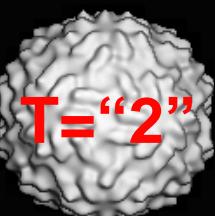
HSV



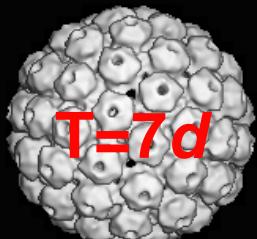
PBCV-1



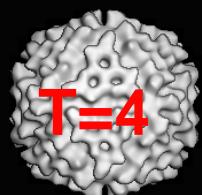
N ω V



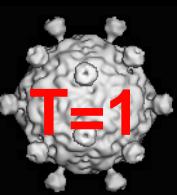
LA-1



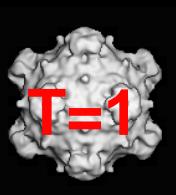
Polyoma



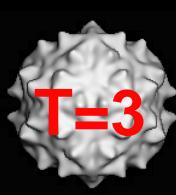
N β V



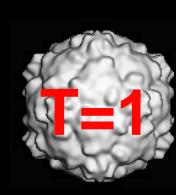
SpV-4



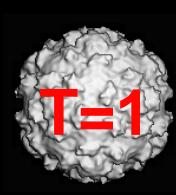
ϕ X174



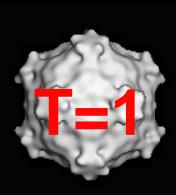
FHV



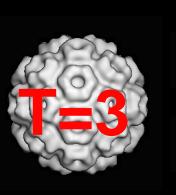
HRV-14



Polio



CPMV



CCMV



B19

500 Å

3D Reconstruction of Icosahedral Particles

Triangulation Number

Key Concept:

T symmetry is **NOT** incorporated into or enforced by the 3D reconstruction algorithms

Hence, T symmetry emerges as a result of a properly performed 3D reconstruction analysis

3D Reconstruction of Icosahedral Particles

Triangulation Number

Key Concept:

T symmetry is **NOT** incorporated into or enforced by the 3D reconstruction algorithms

In other words: What you determine is the structure of one asymmetric unit of the object

3D Reconstruction of Icosahedral Particles

Two Basic Assumptions:

- Specimen consists of stable particles with 'identical' structures (else averaging is invalid)
- Programs test for and assume presence of icosahedral (532) symmetry

3D Reconstruction of Icosahedral Particles

Outline

- Background

- References; examples; etc.

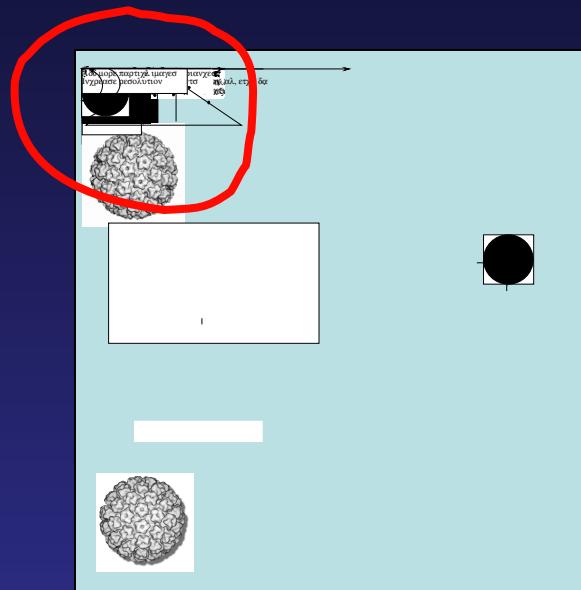
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- “Typical” procedure (flow chart)

- Digitization and boxing
 - Image preprocessing / CTF estimation
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 - 3D reconstruction with CTF corrections
 - Validation (resolution assessment)

- Current and future strategies



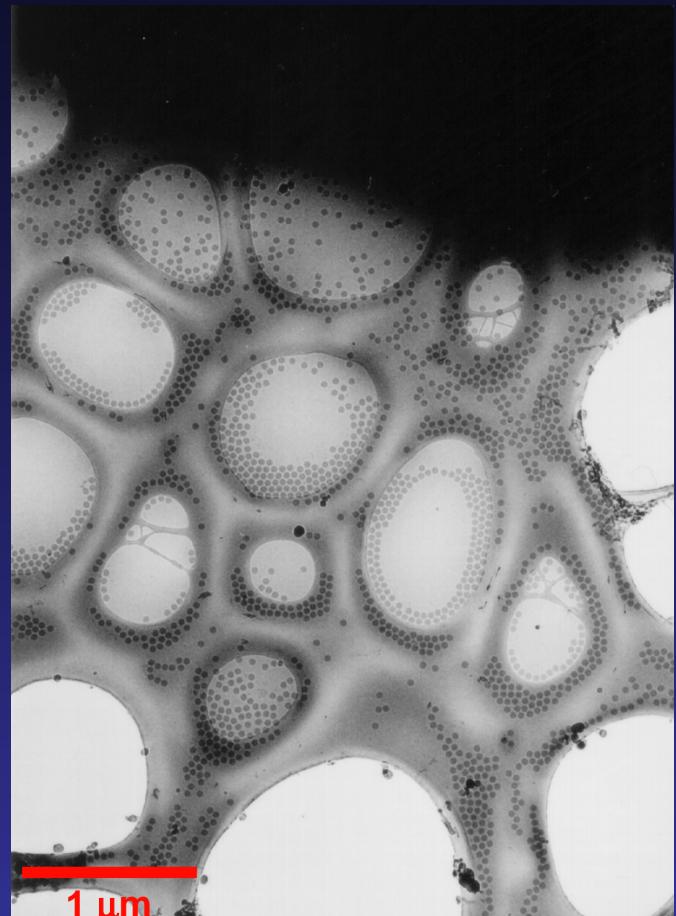
3D Reconstruction of Icosahedral Particles

Protocol

Electron Cryo-Microscopy

Sample : ~2-3 μl at 1-5 mg/ml

Specimen support: holey carbon film (1-2 μm)



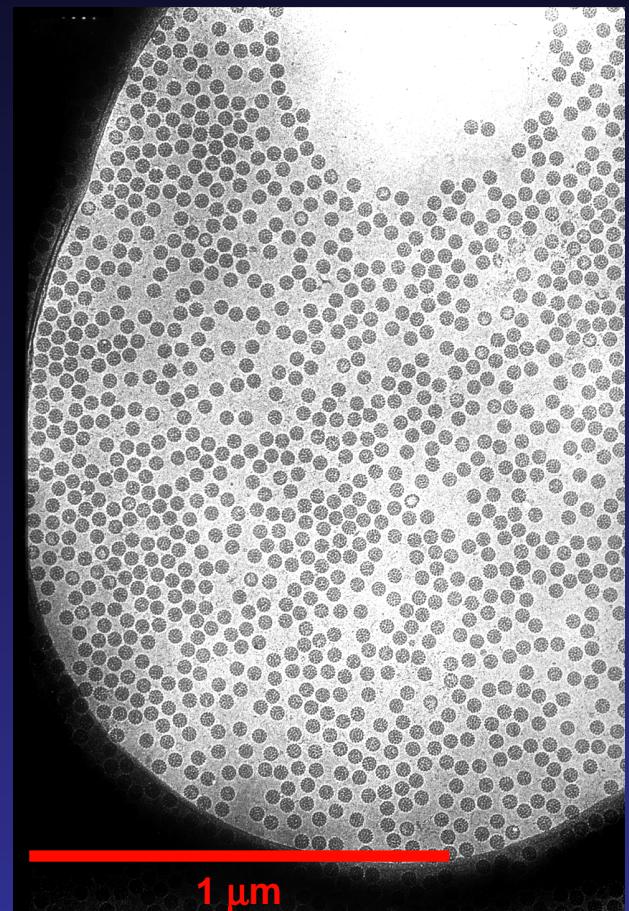
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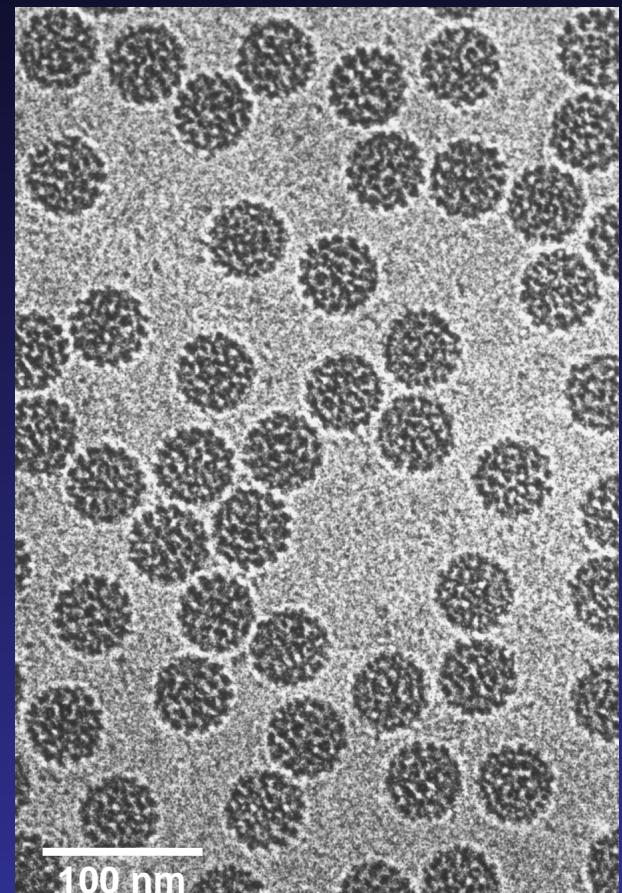
3D Reconstruction of Icosahedral Particles

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3D Reconstruction of Icosahedral Particles

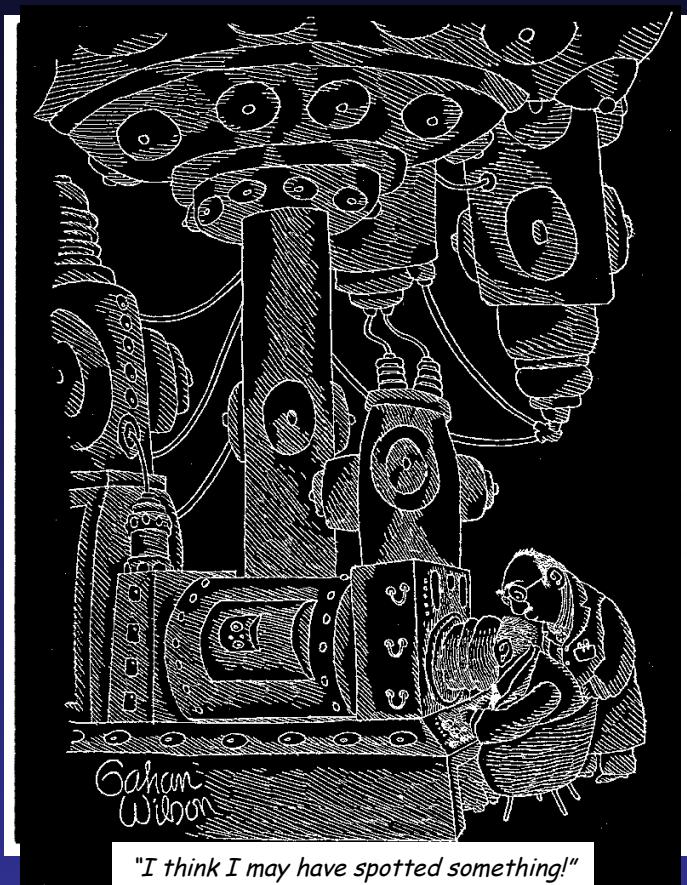
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Electron Cryo-Microscopy

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Specimen support: holey carbon film (1-2 μ m)

Microscope: 200-300 keV with FEG



3D Reconstruction of Icosahedral Particles

Protocol

Electron Cryo-Microscopy

Sample : ~2-3 μ l at 1-5 mg/ml

Specimen support: holey carbon film (1-2 μ m)

Microscope: 200-300 keV with FEG

Defocus range: 1-3 μ m underfocus

Dose: 10-20 e $^-$ / \AA^2

Film: SO-163 (12 min, full strength)

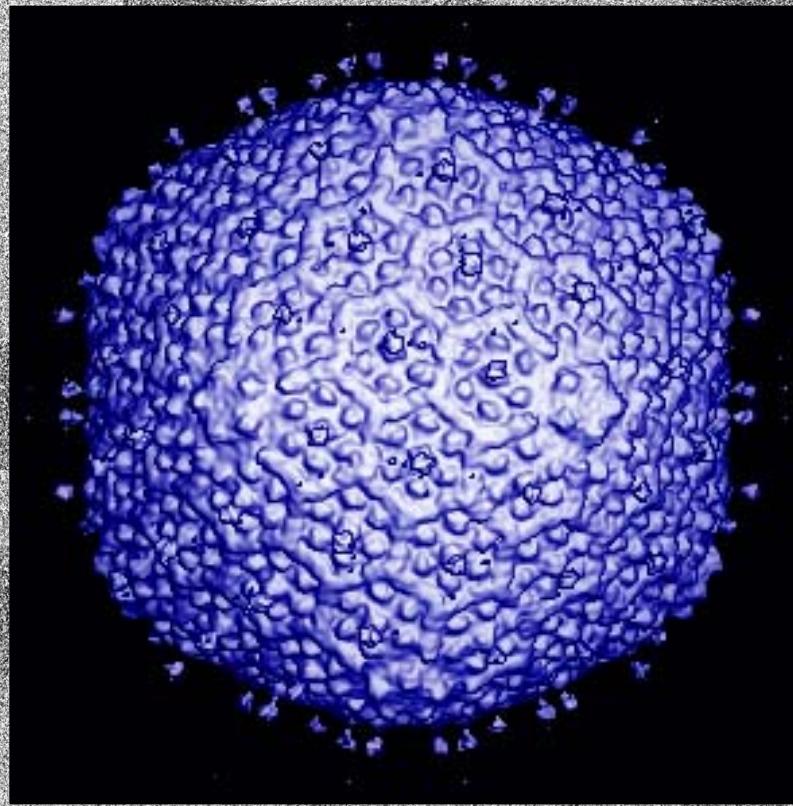
Micrographs: 50-100-->1000s(?)

Particles: 10^3 - 10^4 --> 10^5 ----> 10^6 (?)

Target resolution: 10 - 6 \AA --> 4 \AA (?)



FEI Tecnai F30 Polara



100 nm

3D Reconstruction of Icosahedral Particles

Outline

- Background

- References; examples; etc.

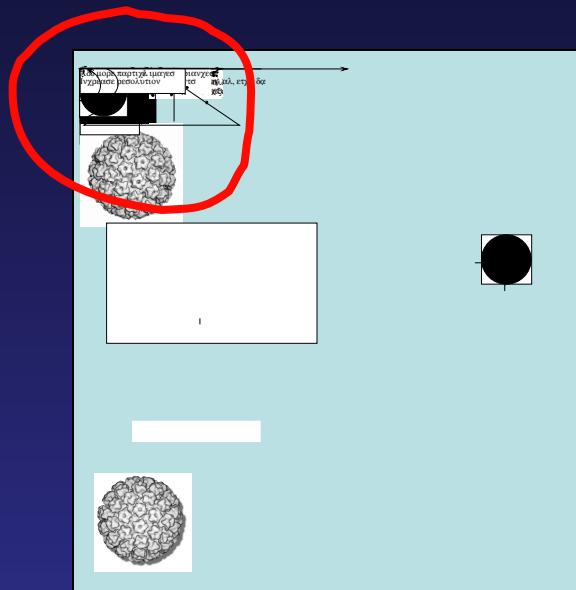
- Symmetry

- Icosahedral (532) point group symmetry
 - Triangulation symmetry

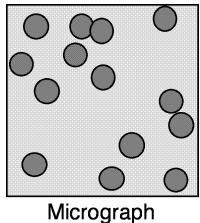
- “Typical” procedure (flow chart)

- Digitization and boxing
 - Image preprocessing / CTF estimation
 - Initial particle orientation/origin search
 - Orientation/origin refinement
 - 3D reconstruction with CTF corrections
 - Validation (resolution assessment)

- Current and future strategies



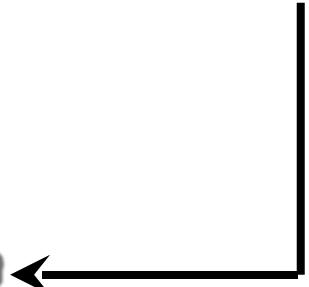
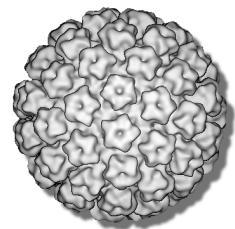
Icosahedral Particle Image Reconstruction Scheme



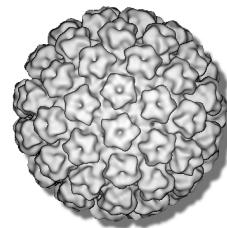
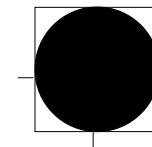
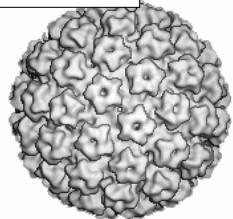
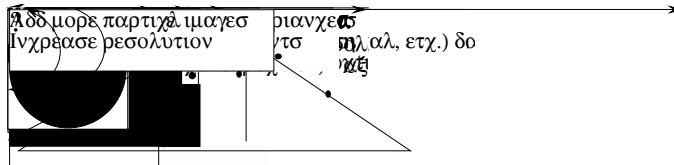
Micrograph



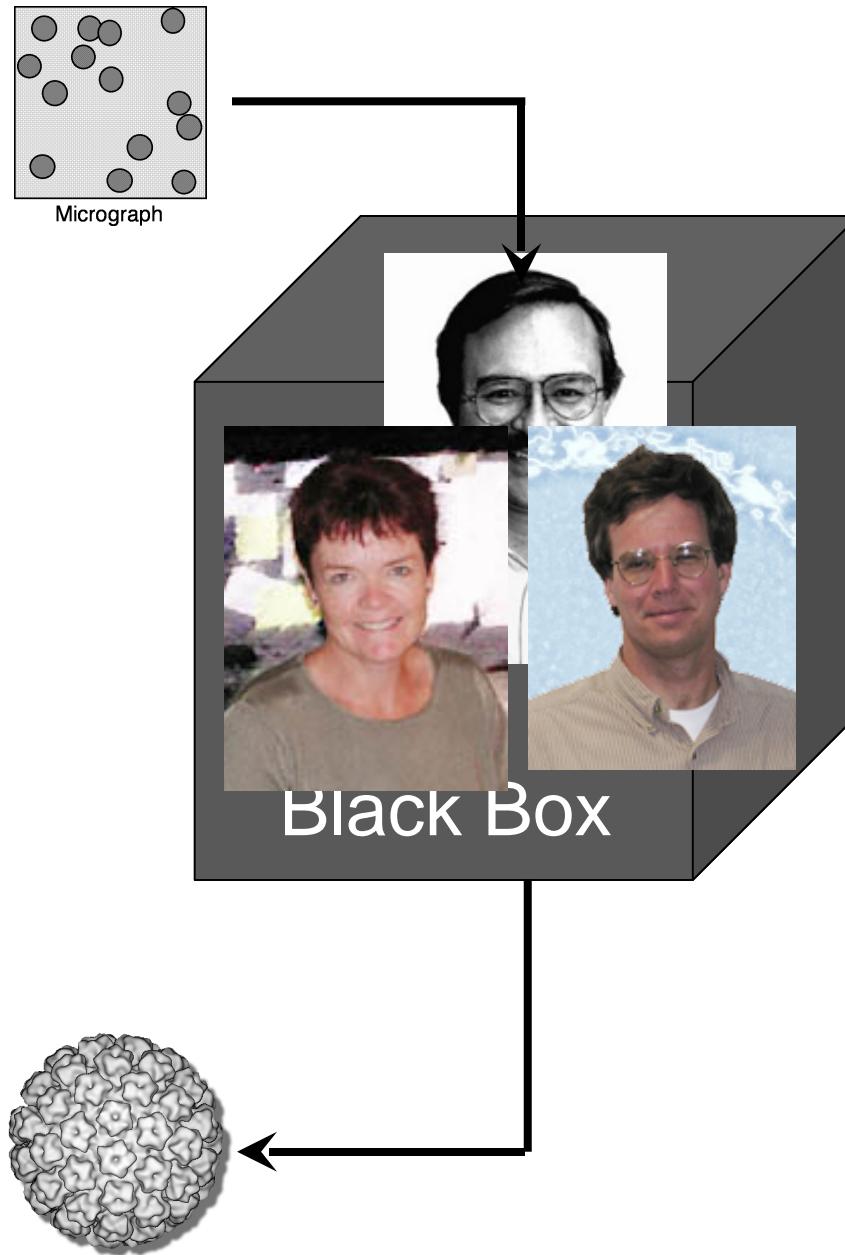
?



Icosahedral Particle Image Reconstruction Scheme

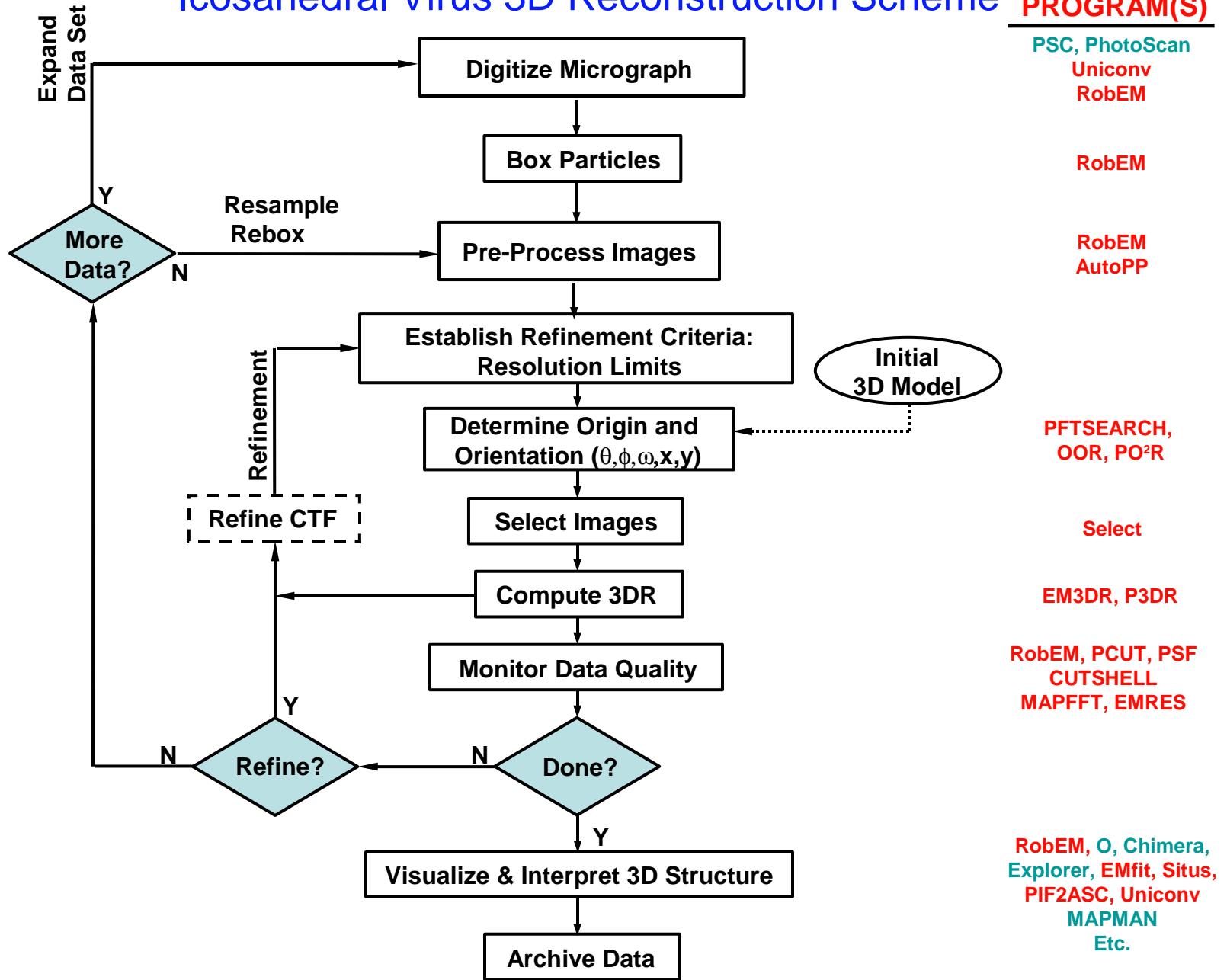


Icosahedral Particle Image Reconstruction Scheme

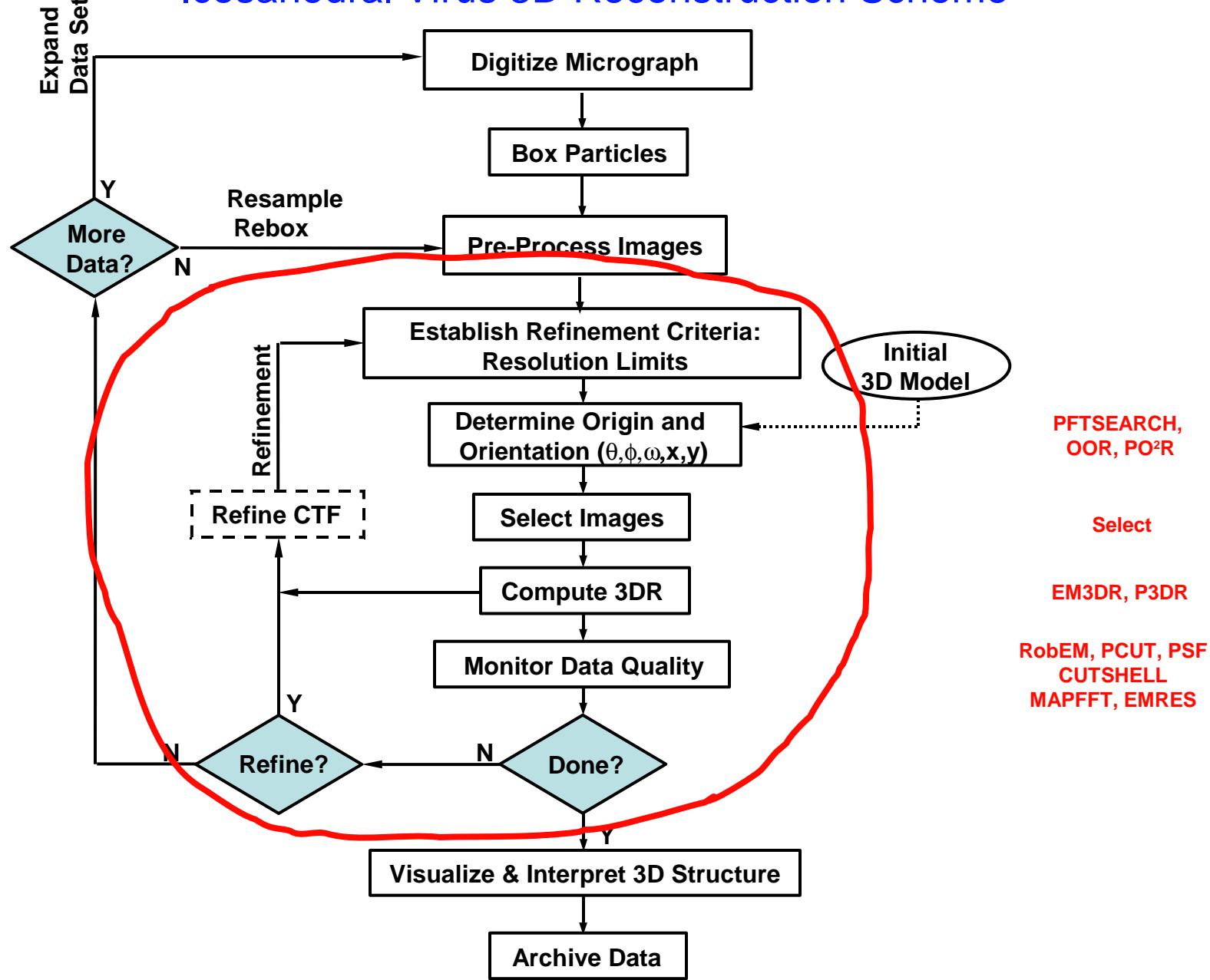


Icosahedral Virus 3D Reconstruction Scheme

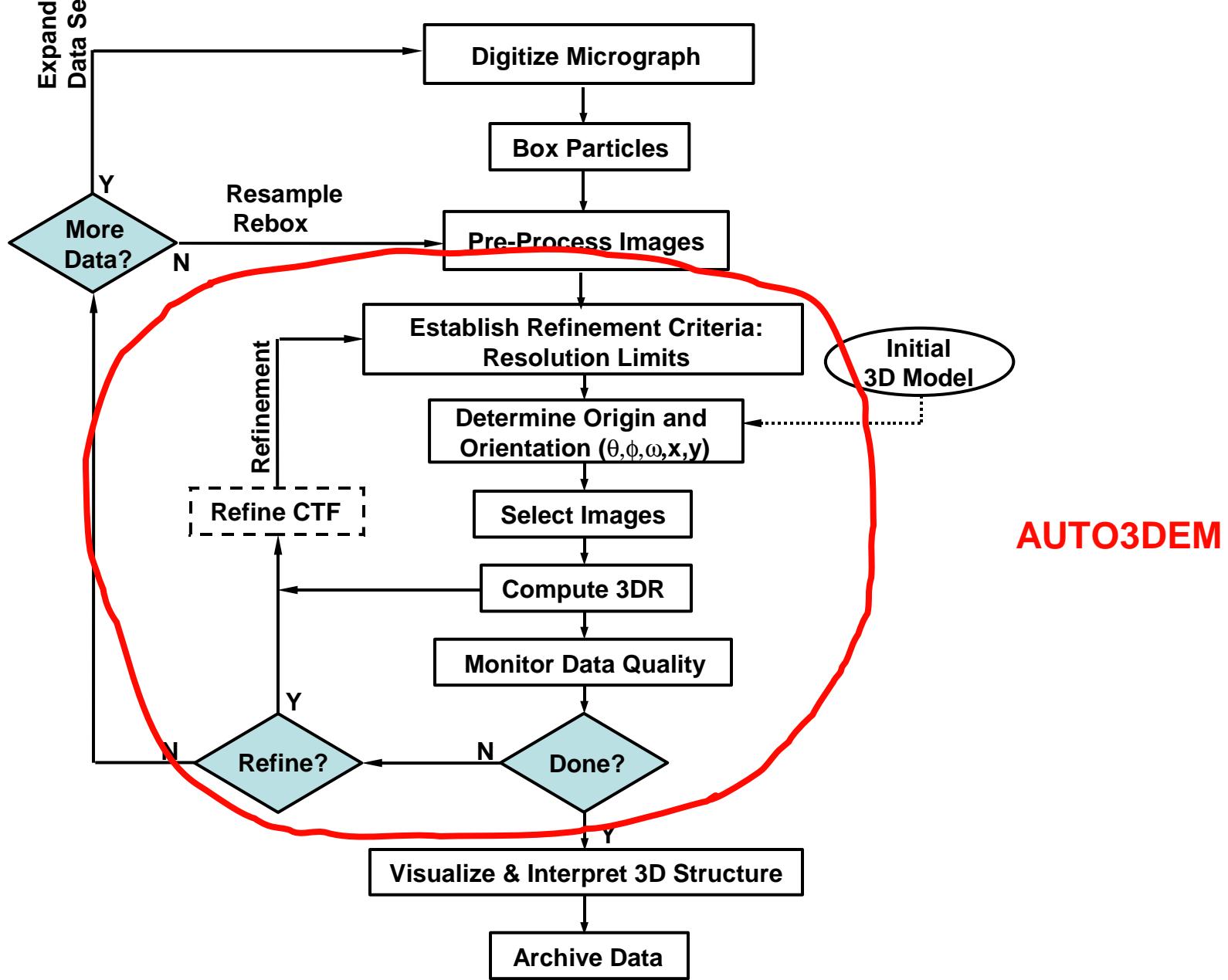
PROGRAM(S)



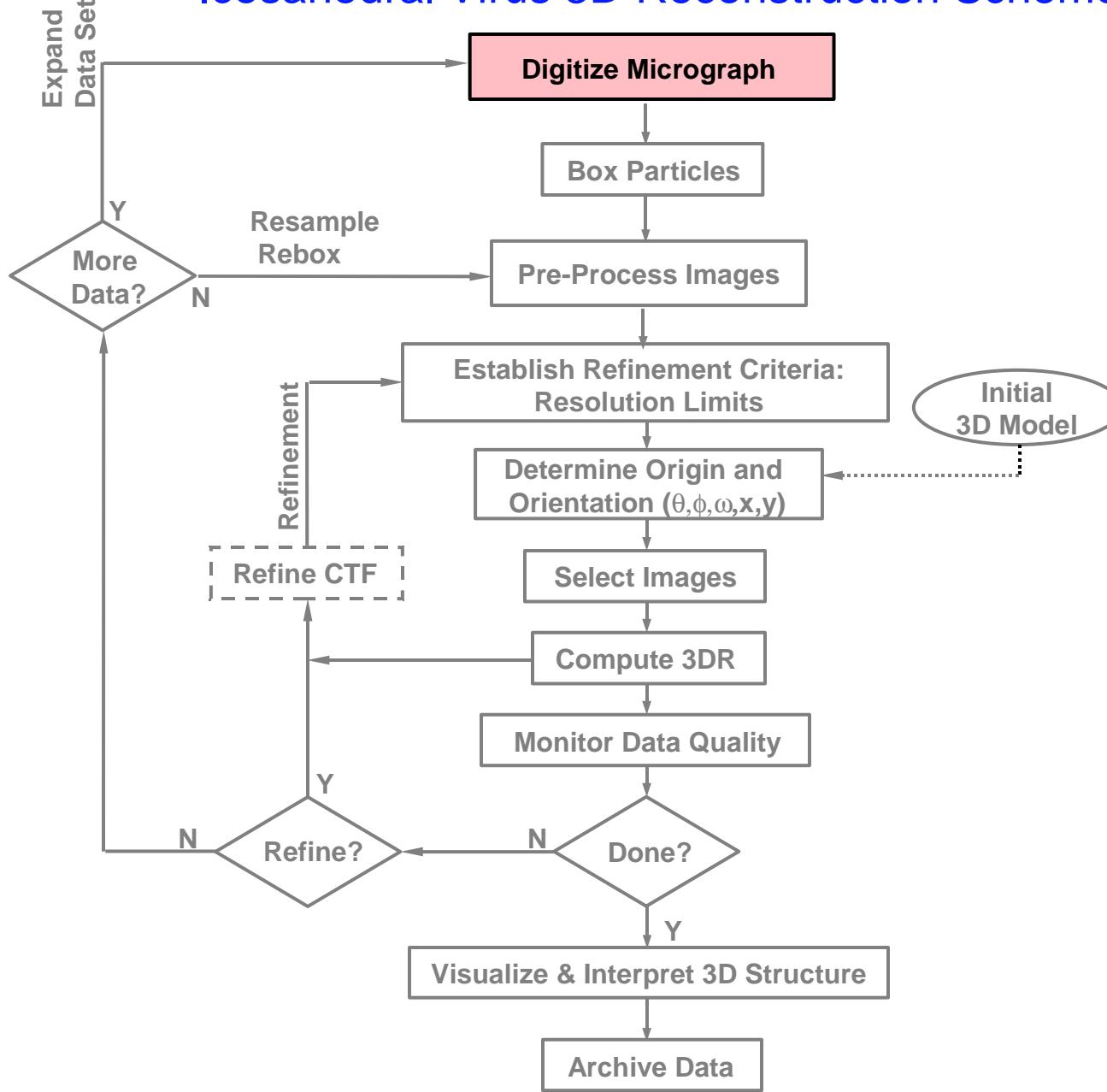
Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme



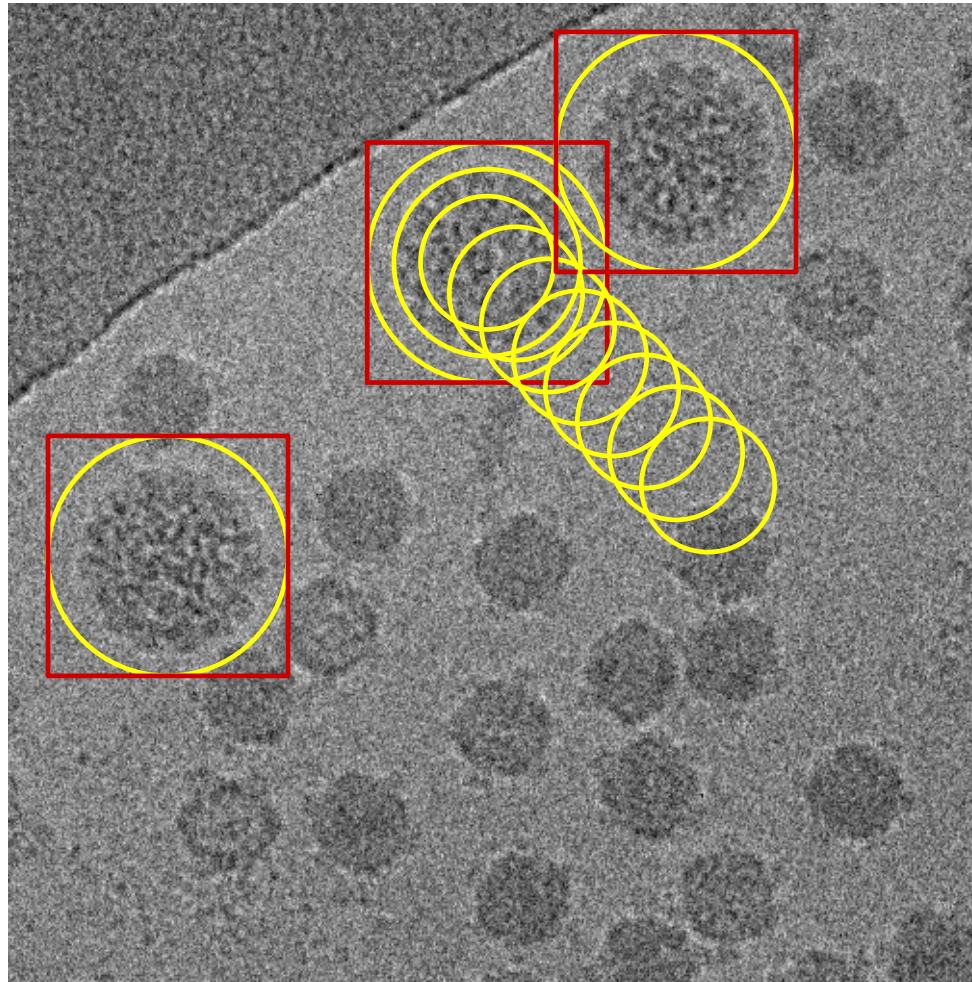
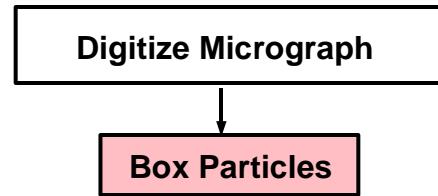
Icosahedral Virus 3D Reconstruction Scheme



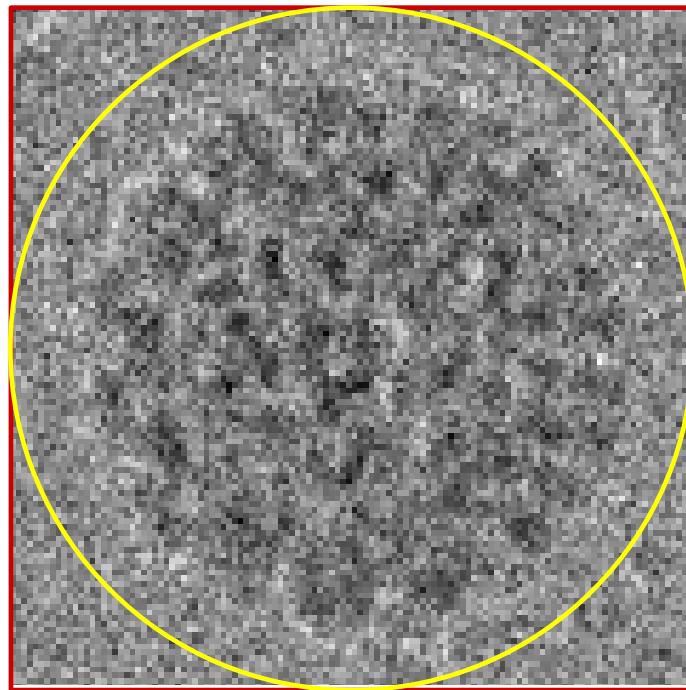
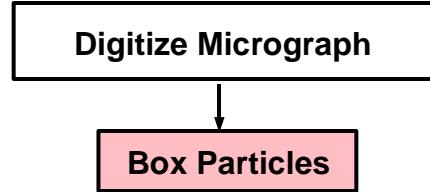
Icosahedral Virus 3D Reconstruction Scheme

Digitize Micrograph

Icosahedral Virus 3D Reconstruction Scheme

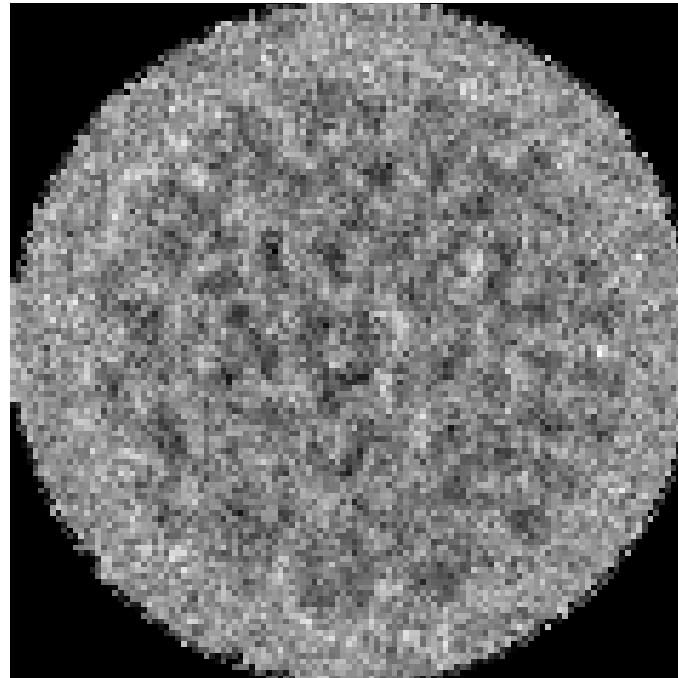
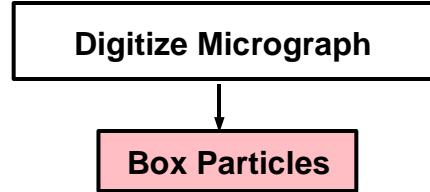


Icosahedral Virus 3D Reconstruction Scheme



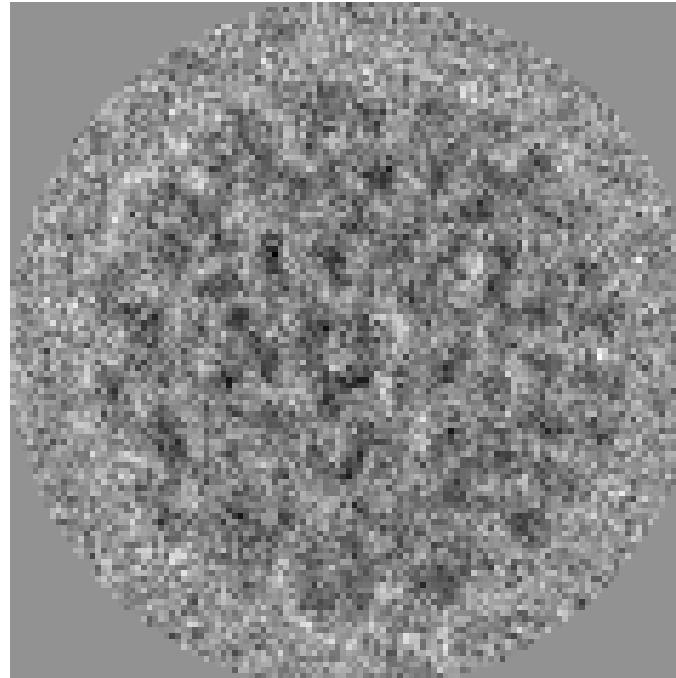
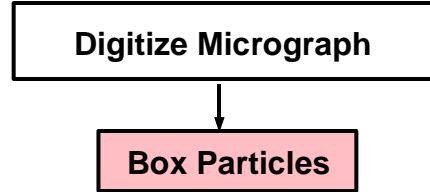
Extracted

Icosahedral Virus 3D Reconstruction Scheme



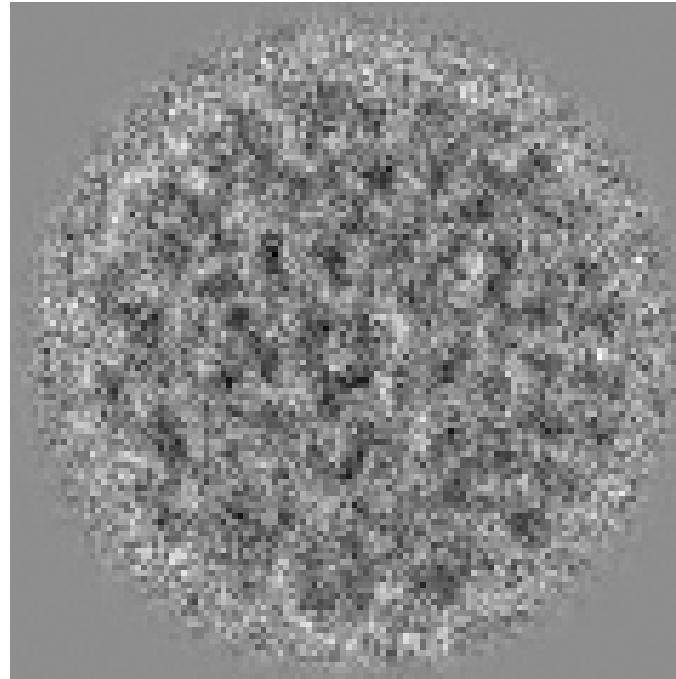
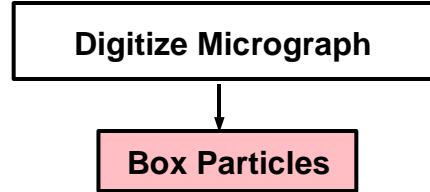
Masked

Icosahedral Virus 3D Reconstruction Scheme



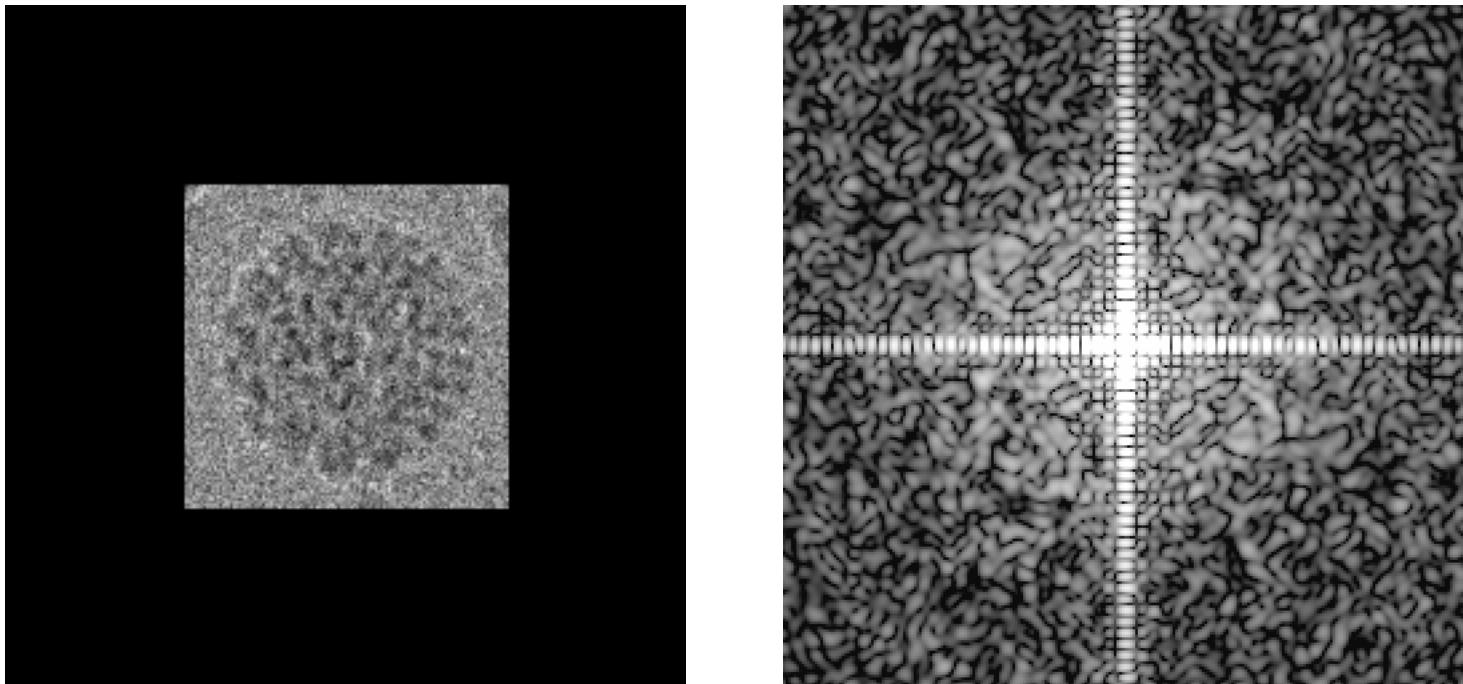
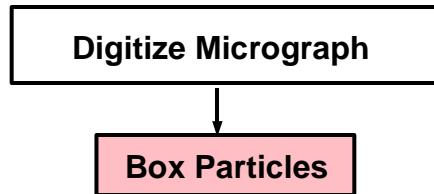
Floated

Icosahedral Virus 3D Reconstruction Scheme



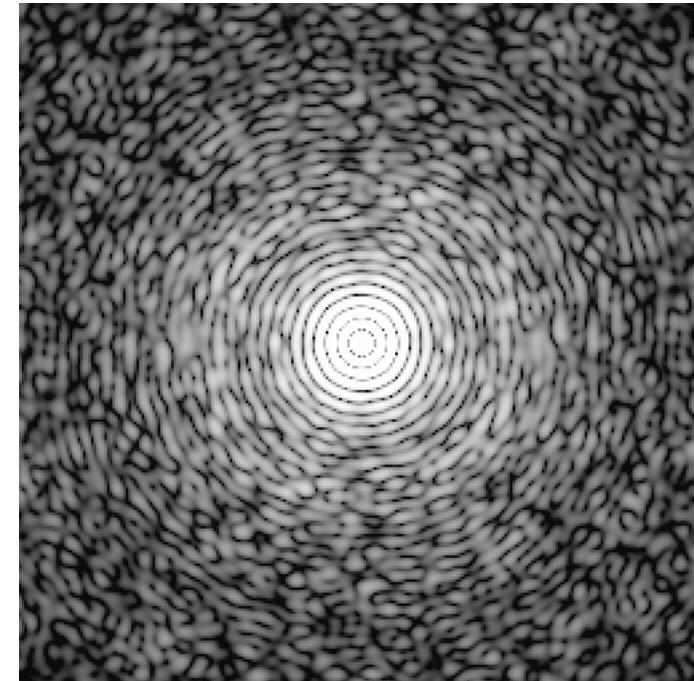
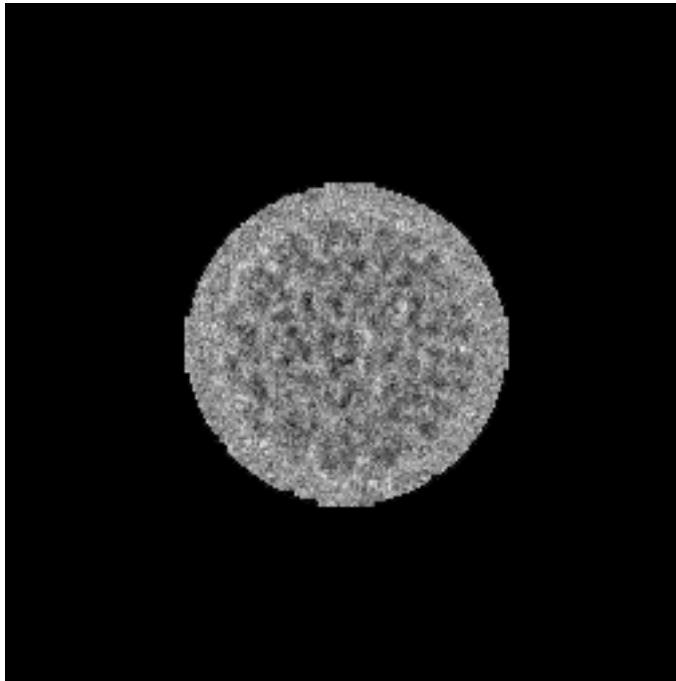
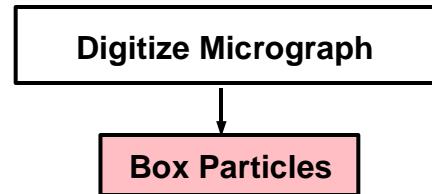
Apodized

Icosahedral Virus 3D Reconstruction Scheme



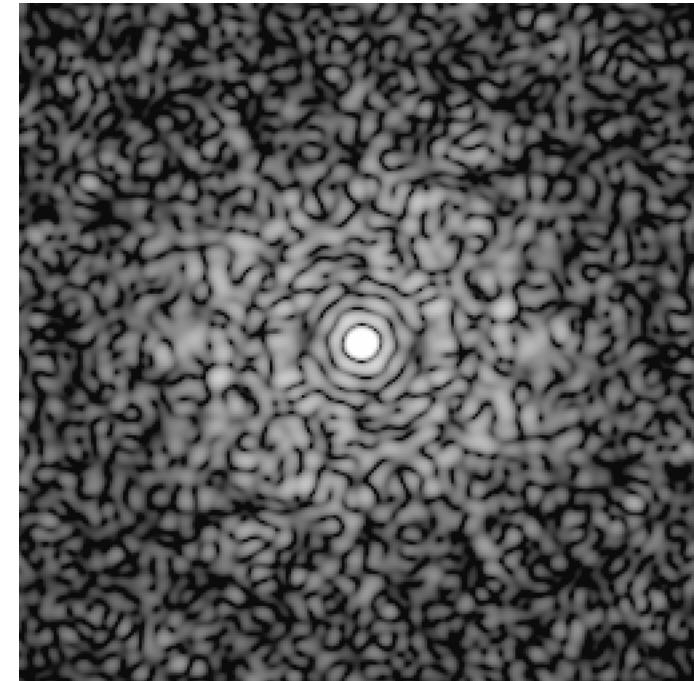
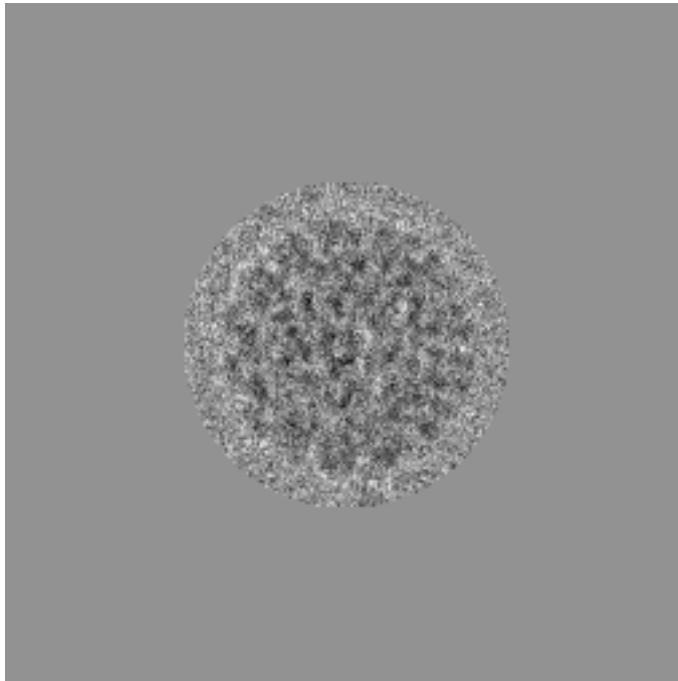
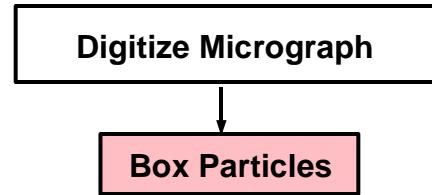
Square mask; unfloated

Icosahedral Virus 3D Reconstruction Scheme



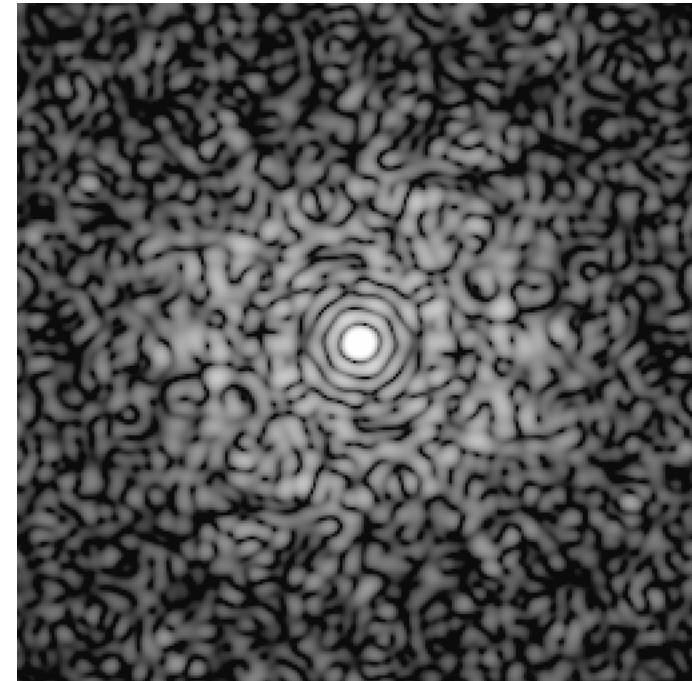
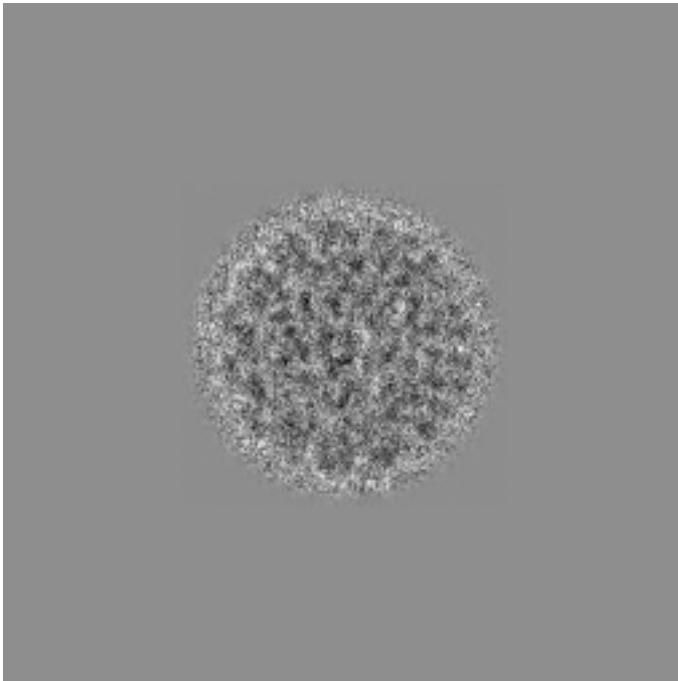
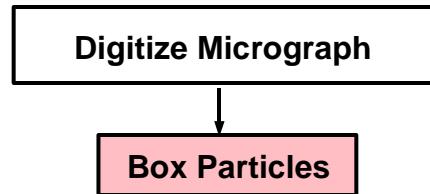
Circular mask; unfloated

Icosahedral Virus 3D Reconstruction Scheme



Circular mask; floated

Icosahedral Virus 3D Reconstruction Scheme

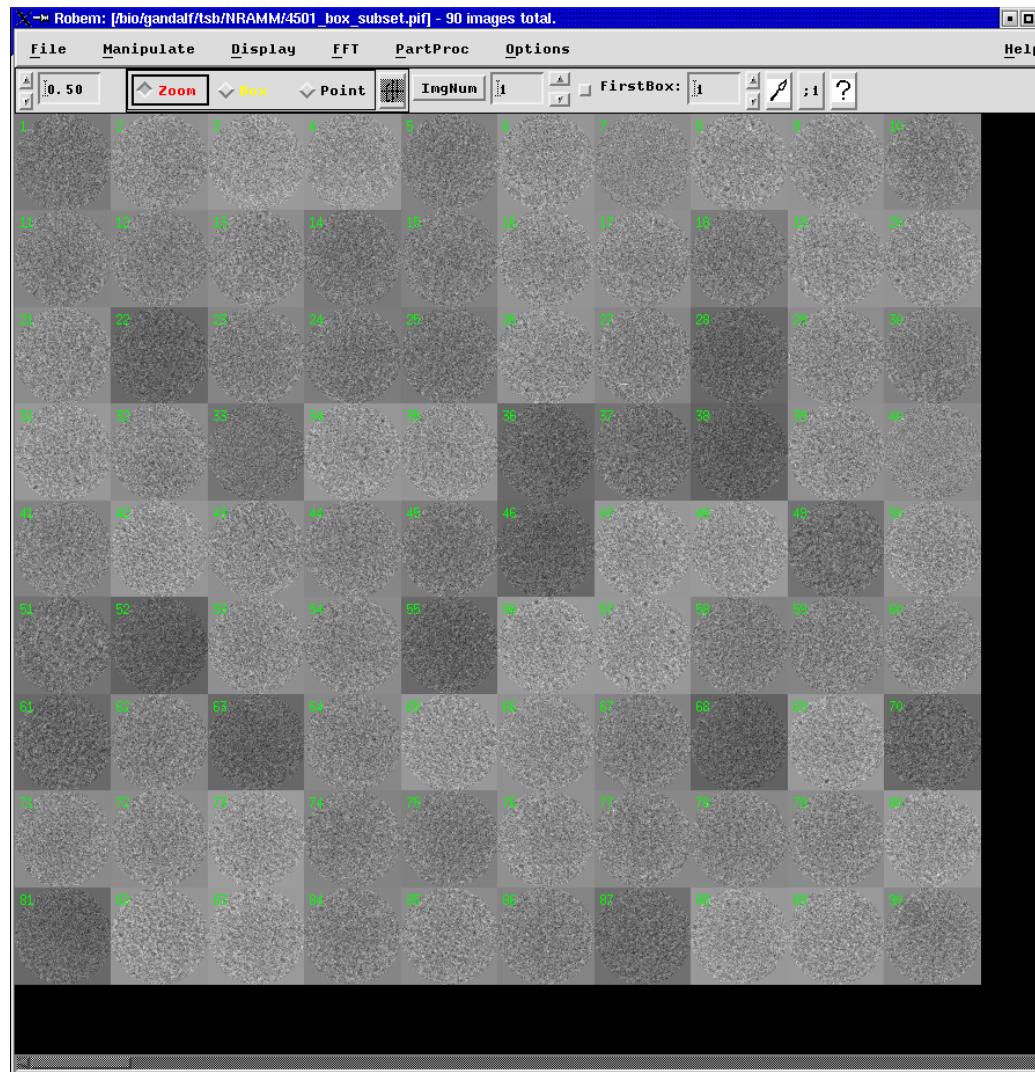


Circular mask; floated & apodized

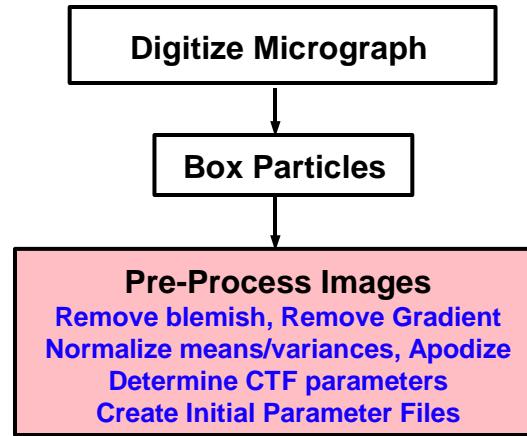
Icosahedral Virus 3D Reconstruction Scheme

Digitize Micrograph

Box Particles

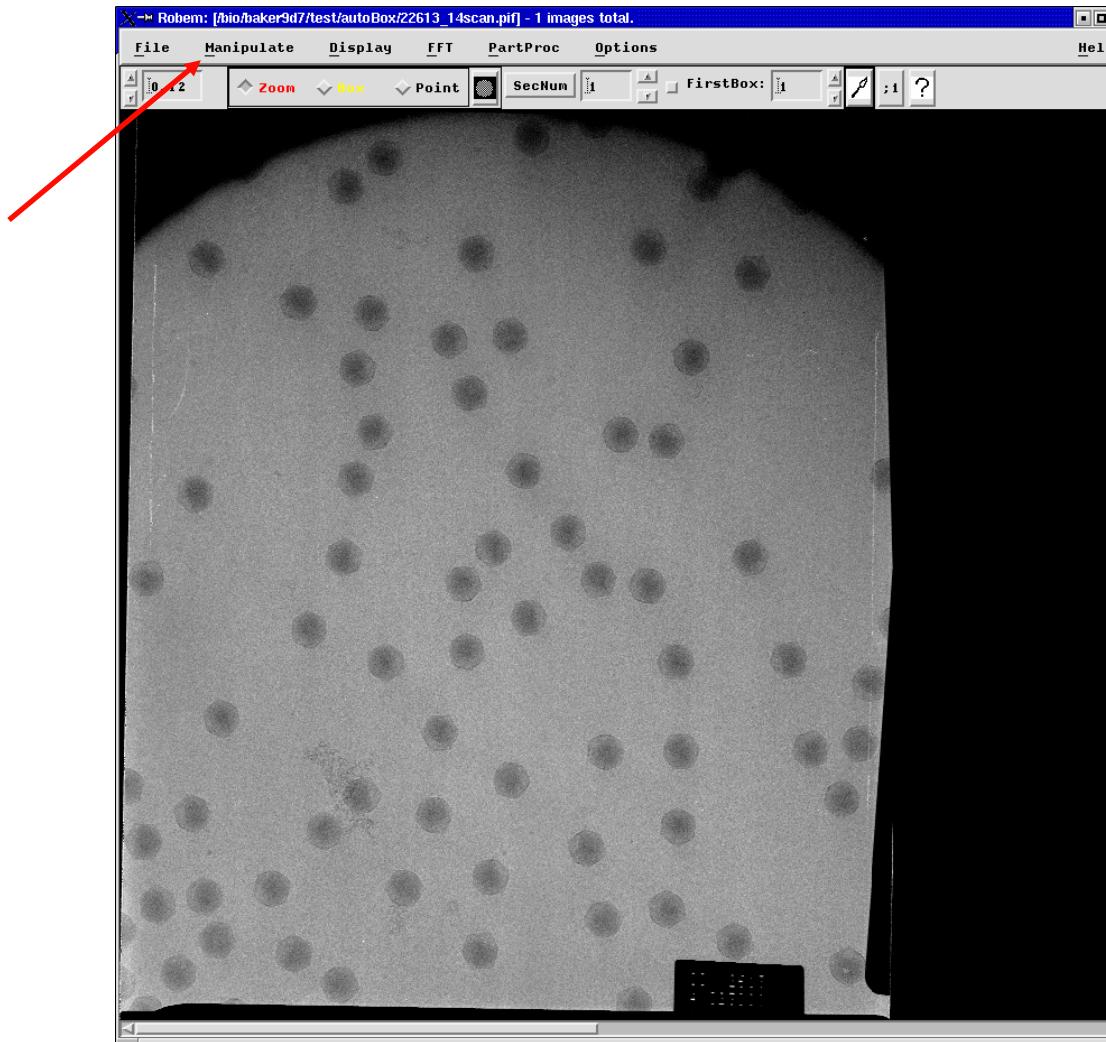


Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme

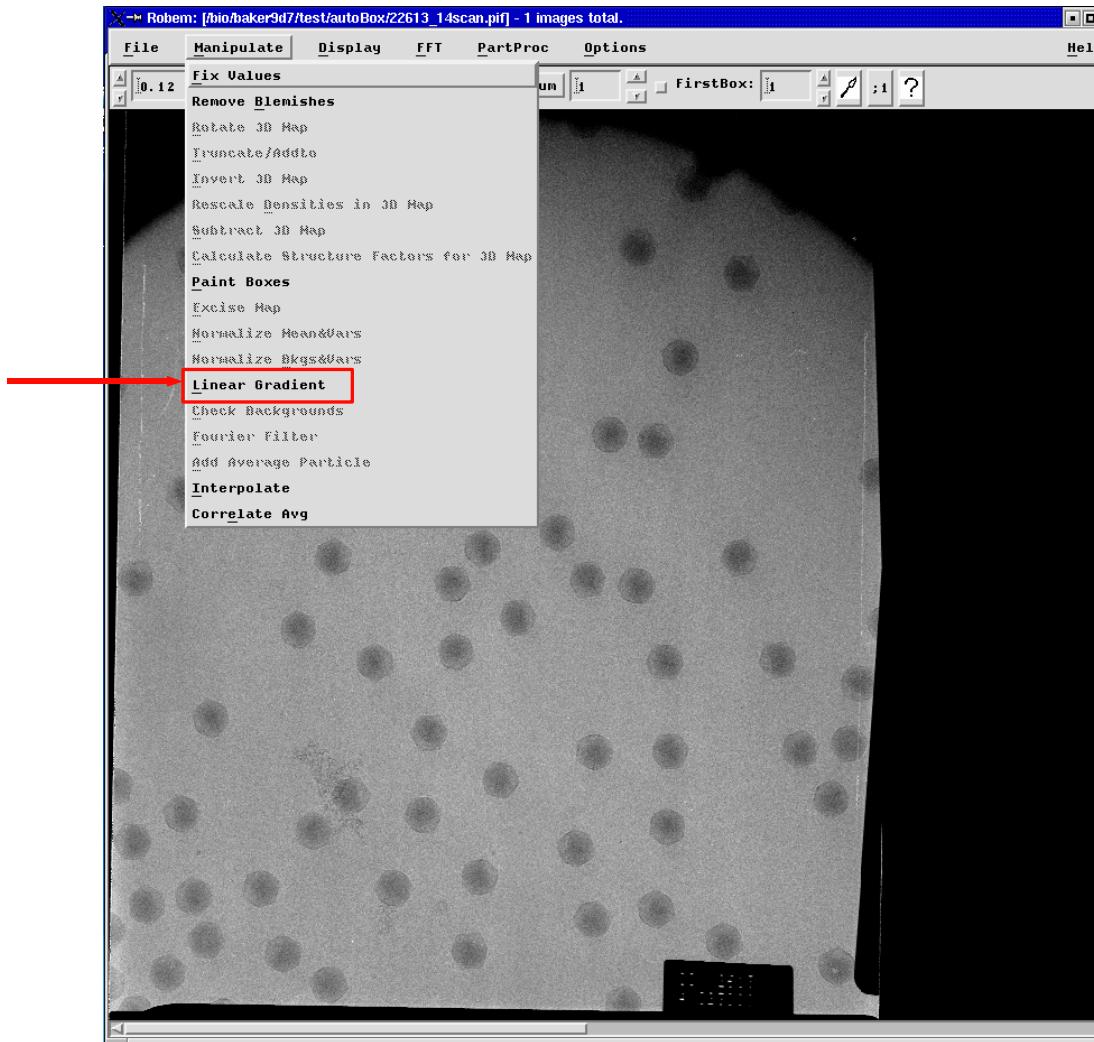
Pre-Process Images
Remove blemish, Remove Gradient
Normalize means/variances, Anodize
Determine CTF parameters
Create Initial Parameter Files



Icosahedral Virus 3D Reconstruction Scheme

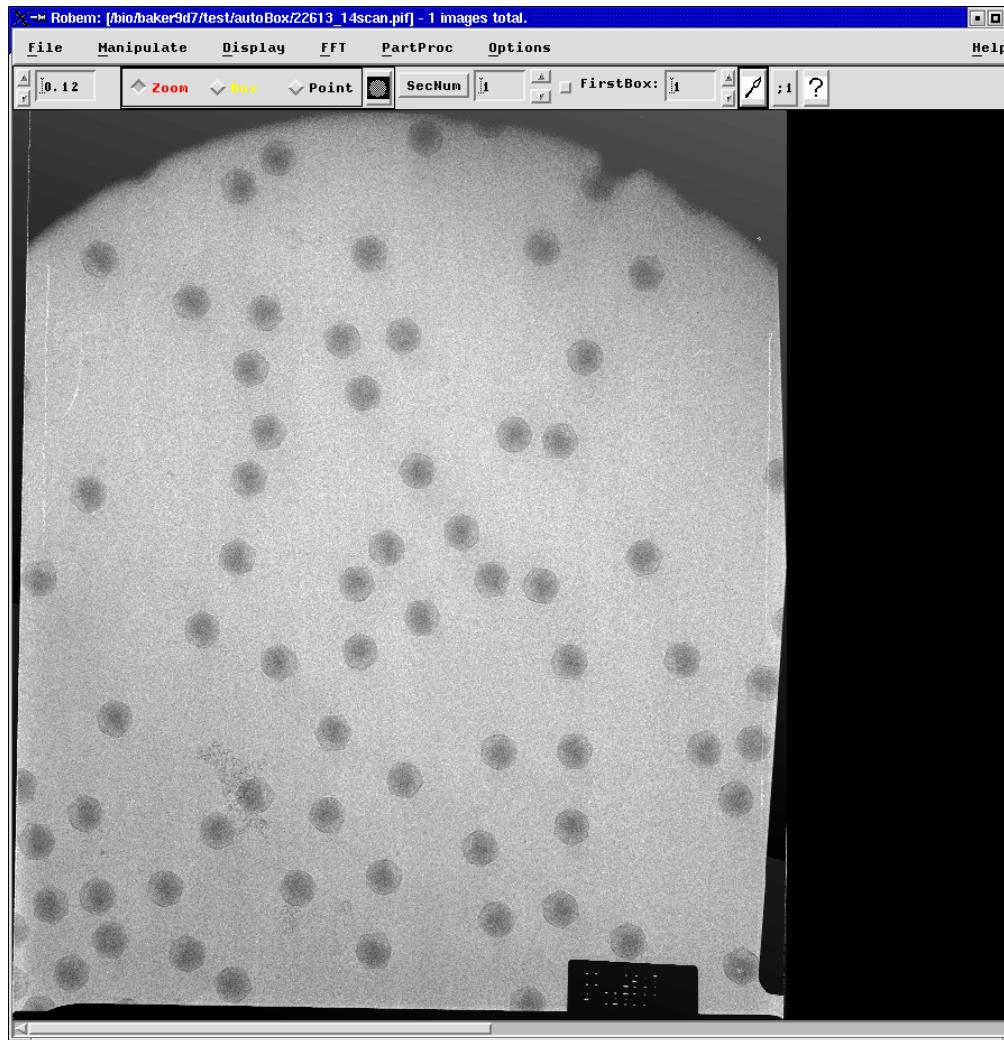
↓

Pre-Process Images
Remove blemish, Remove Gradient
Normalize means/variances, Anodize
Determine CTF parameters
Create Initial Parameter Files



Icosahedral Virus 3D Reconstruction Scheme

Pre-Process Images
Remove blemish, Remove Gradient
Normalize means/variances, Anodize
Determine CTF parameters
Create Initial Parameter Files



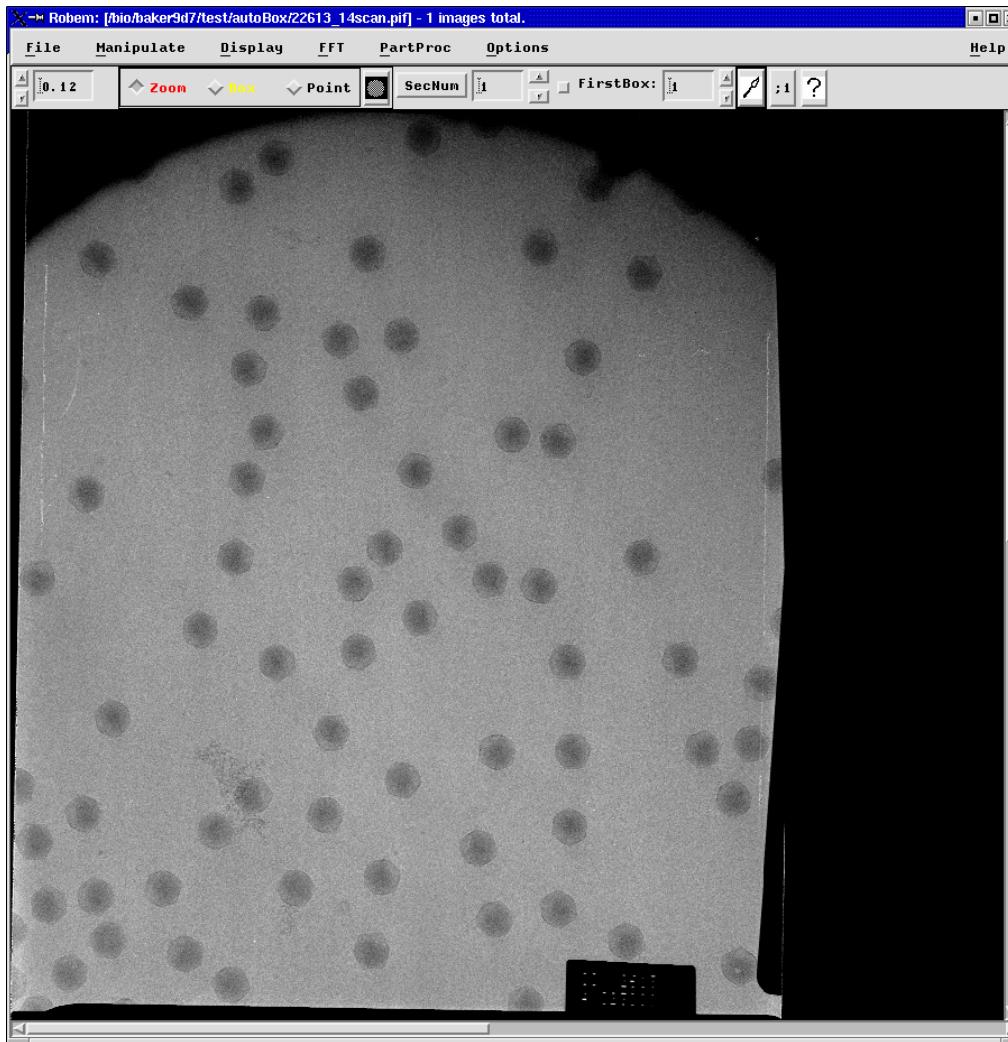
Gradient removed

Icosahedral Virus 3D Reconstruction Scheme



Pre-Process Images

Remove blemish, Remove Gradient
Normalize means/variances, Anodize
Determine CTF parameters
Create Initial Parameter Files



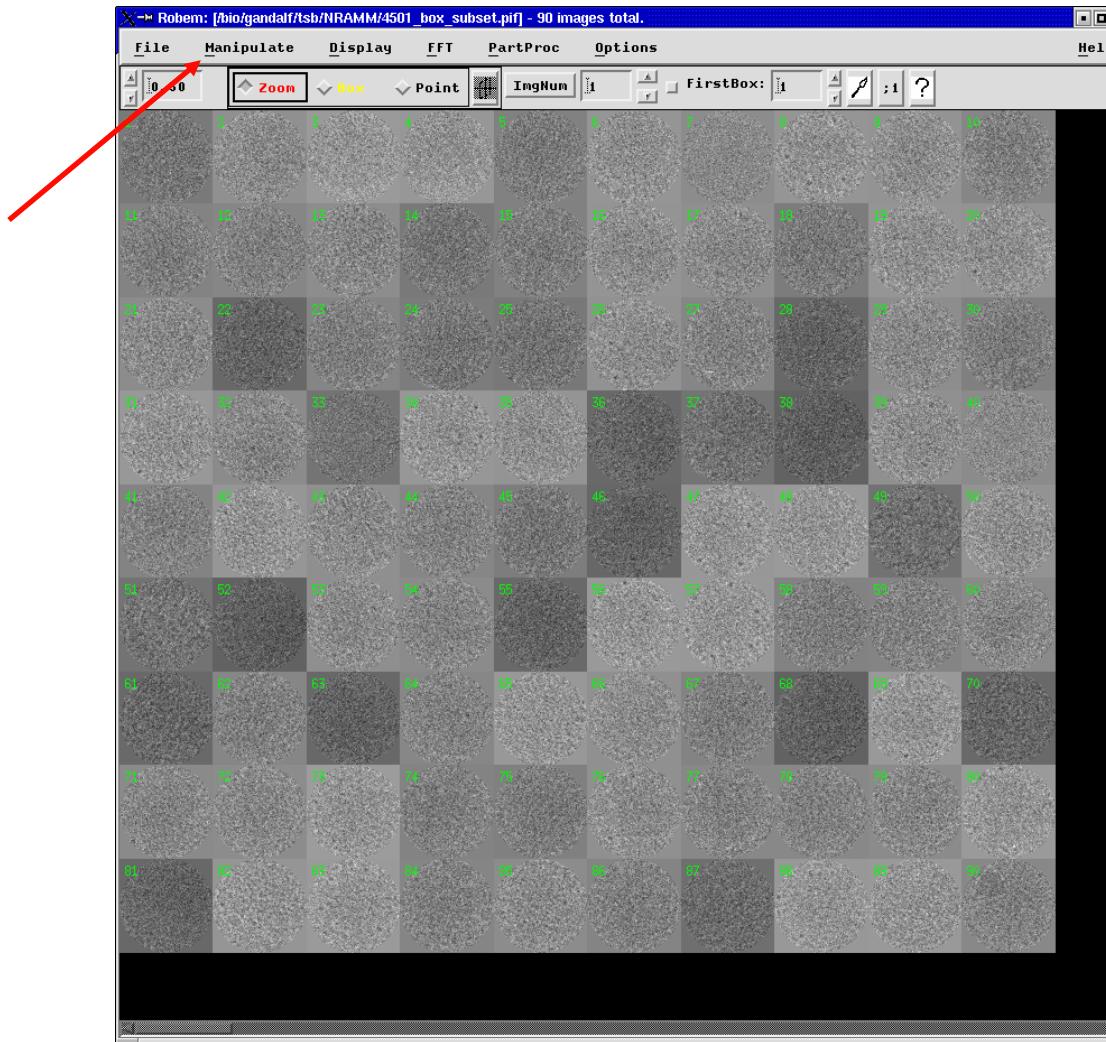
Gradient
not removed

Icosahedral Virus 3D Reconstruction Scheme

↓

Pre-Process Images

Remove blemish, Remove Gradient
Normalize means/variances, Anodize
Determine CTF parameters
Create Initial Parameter Files



Icosahedral Virus 3D Reconstruction Scheme

↓

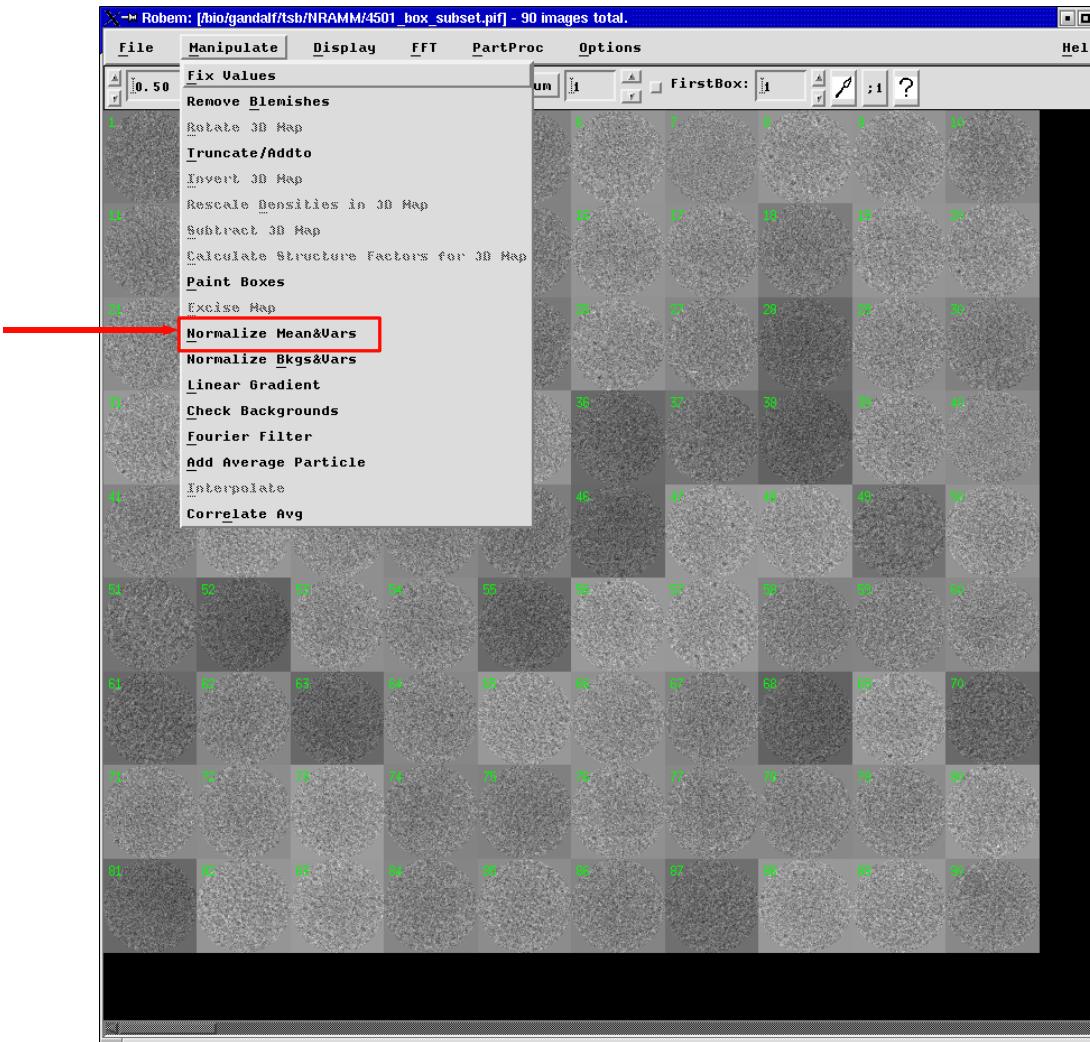
Pre-Process Images

~~Remove blemish, Remove Gradient~~

Normalize means/variances, Apodize

~~Determine CTF parameters~~

Create Initial Parameter Files

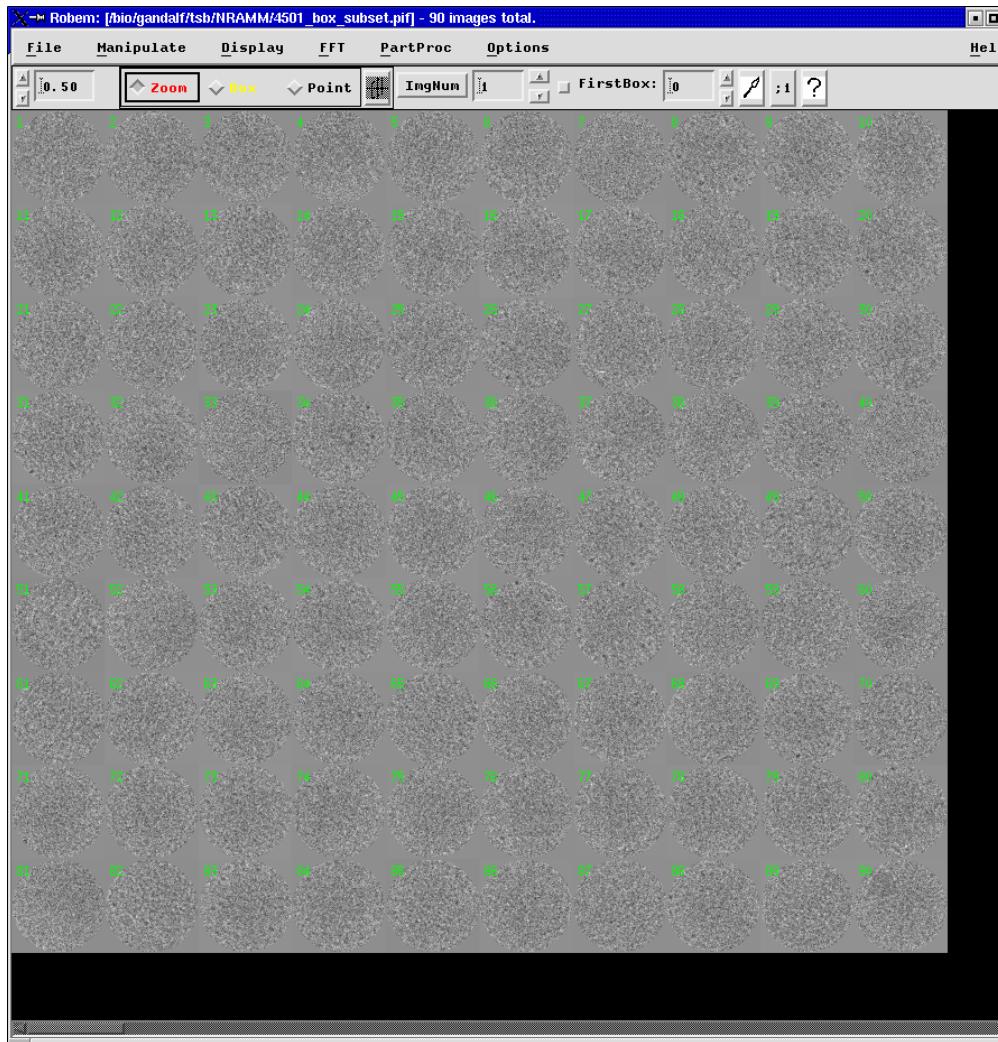


Icosahedral Virus 3D Reconstruction Scheme



Pre-Process Images

- Remove blemish, Remove Gradient
- Normalize means/variances, Apodize
- Determine CTF parameters
- Create Initial Parameter Files

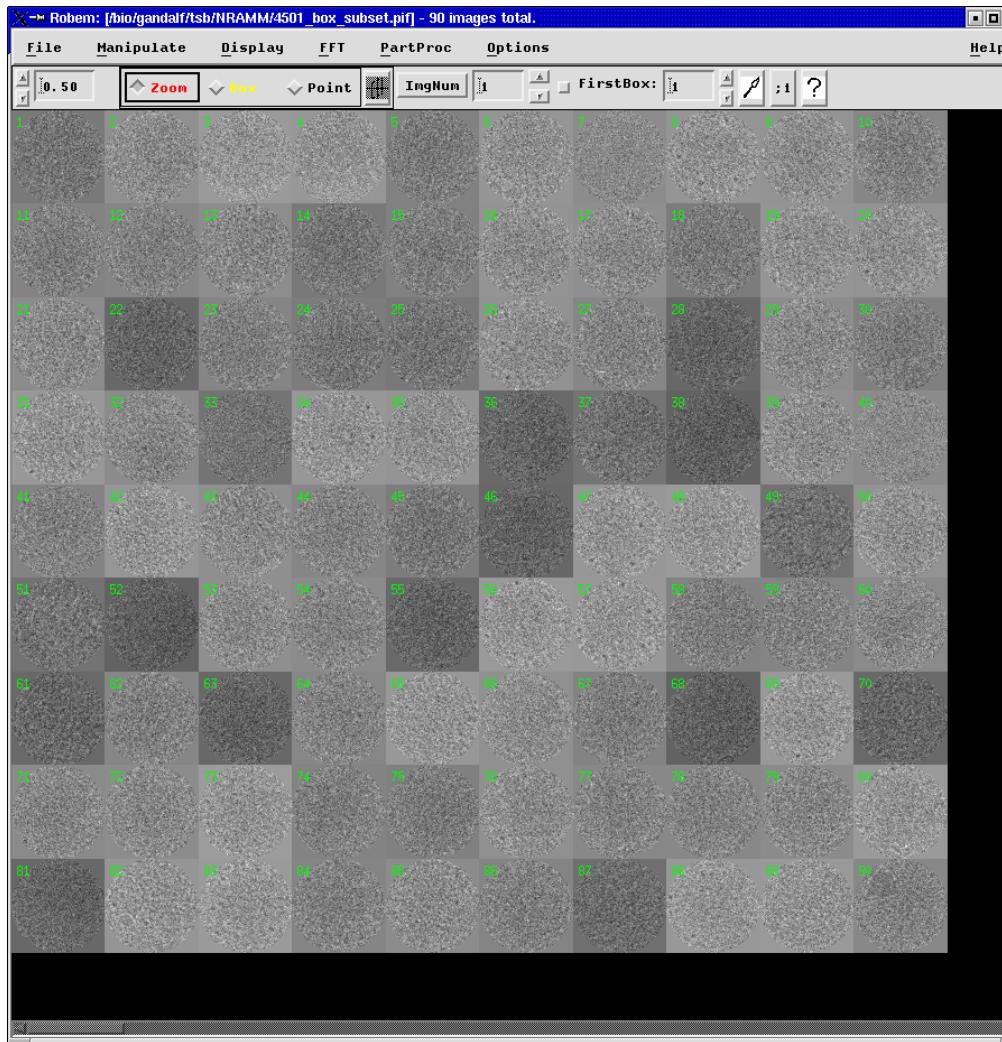


Icosahedral Virus 3D Reconstruction Scheme

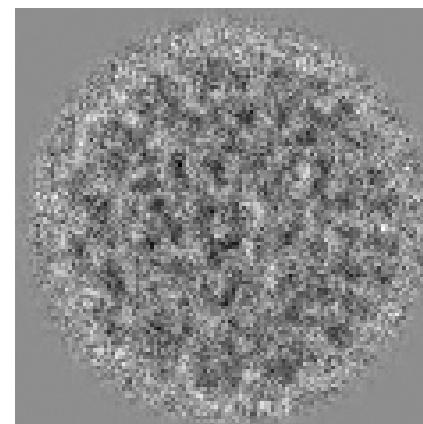
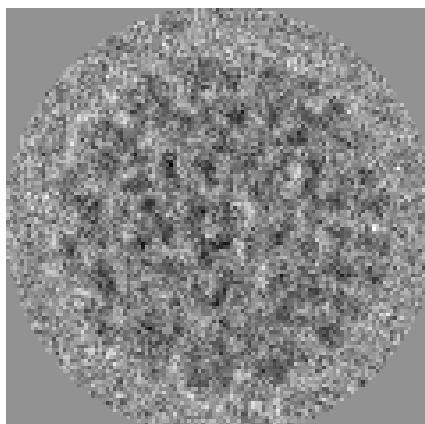
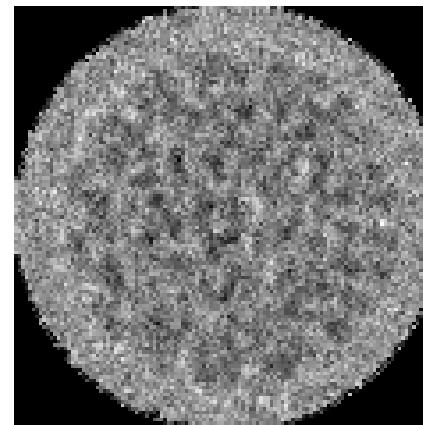
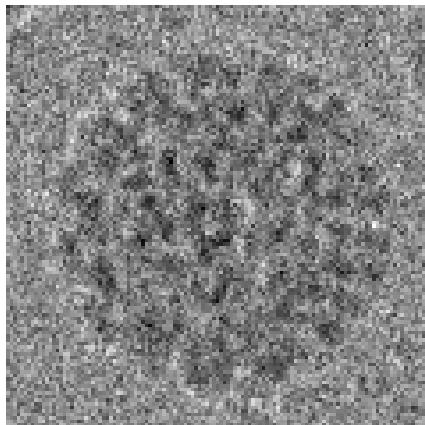
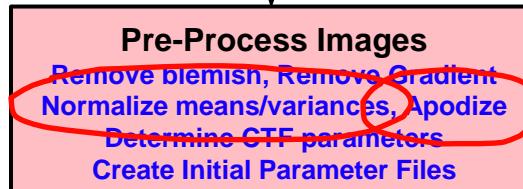


Pre-Process Images

- Remove blemish, Remove Gradient
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- Create Initial Parameter Files



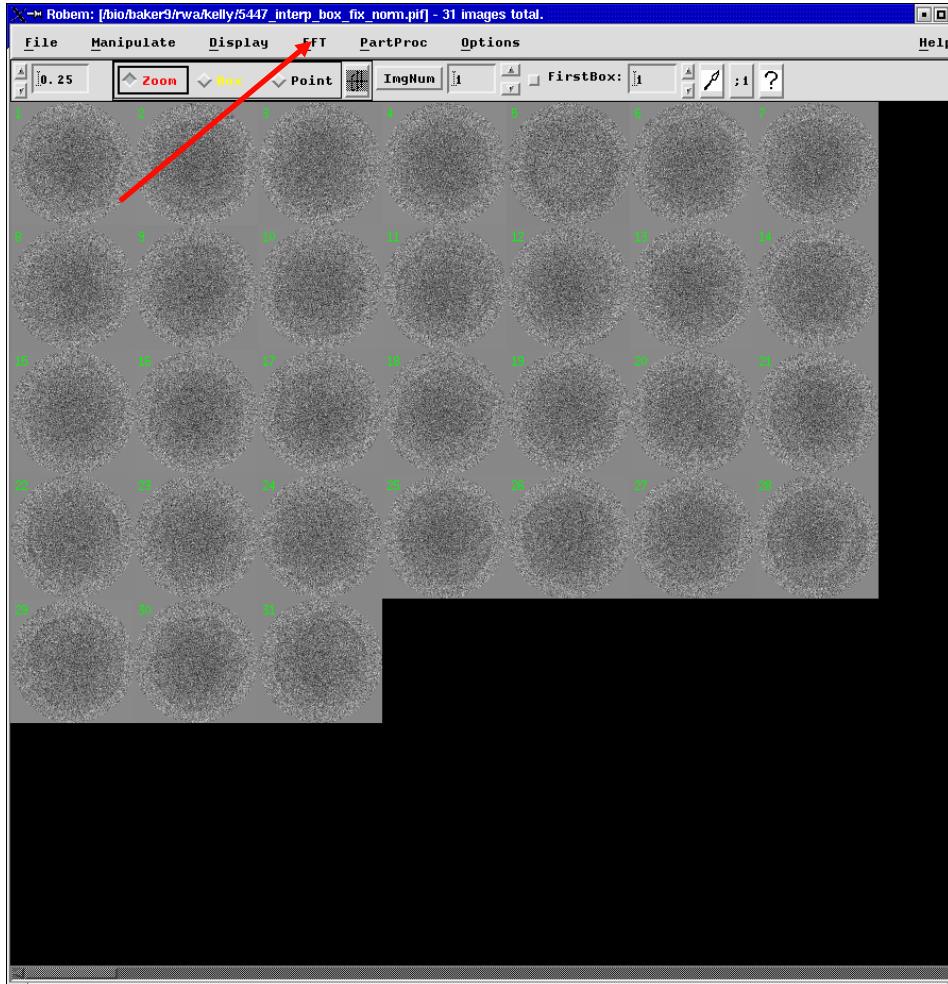
Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme



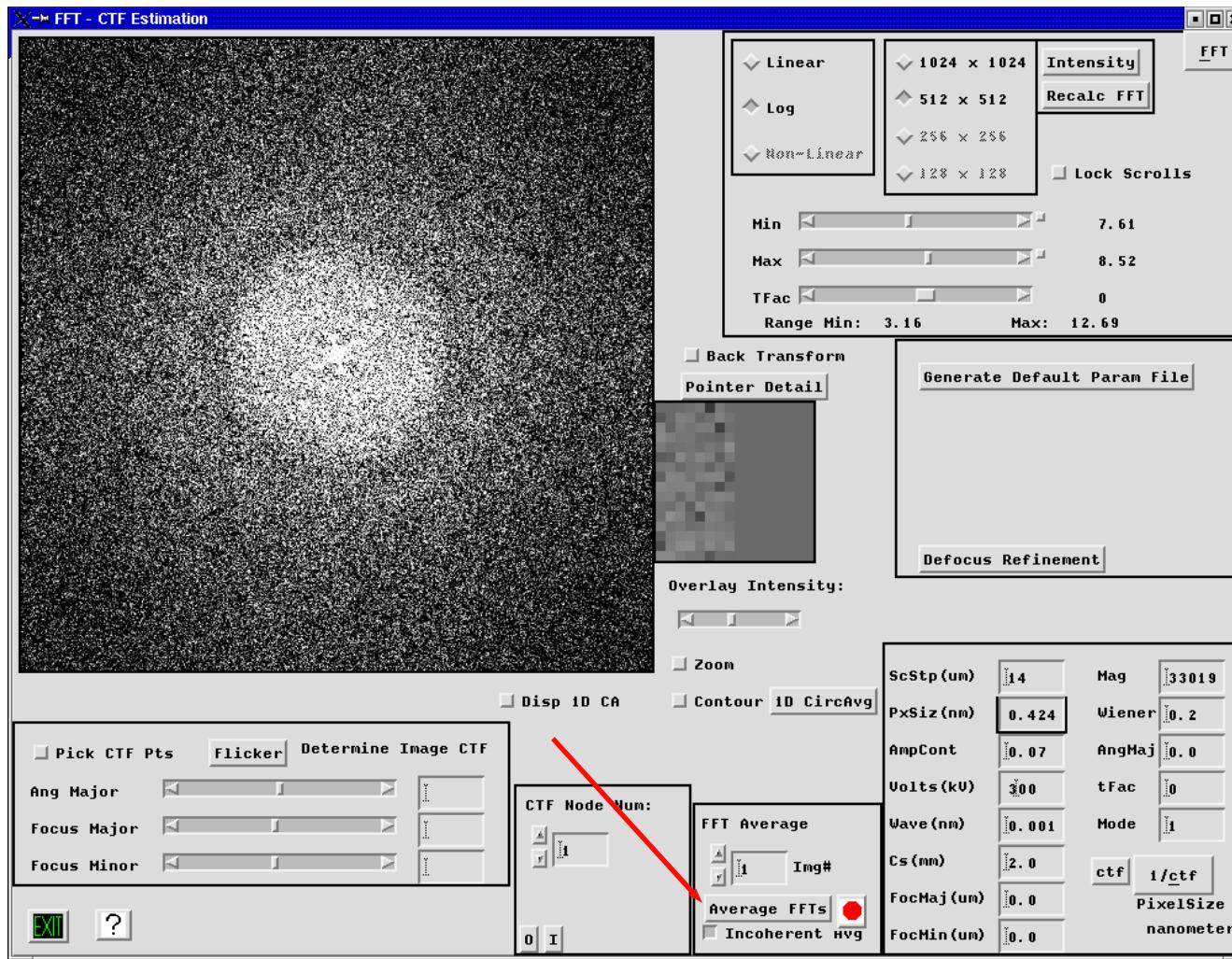
Pre-Process Images
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Icosahedral Virus 3D Reconstruction Scheme

↓

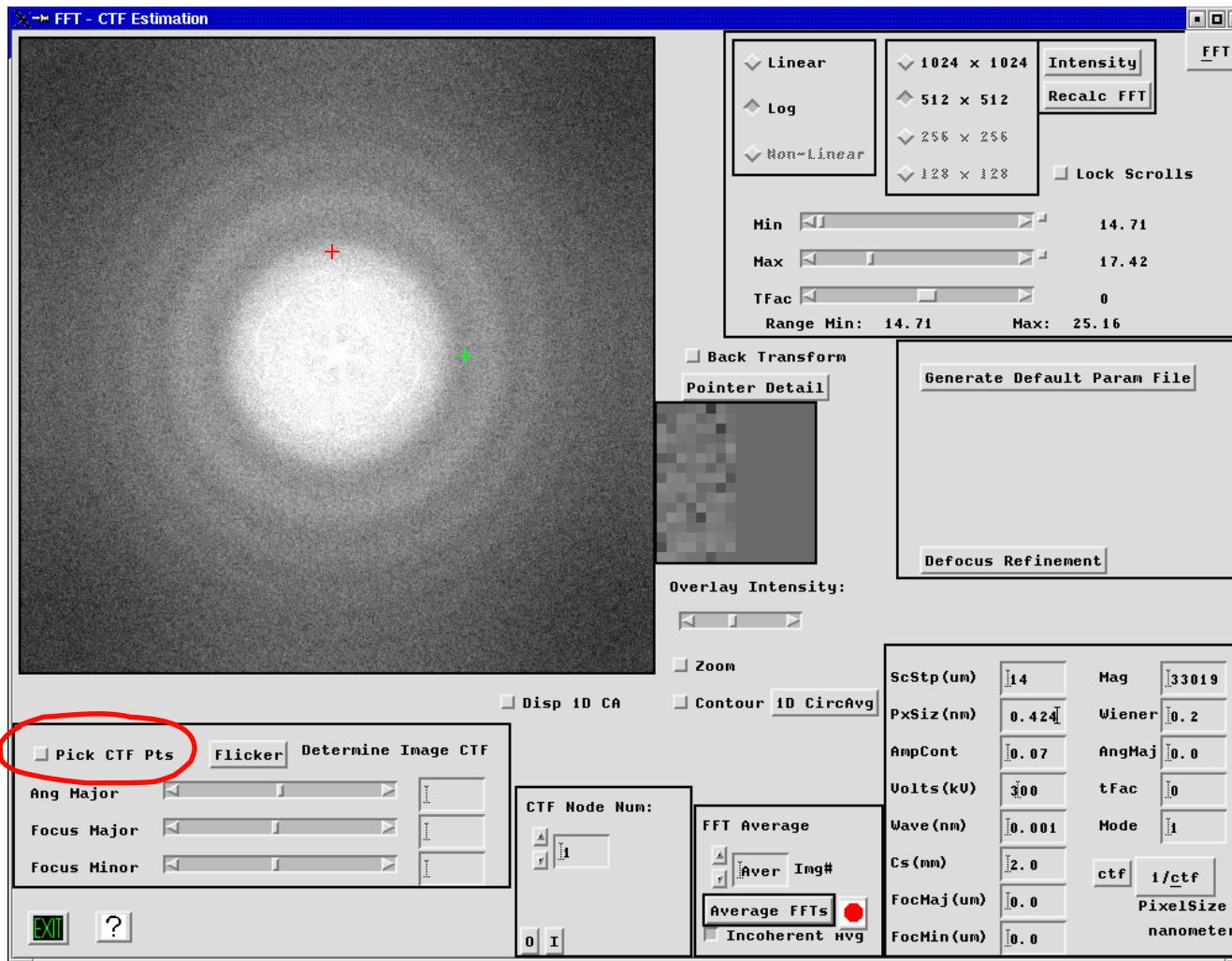
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Icosahedral Virus 3D Reconstruction Scheme

↓

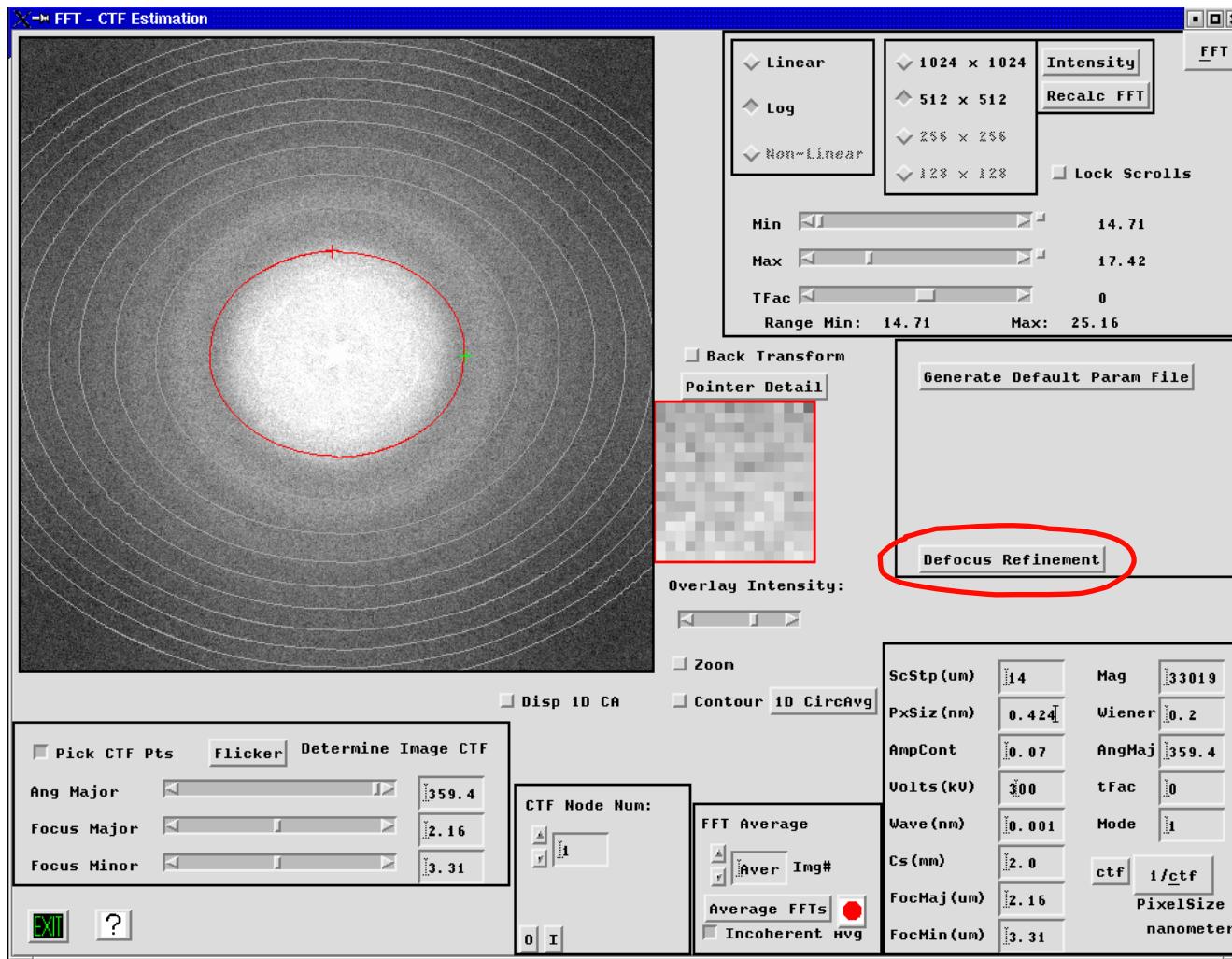
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Icosahedral Virus 3D Reconstruction Scheme

↓

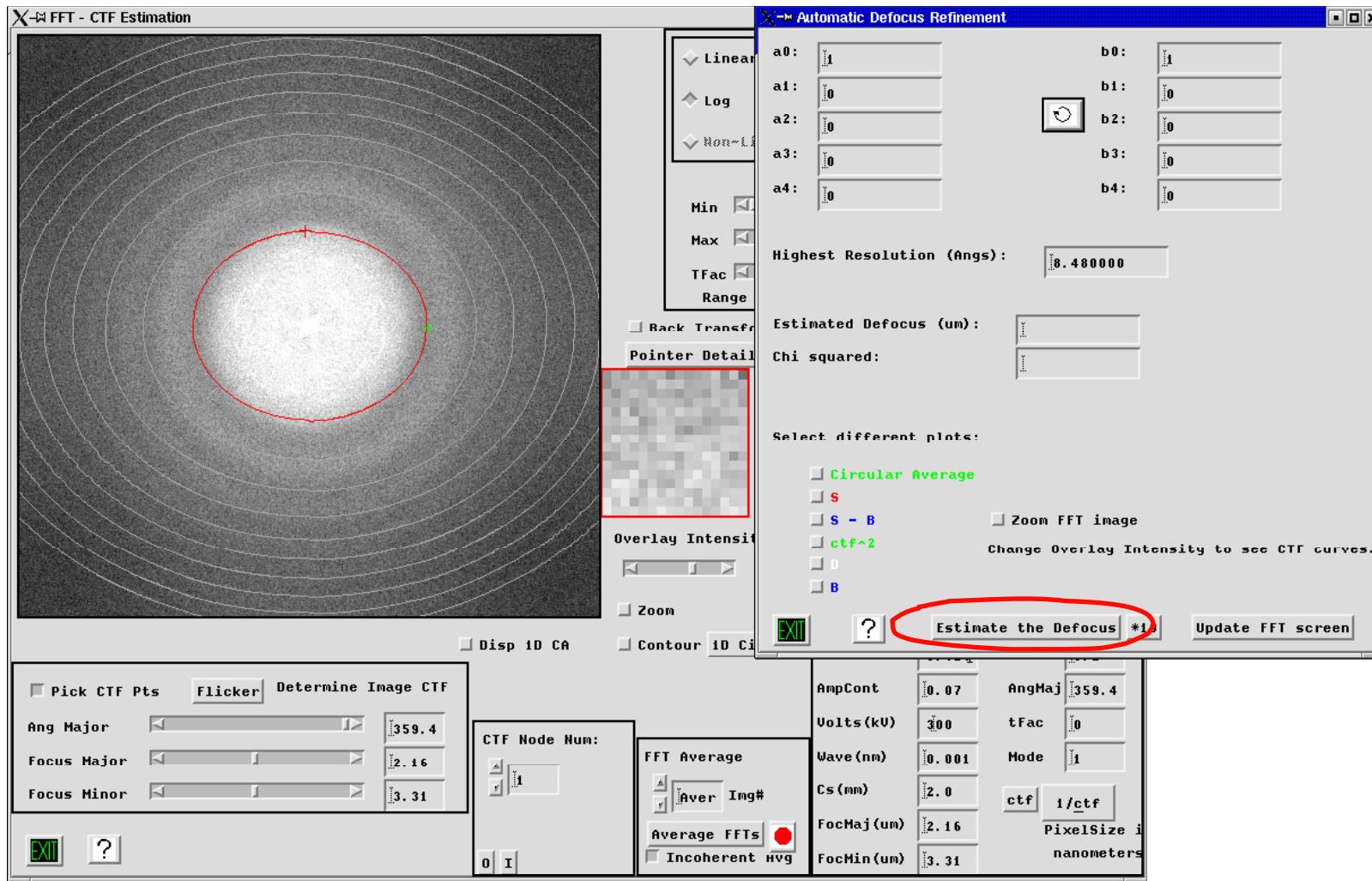
Pre-Process Images
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Icosahedral Virus 3D Reconstruction Scheme

↓

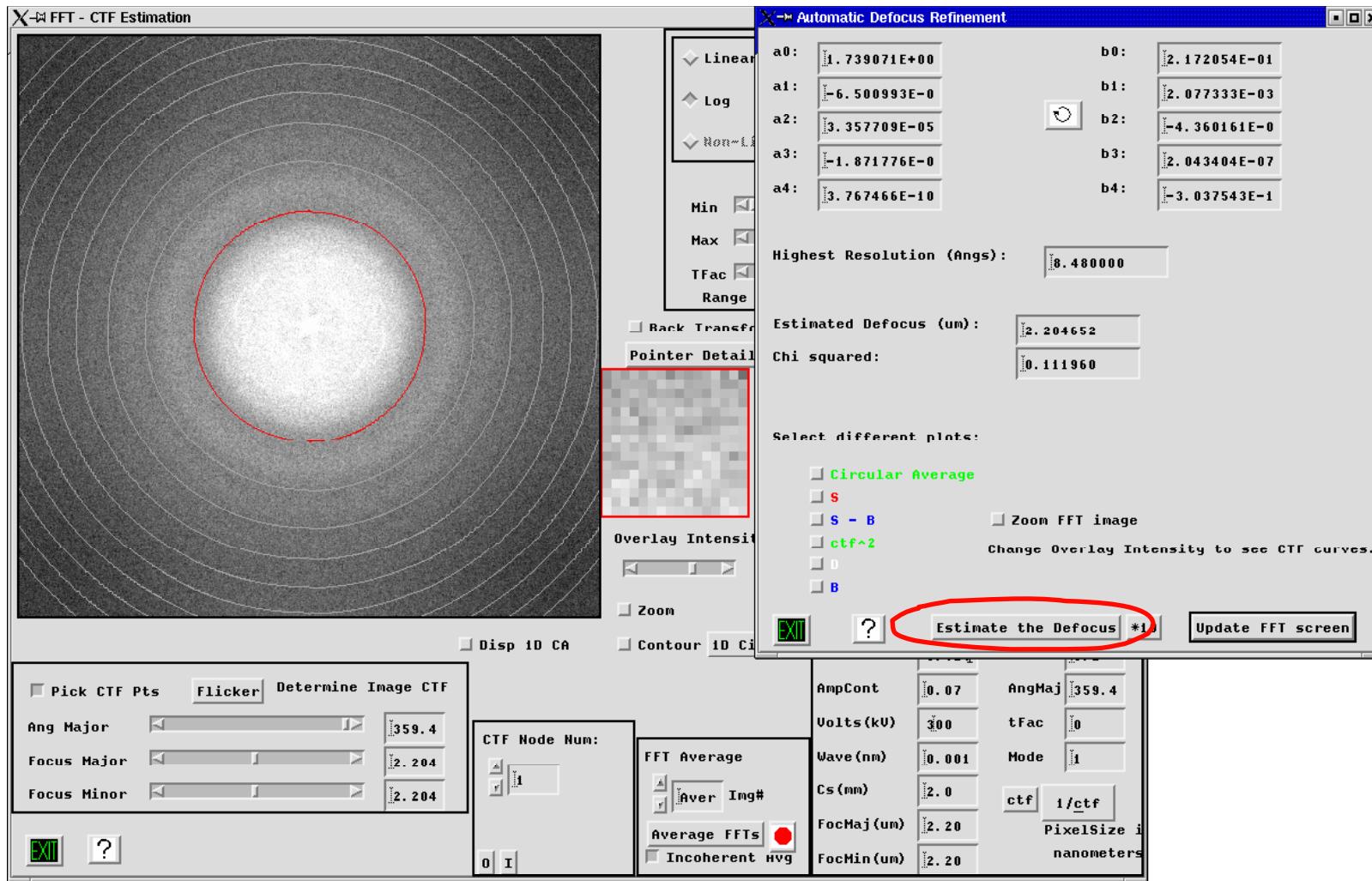
Pre-Process Images
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Icosahedral Virus 3D Reconstruction Scheme

↓

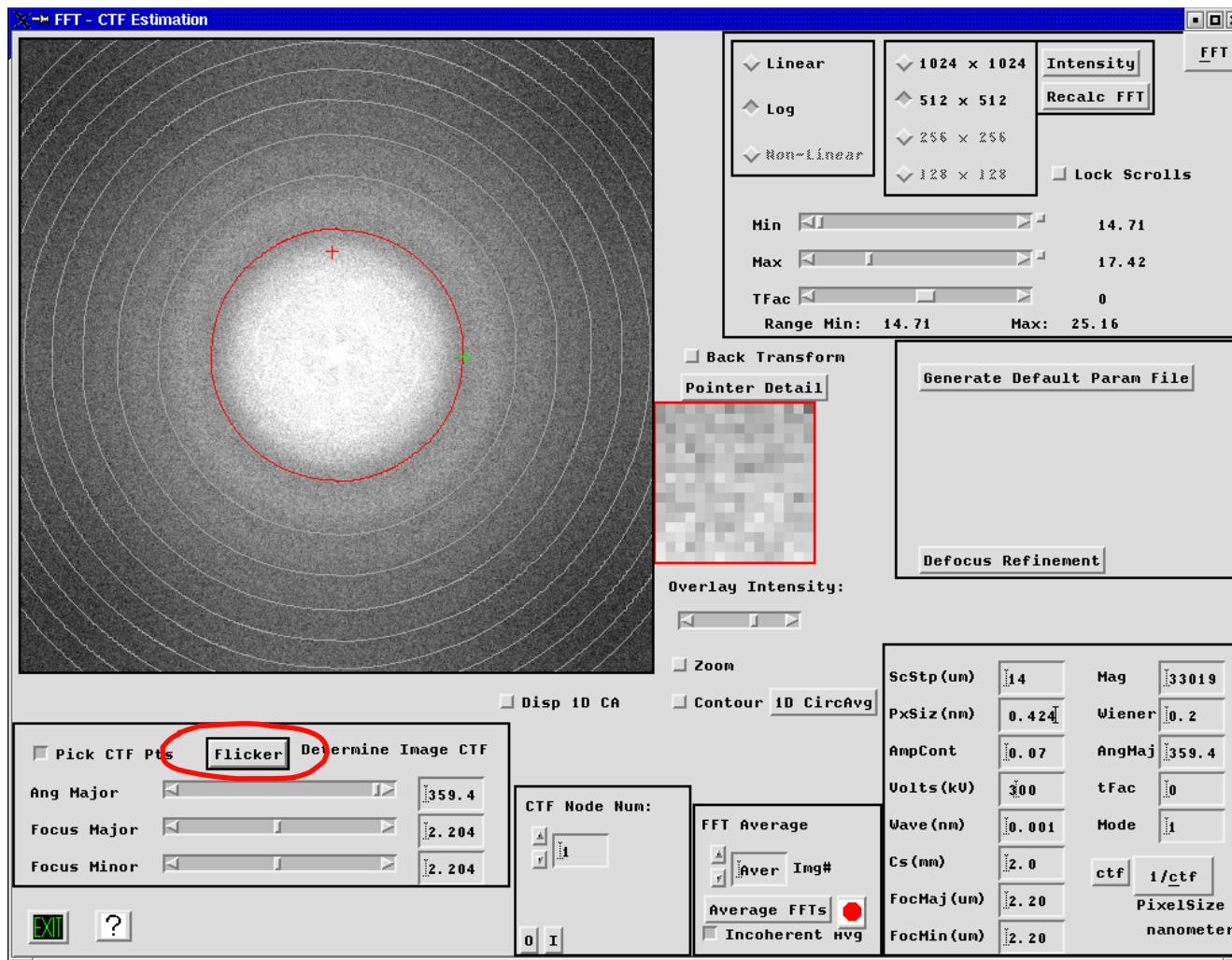
Pre-Process Images
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Icosahedral Virus 3D Reconstruction Scheme

↓

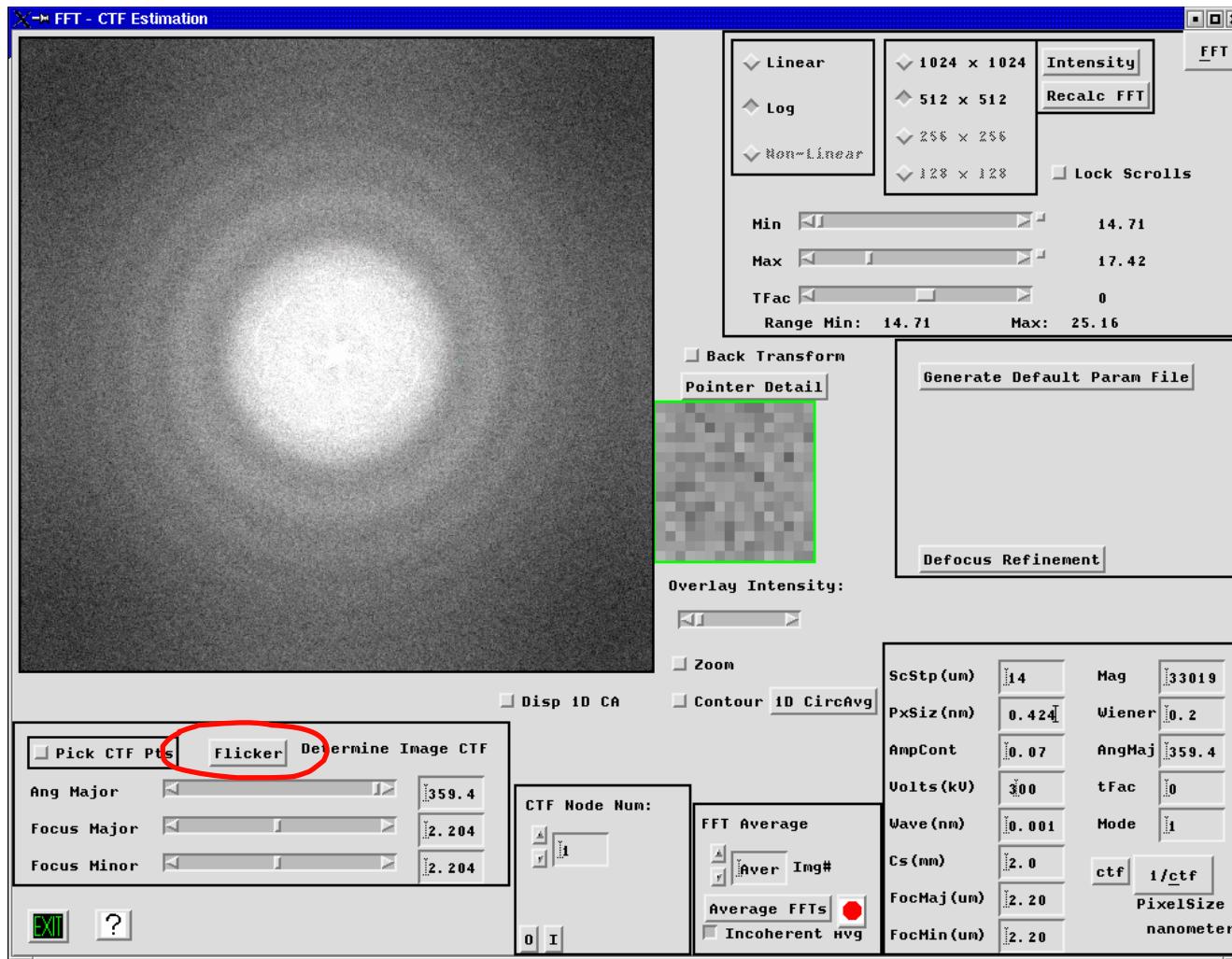
Pre-Process Images
Remove blemish, Remove Gradient
Normalize means/variances, Apodize
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Create Initial Parameter Files



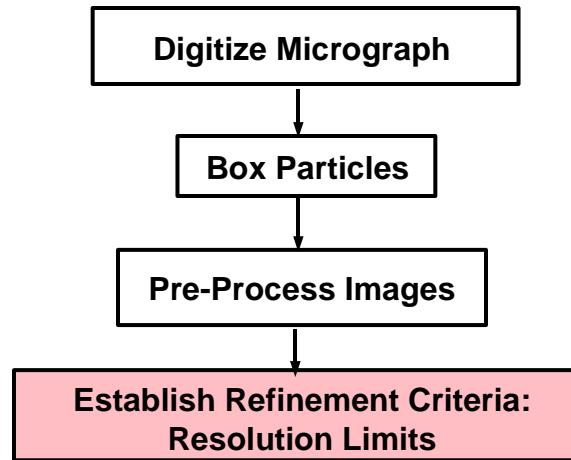
Icosahedral Virus 3D Reconstruction Scheme

↓

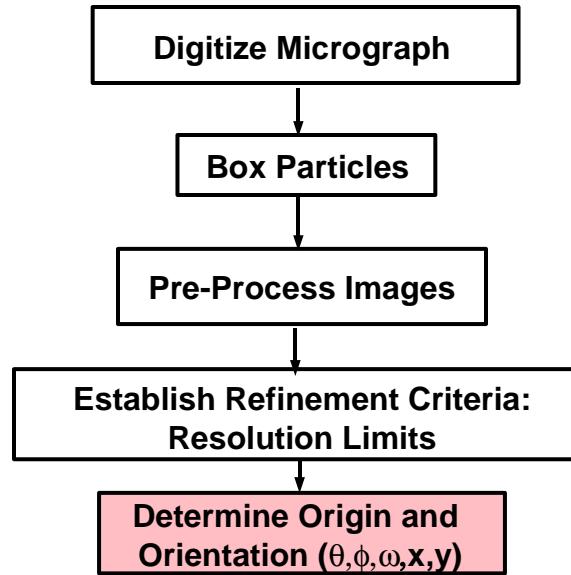
Pre-Process Images
Remove blemish, Remove Gradient
Normalize means/variances, Apodize
Determine CTF parameters
Create Initial Parameter Files



Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme

↓
Determine Origin and
Orientation ($\theta, \phi, \omega, x, y$)

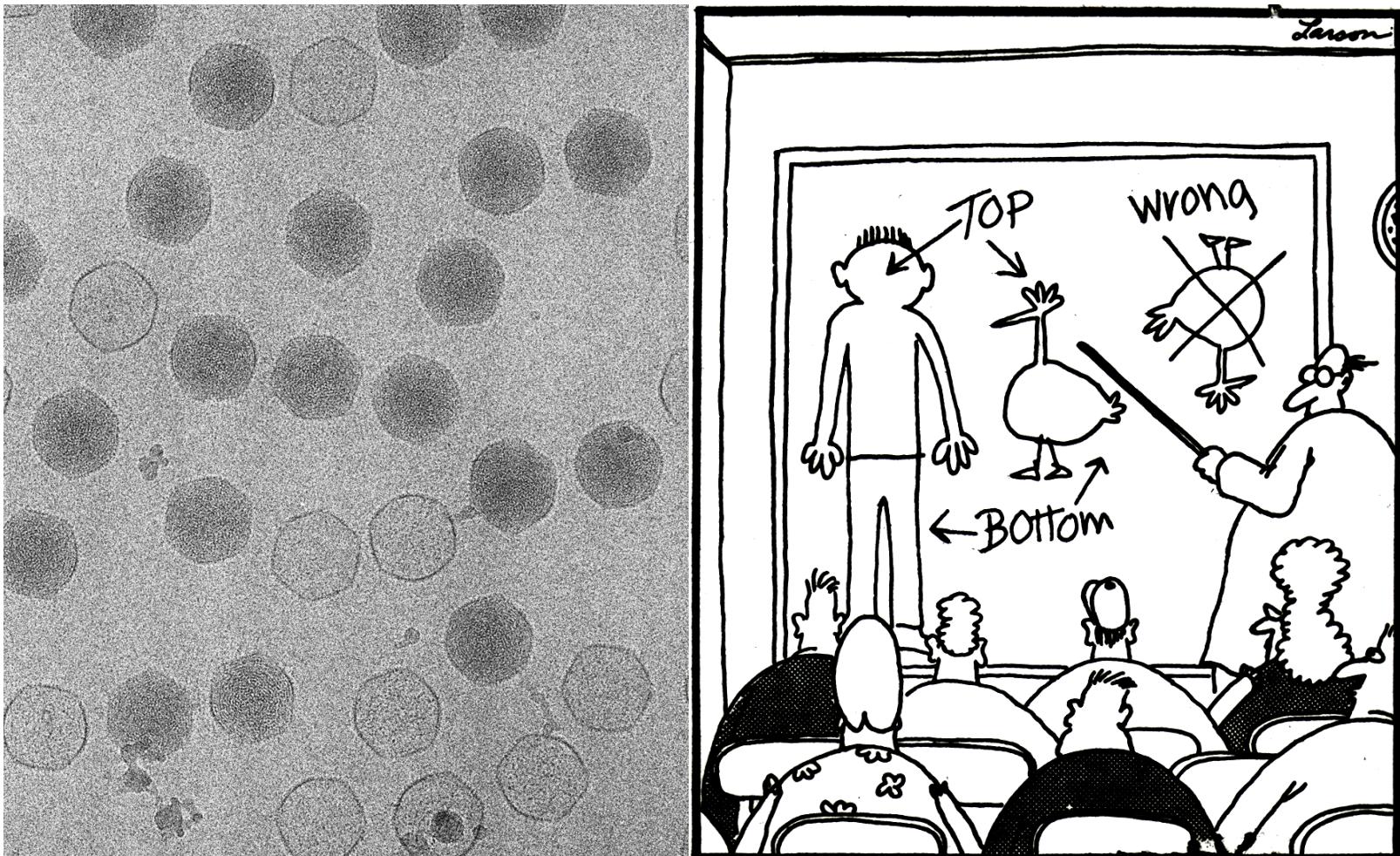
Goal: determine phase origin and view orientation for each boxed particle

MOST IMPORTANT STEP?

Garbage in -----> garbage out

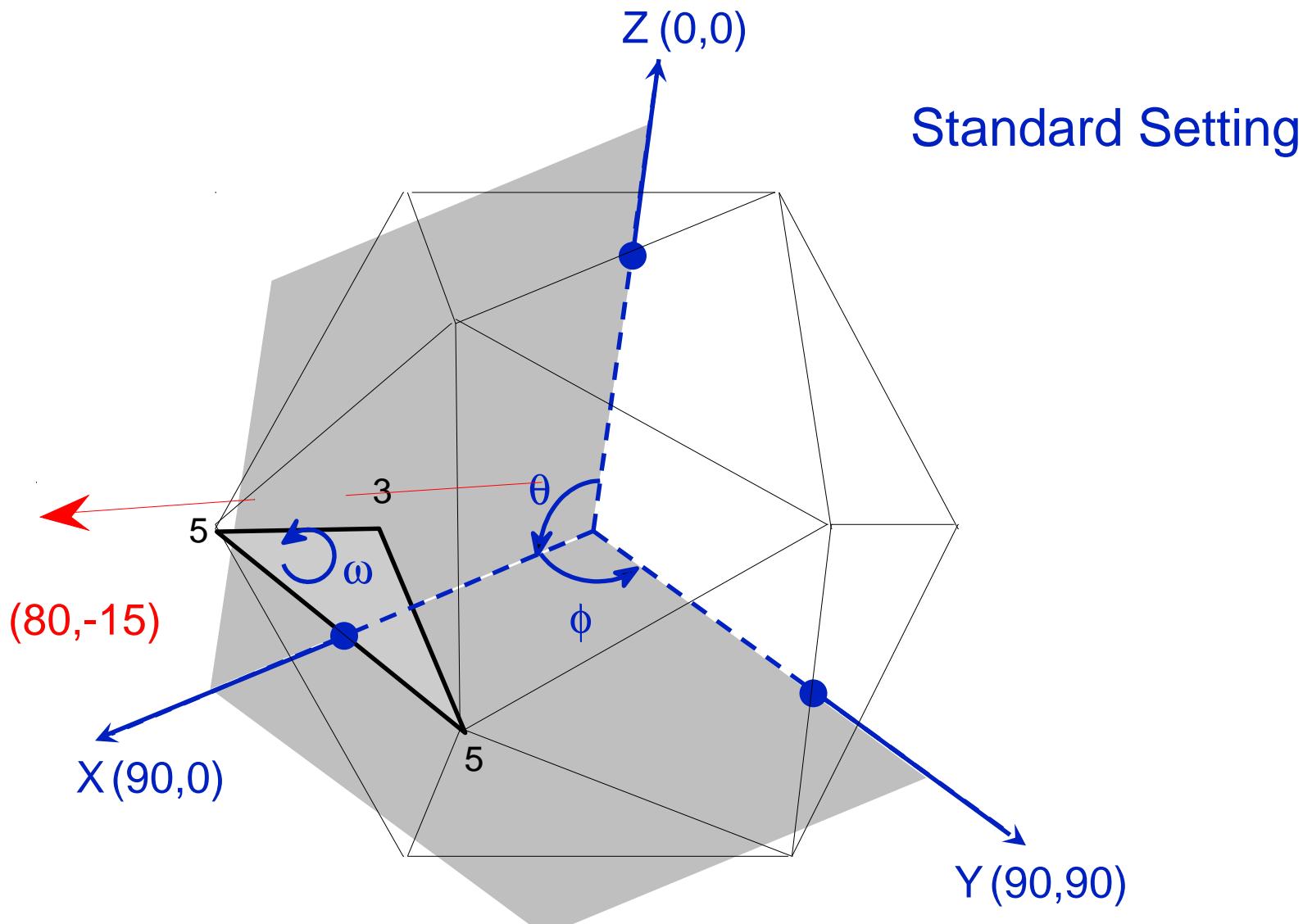
Icosahedral Virus 3D Reconstruction Scheme

Determine Origin and Orientation ($\theta, \phi, \omega, x, y$)

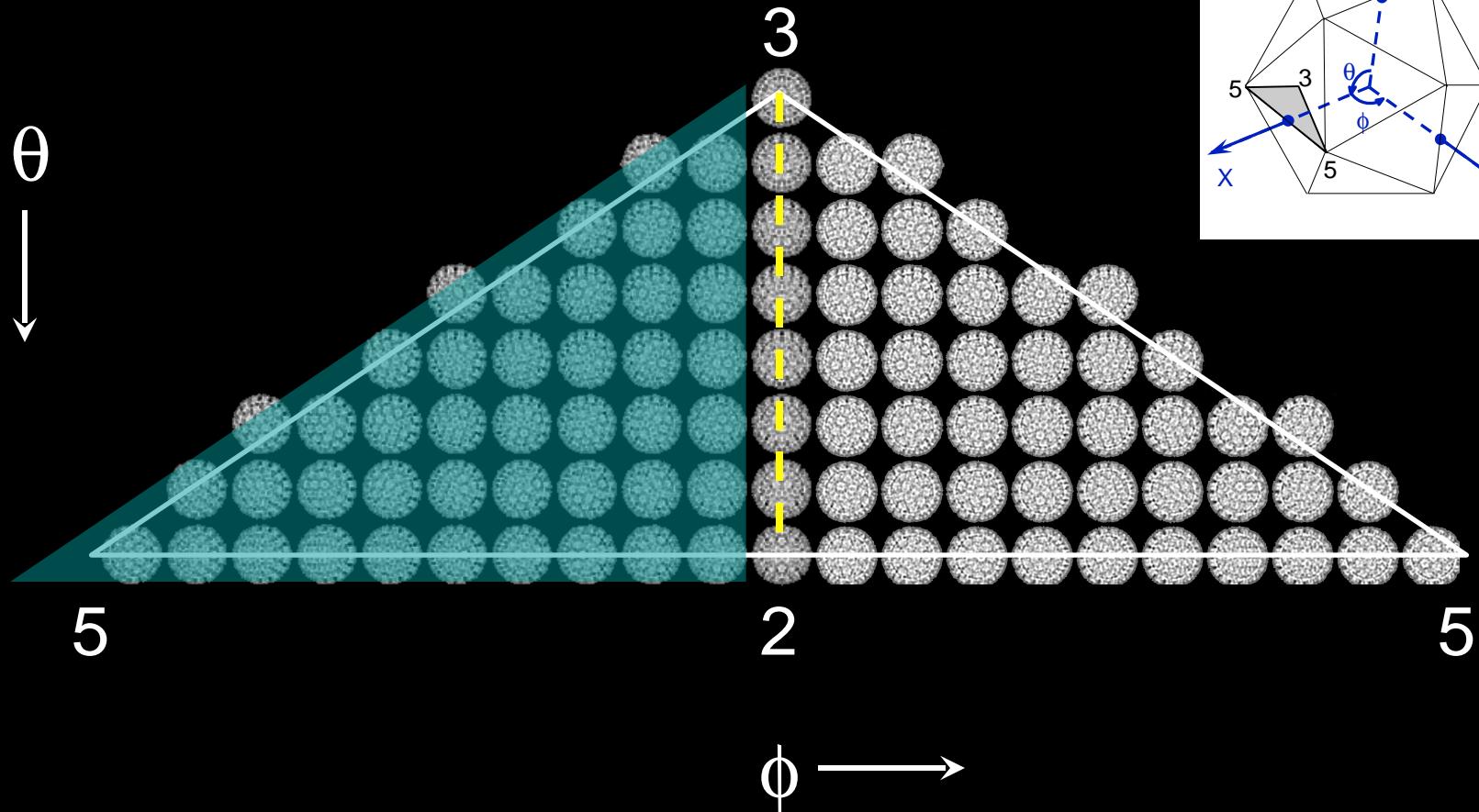


People who don't know which end is up

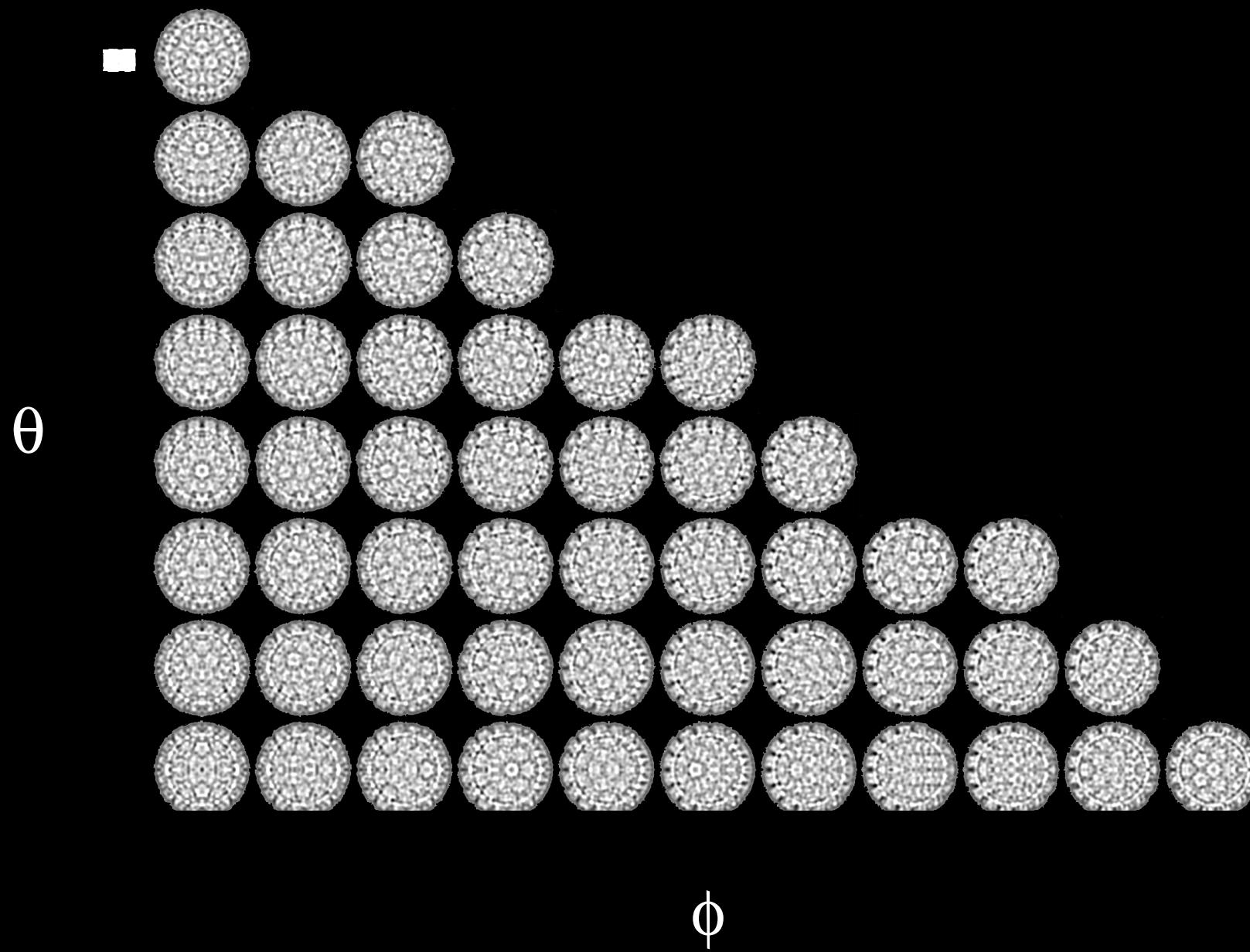
Specifying Direction of View: (θ, ϕ, ω) Orientation



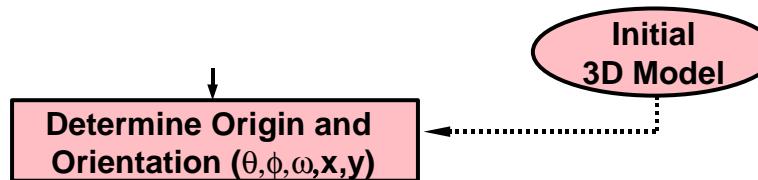
BPV Projections: Icosahedral ASU



BPV Projections: 1/2 Icosahedral ASU



Icosahedral Virus 3D Reconstruction Scheme



How do we determine the $(\theta, \phi, \omega, x, y)$ parameters?

Two methods:

1. Common lines

New or unknown structure

2. Model-based (template) matching

General features of structure are known or a crude model can be generated

Icosahedral Virus 3D Reconstruction Scheme

↓
Determine Origin and
Orientation ($\theta, \phi, \omega, x, y$)

How do we determine the $(\theta, \phi, \omega, x, y)$ parameters?

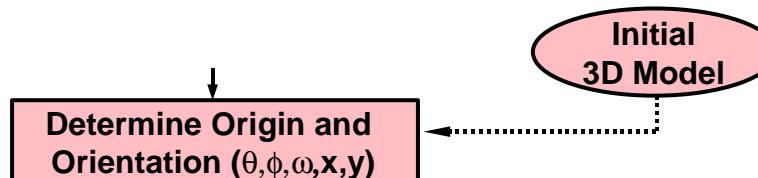
Two methods:

1. *Ab initio* (e.g. Common lines)

New or unknown structure

2. By guess and by golly

Icosahedral Virus 3D Reconstruction Scheme



How do we determine the $(\theta, \phi, \omega, x, y)$ parameters?

Two methods:

1. *Ab initio* (e.g. Common lines)

New or unknown structure

2. Model-based (template) matching

General features of structure are known or a crude model can be generated (...or, sometimes, even a lousy model will work)

Icosahedral Virus 3D Reconstruction Scheme

↓
Determine Origin and
Orientation ($\theta, \phi, \omega, x, y$)

Common Lines

The ‘gospel’ according to Tony Crowther (*Phil. Trans. R. Soc. Lond. B.*(1971) 261:221-230)

“[Common lines] arise as follows:”

“An observed section of the transform intersects an identical symmetry-related section in a *line*, along which the transform must have the *same value in both sections*”

“The common line lies in the original section.”

“However, regarded as lying in the symmetry-related section it must have been generated by the symmetry operation from some other line in the original section.”

Icosahedral Virus 3D Reconstruction Scheme

↓
Determine Origin and
Orientation ($\theta, \phi, \omega, x, y$)

Common Lines

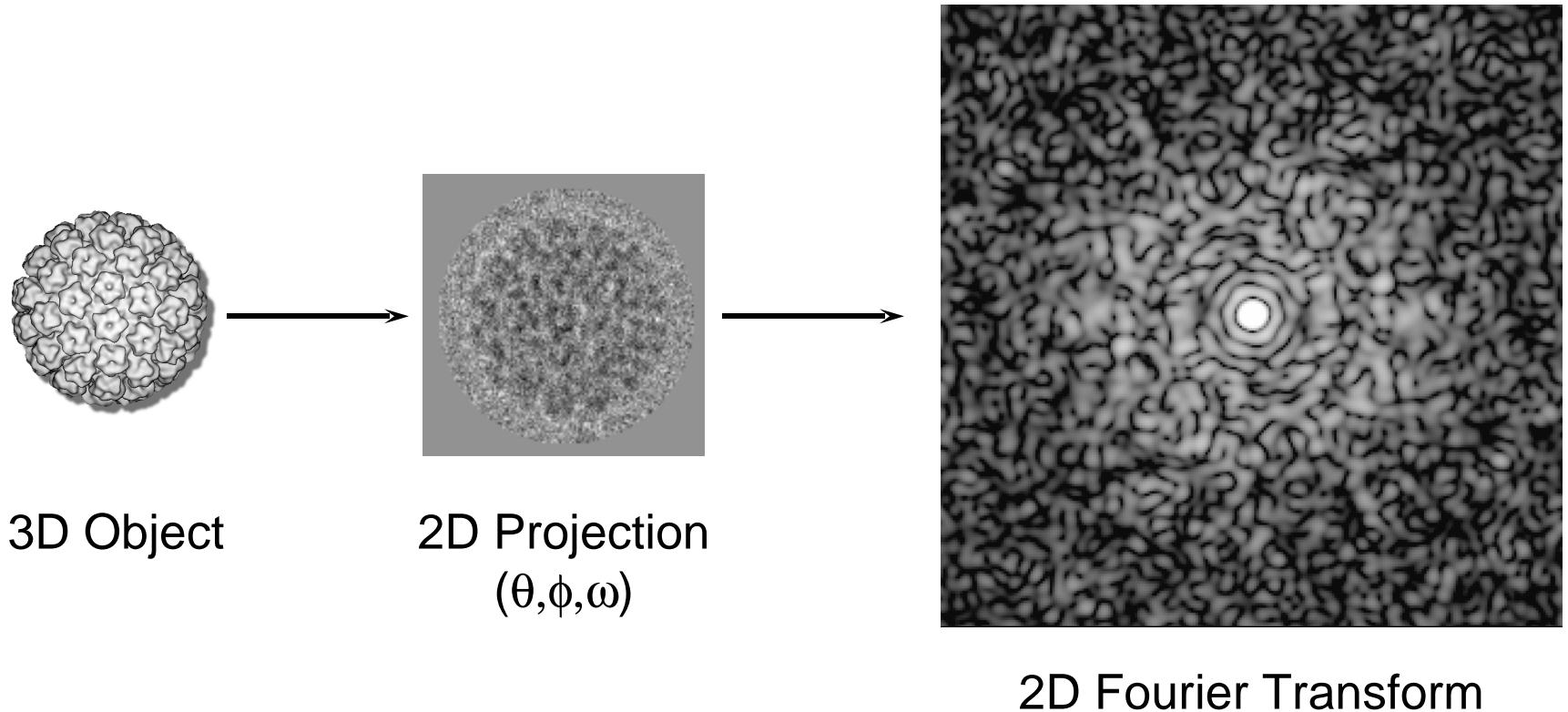
The ‘gospel’ continued:

“We therefore have a *pair of lines in the original transform plane along which the transform must have identical values*”

“A similar pair of lines will be generated by each possible choice of pairs of symmetry operations”

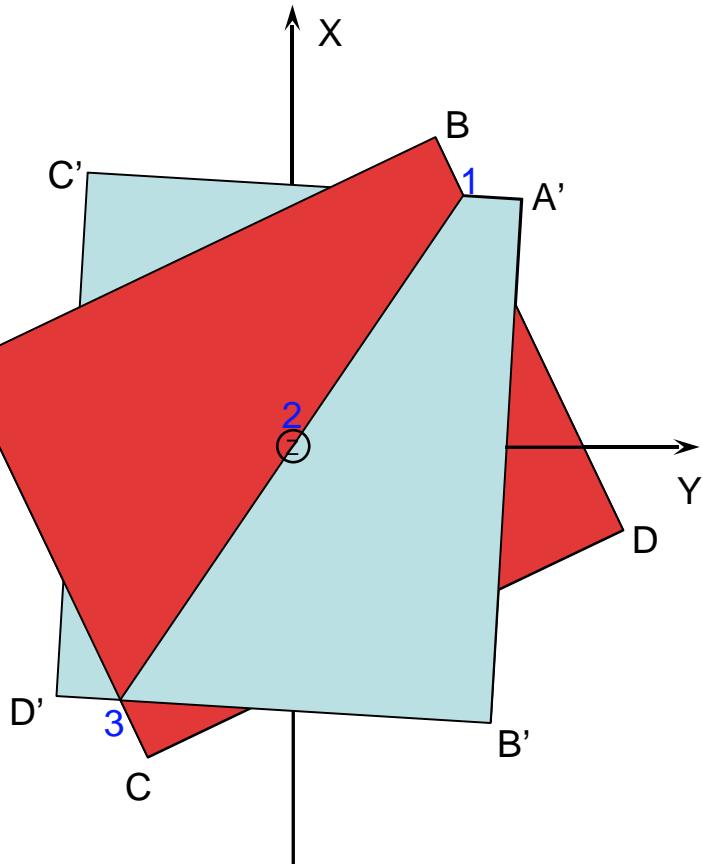
“The angular positions of these lines are dependent on the orientation of the particle.”

Orientation Determination by Common Lines



Orientation Determination by Common Lines

Simple example: object with single three-fold axis of symmetry



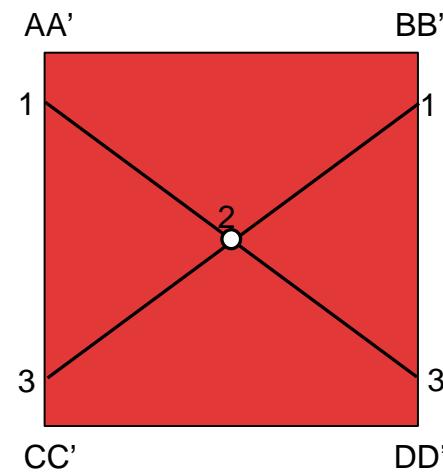
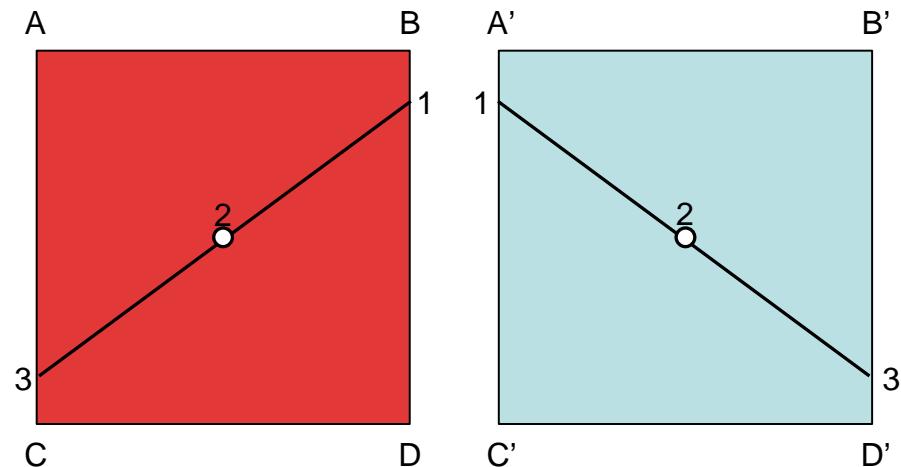
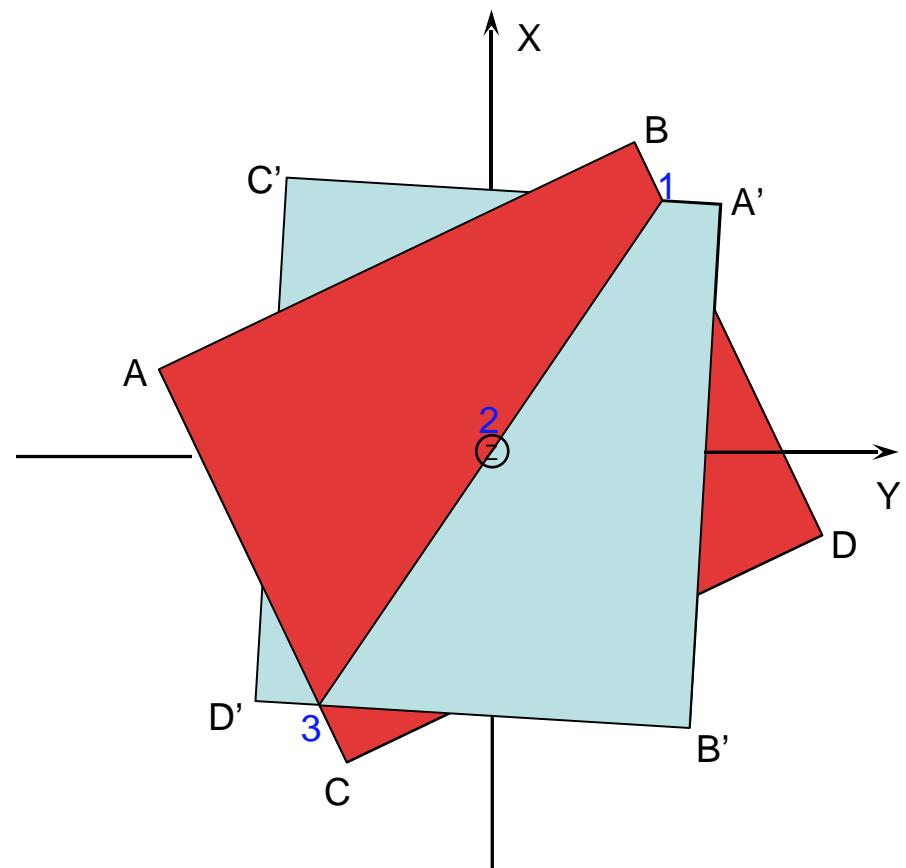
$ABCD = 2D$ transform of image from particle **not** viewed along an axis of symmetry

Let Z-direction coincide with **3-fold** axis of symmetry

3-fold operation generates **two** additional FT sections (only $A'B'C'D'$ is shown)

Both planes have **common values** along the **line** (1,2,3) of their intersection

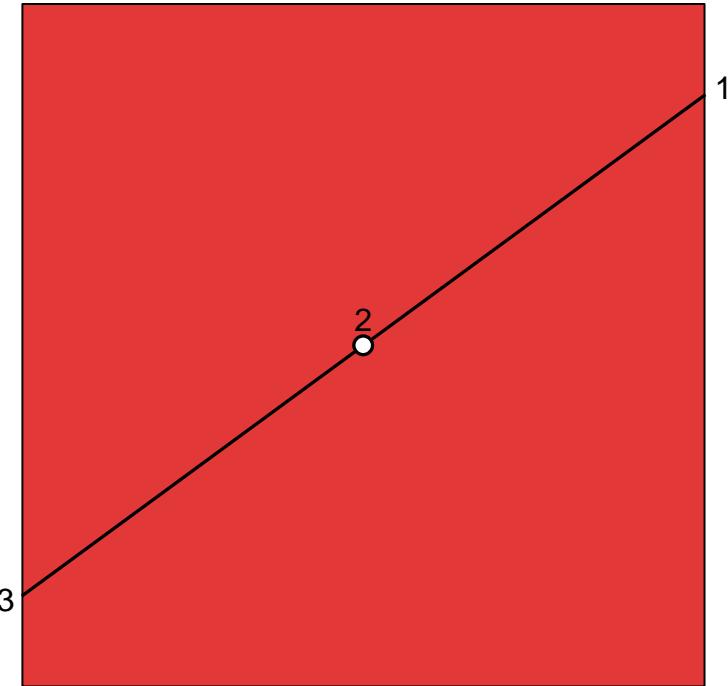
Orientation Determination by Common Lines



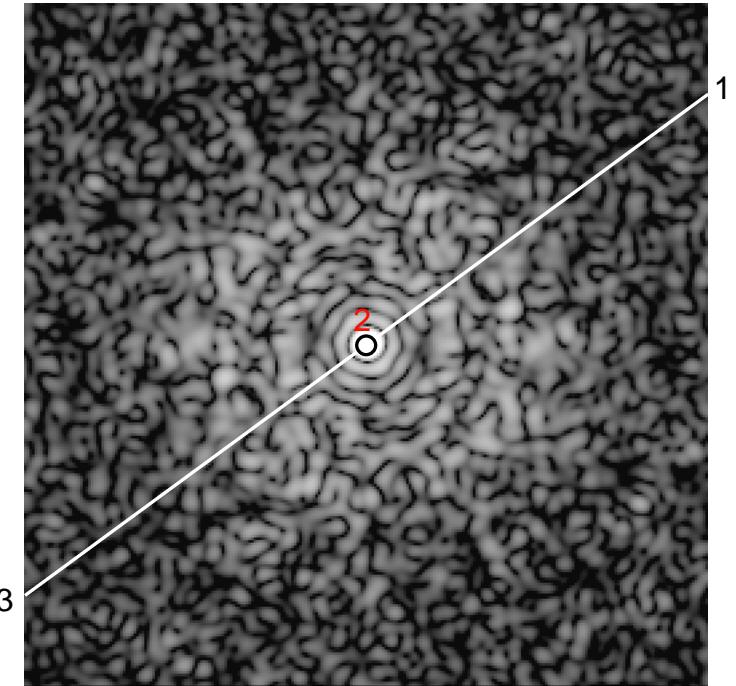
Adapted from Moody (1990) Fig. 7.68,
p.245

Adapted from Moody (1990) Fig. 7.69, p.246

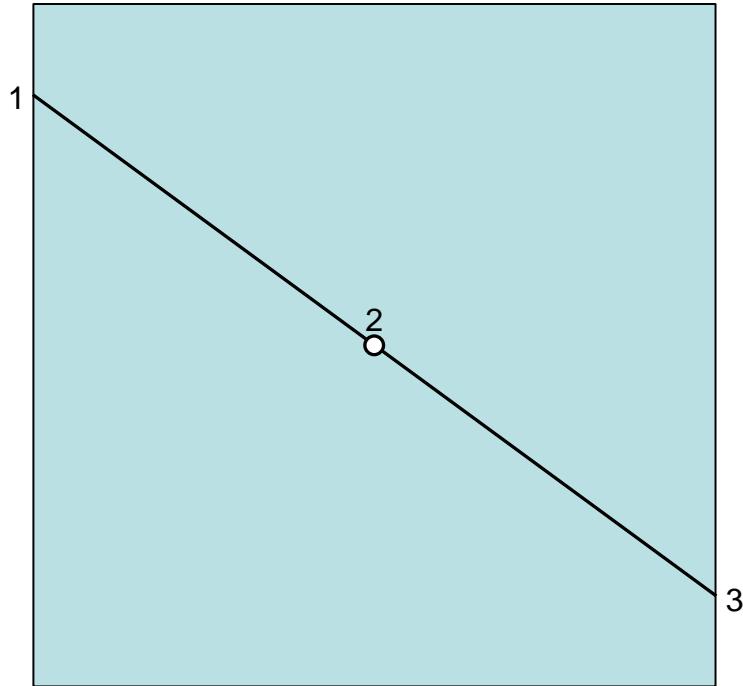
Orientation Determination by Common Lines



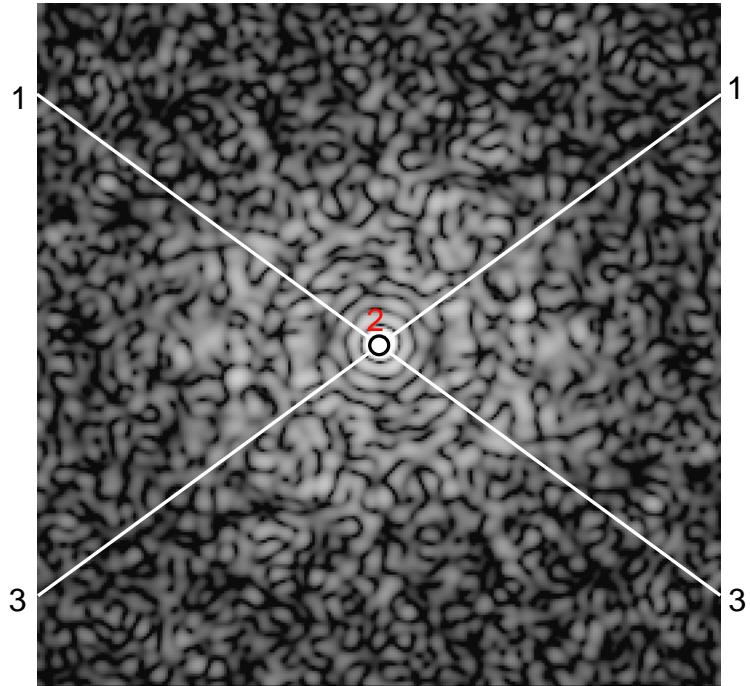
Original Transform Plane



Orientation Determination by Common Lines



Symmetry-Related
Transform Plane



Orientation Determination by Common Lines

Ok, that's easy (simple object with single 3-fold axis)

What about an object with 532 symmetry?

For a **general view**, icosahedral symmetry generates:

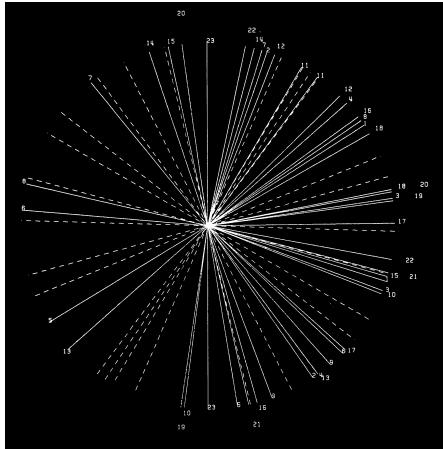
$$5\text{-folds: } \frac{12}{2} \times 2 = 12 \text{ pairs}$$

$$3\text{-folds: } \frac{20}{2} \times 1 = 10 \text{ pairs}$$

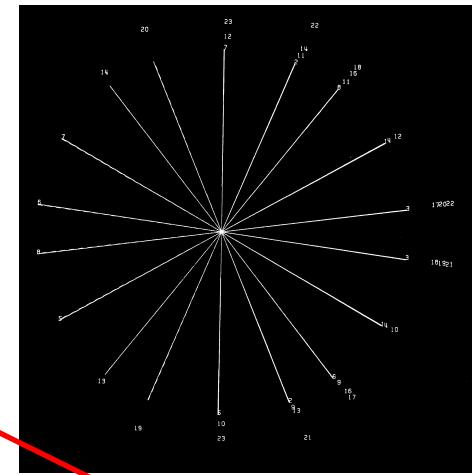
$$2\text{-folds: } \frac{30}{2} \times 1 = \underline{15} \text{ real lines}$$

37 common lines

Orientation Determination by Common Lines

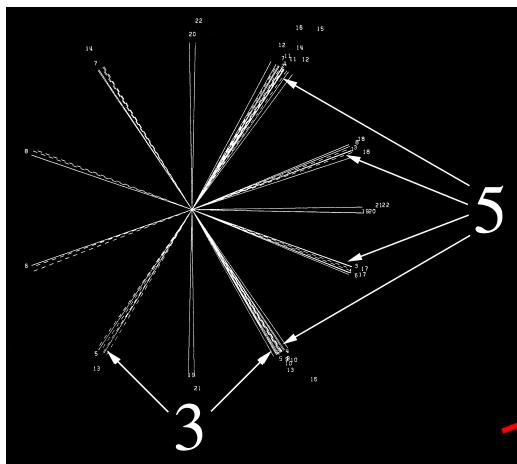


(80,11)

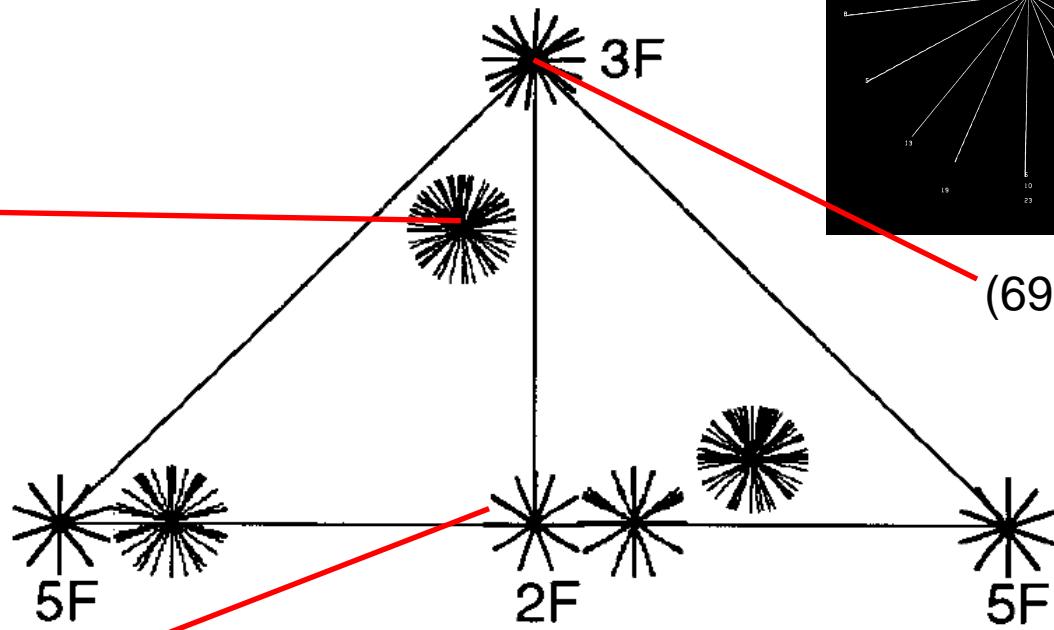


3F

(69,0)



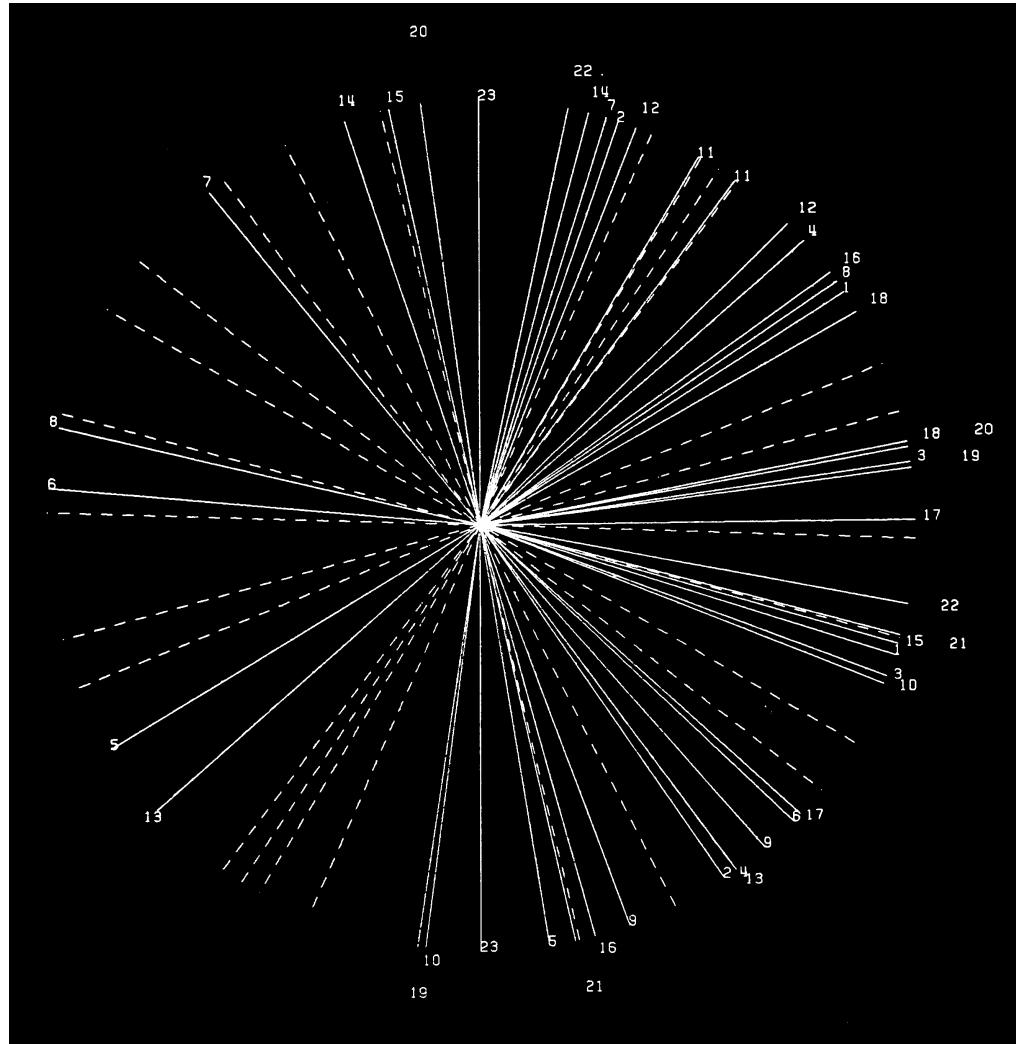
3



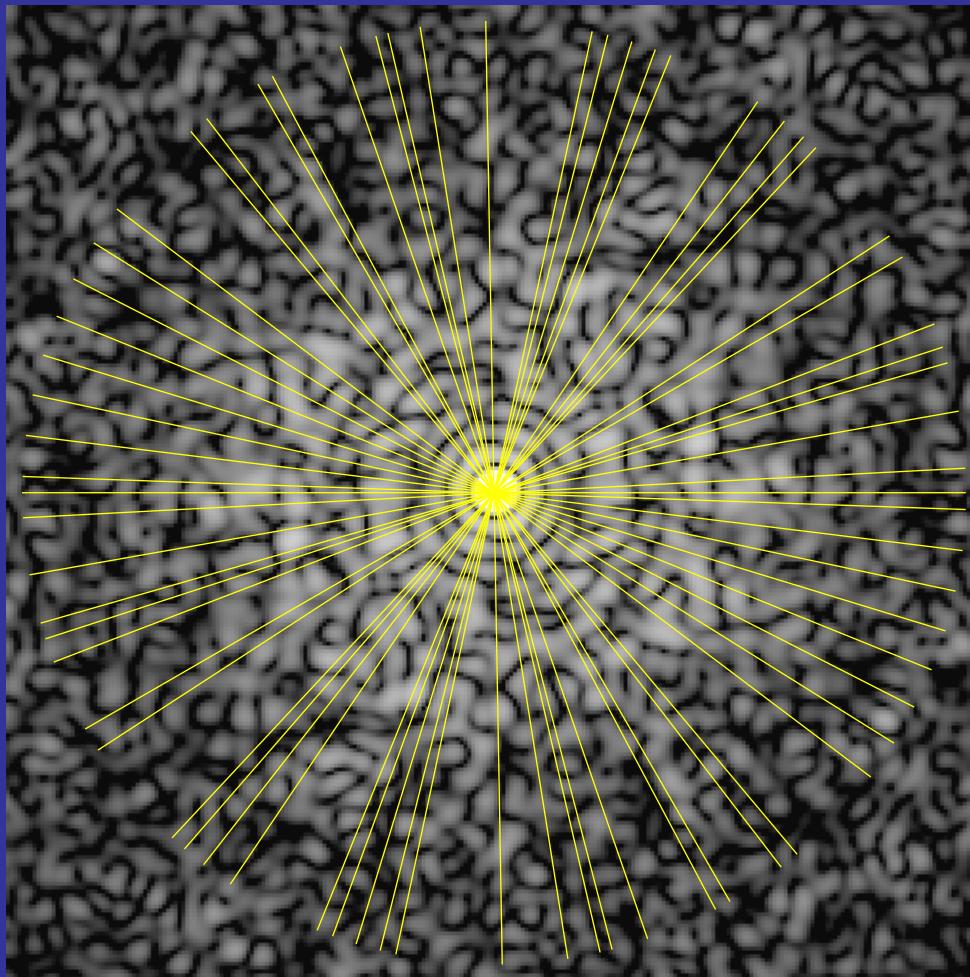
2F

5F

Orientation Determination by Common Lines



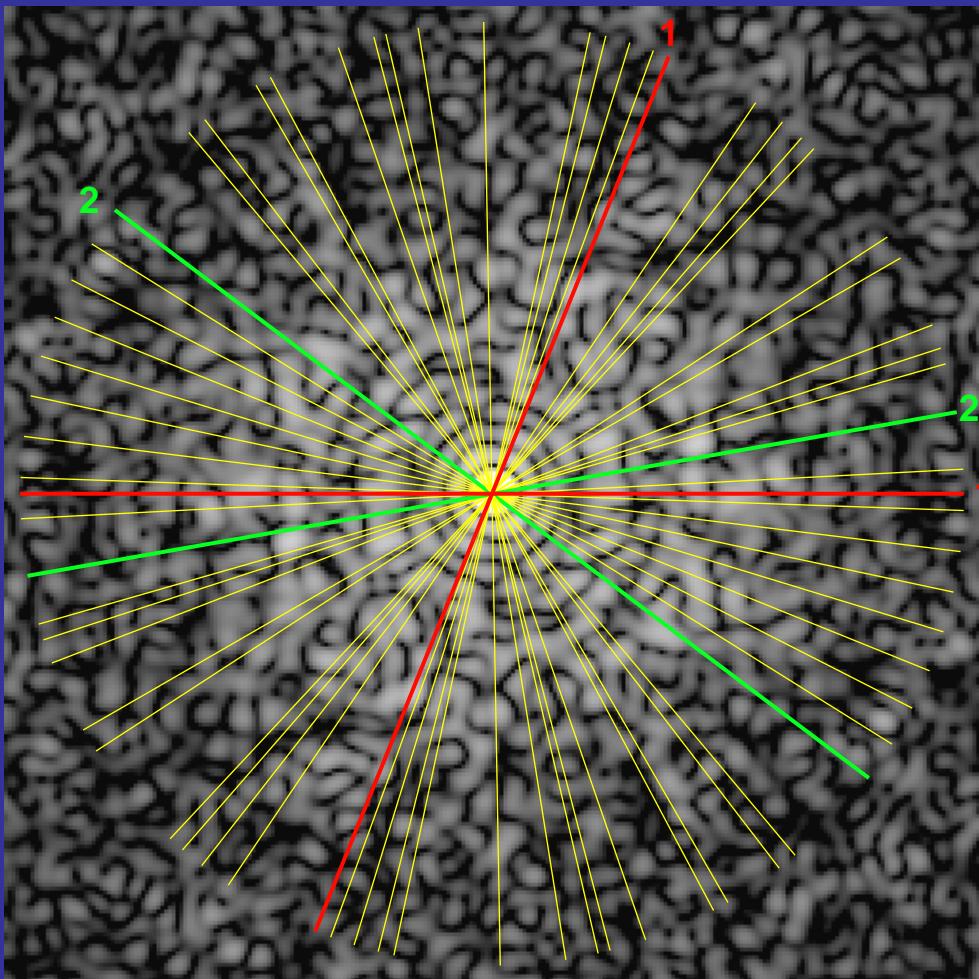
Orientation Determination by Common Lines



(80,11)

What is (θ, ϕ, ω) for this particle?

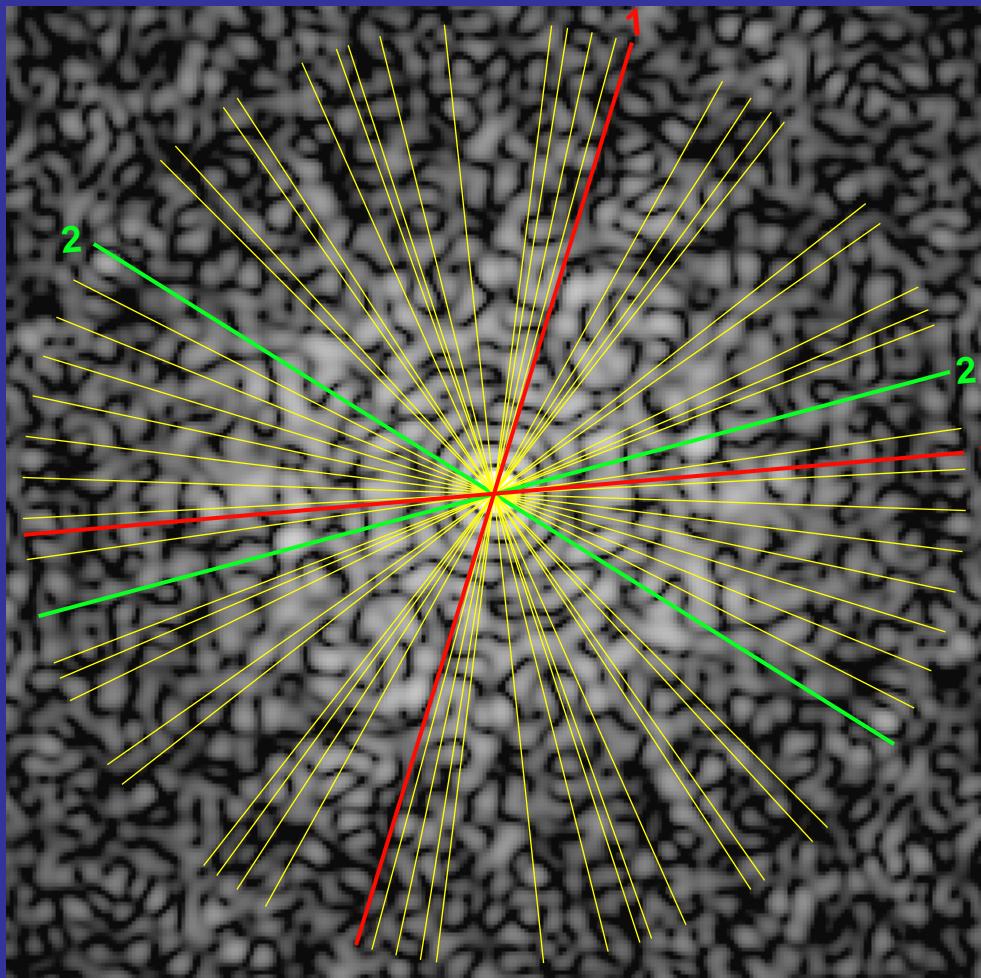
Orientation Determination by Common Lines



ω

(80,11,0)

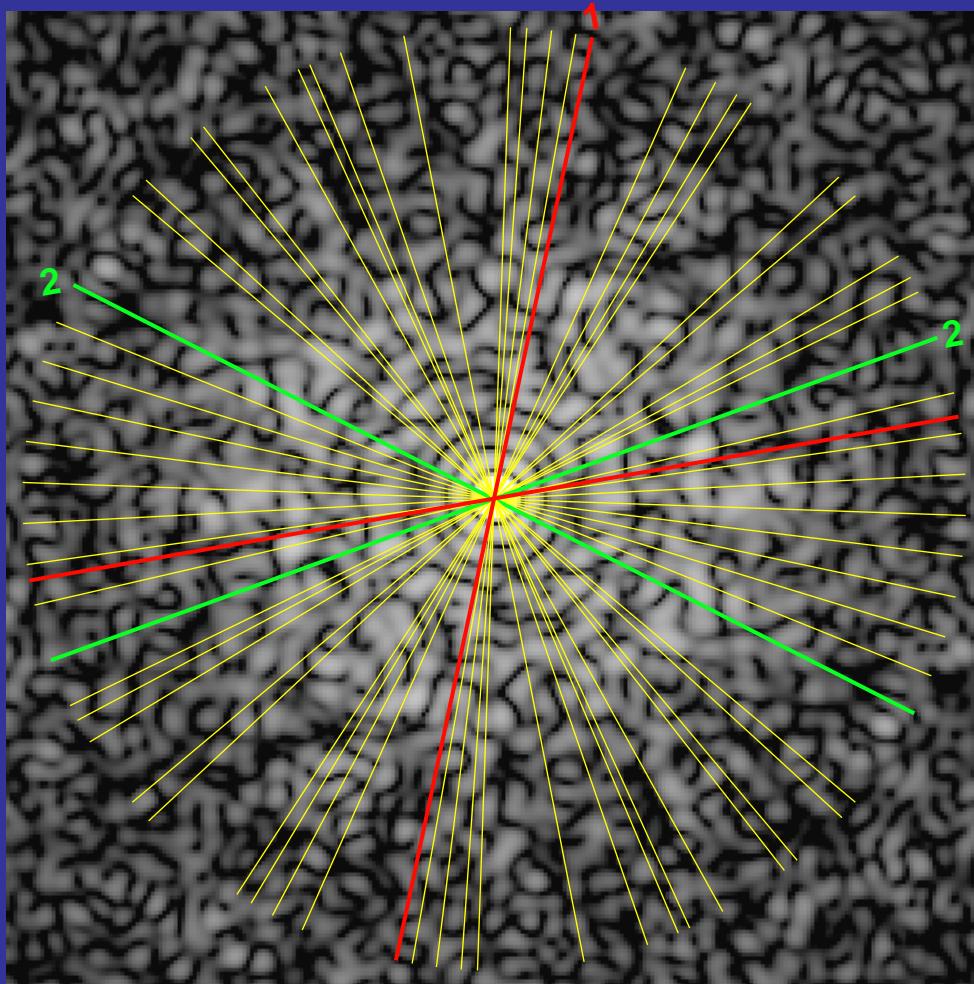
Orientation Determination by Common Lines



ω

(80,11,5)

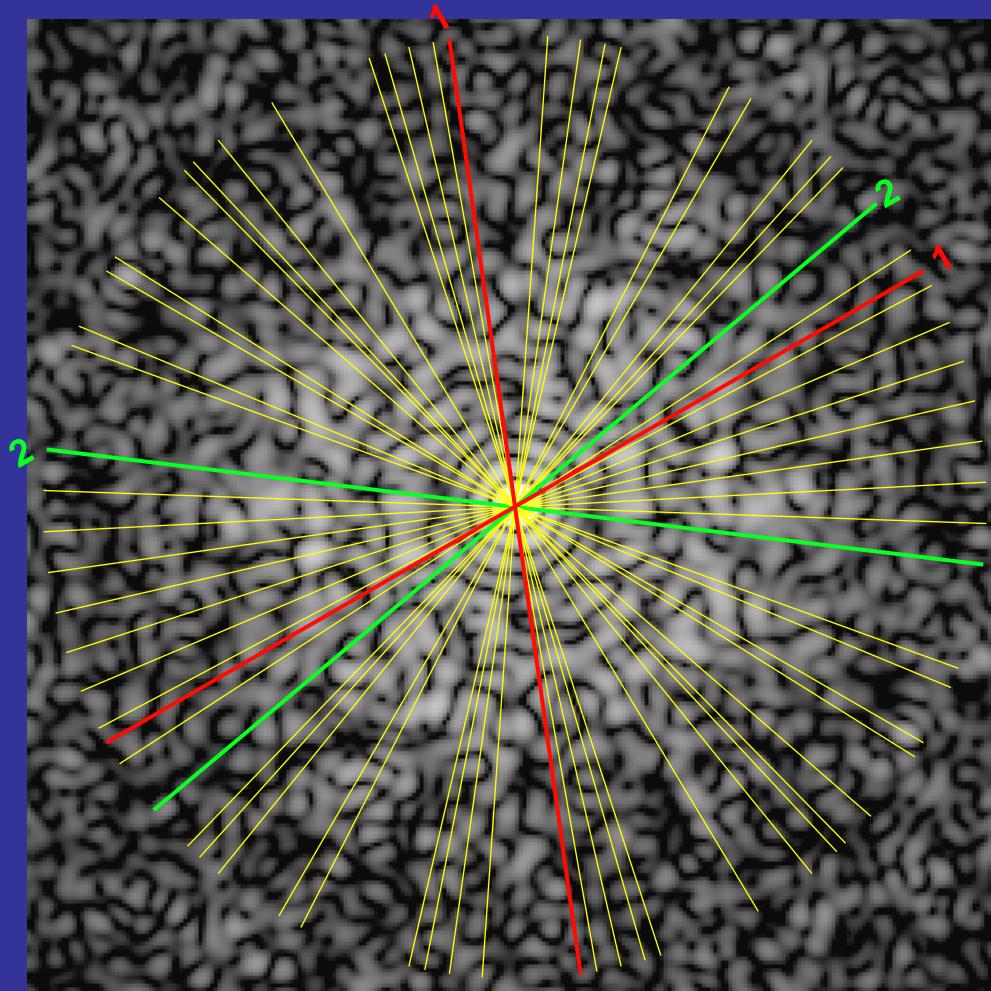
Orientation Determination by Common Lines



ω

(80,11,10)

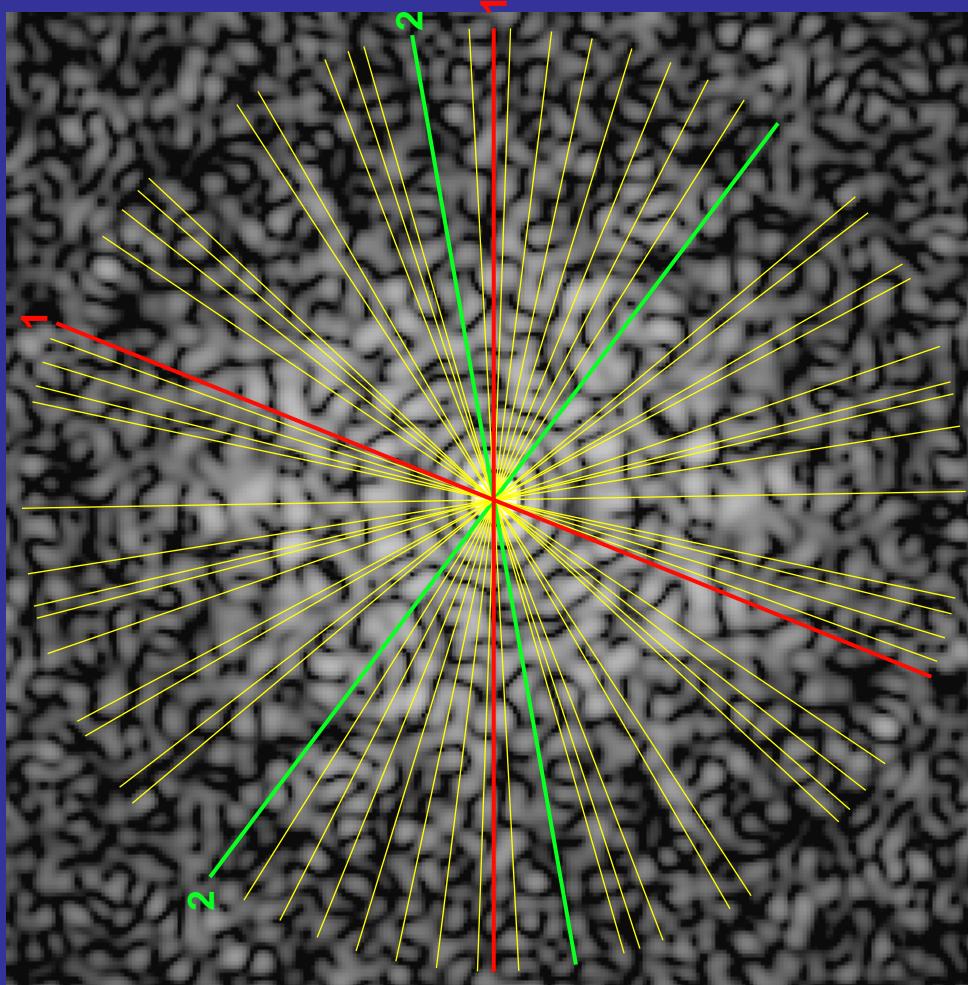
Orientation Determination by Common Lines



ω

(80,11,30)

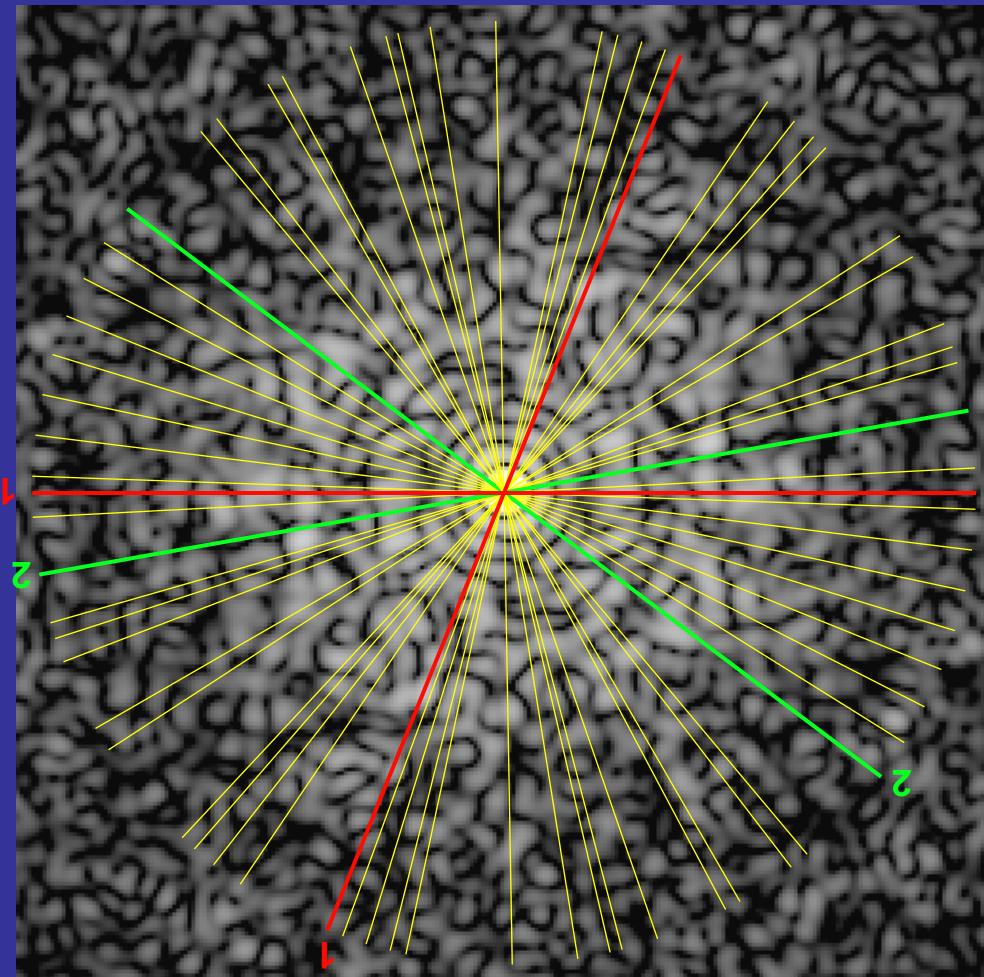
Orientation Determination by Common Lines



ω
↓

(80,11,90)

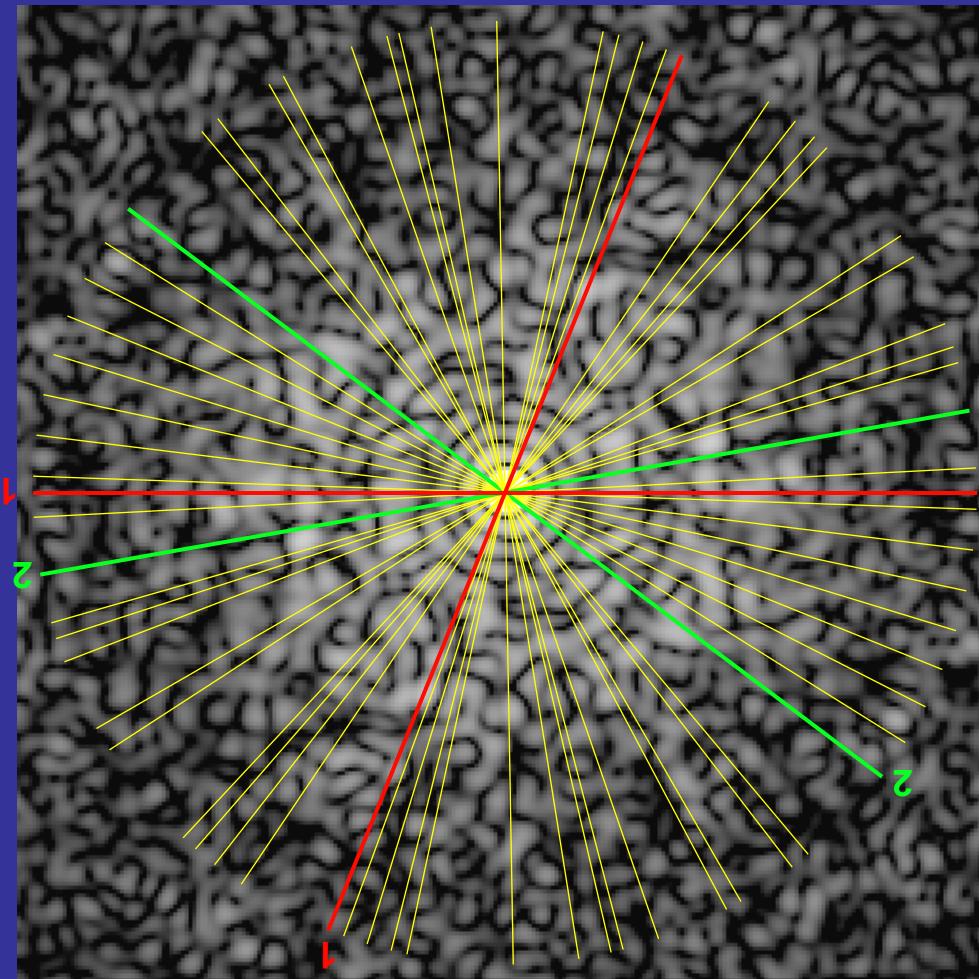
Orientation Determination by Common Lines



ω
↓

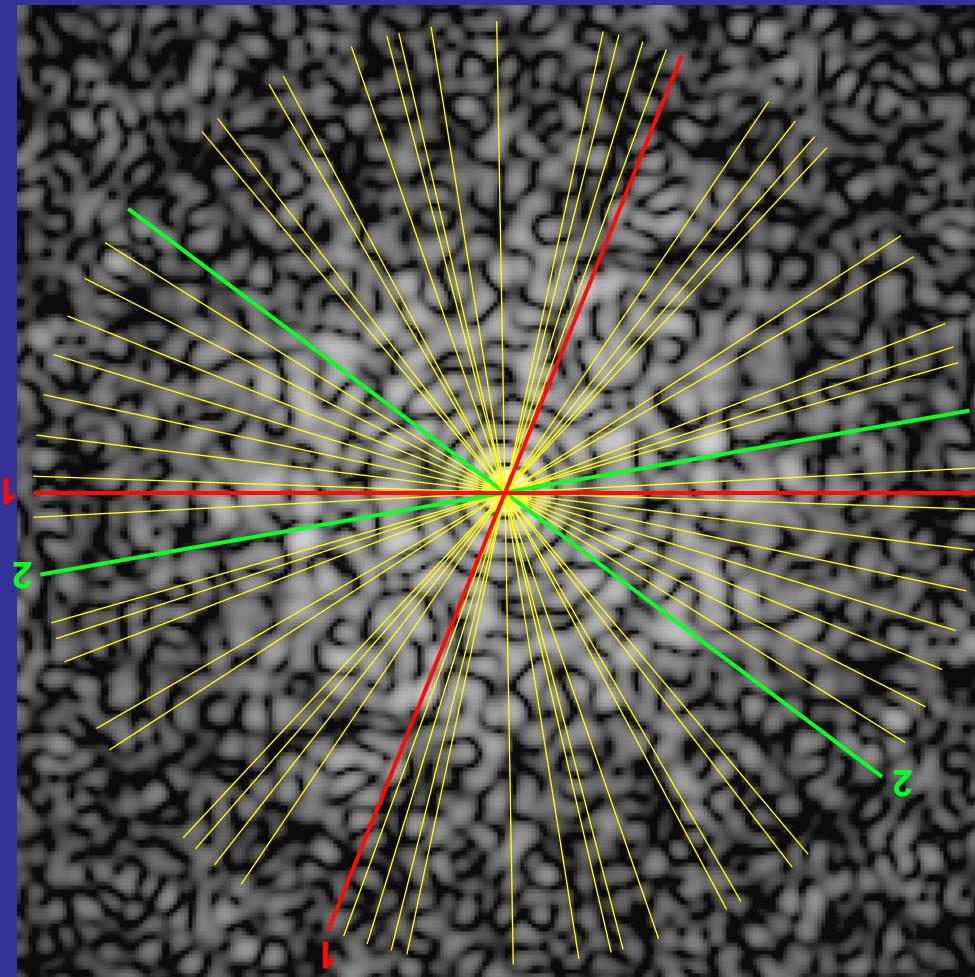
(80,11,180)

Orientation Determination by Common Lines



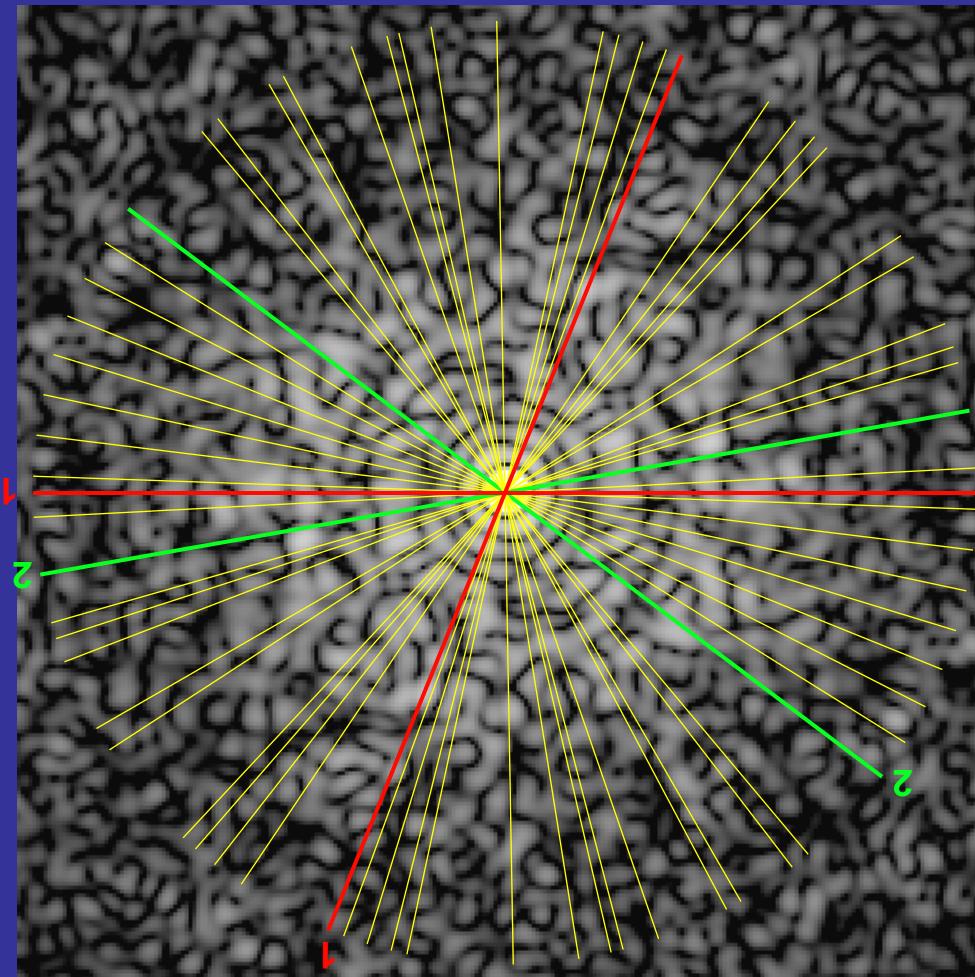
Metric: Identify ω that gives lowest phase residual

Orientation Determination by Common Lines



Repeat process for all possible (θ, ϕ, ω) combinations

Orientation Determination by Common Lines



> 250,000 combinations for 1° angular search intervals

Icosahedral Virus 3D Reconstruction Scheme

↓
Determine Origin and
Orientation ($\theta, \phi, \omega, x, y$)

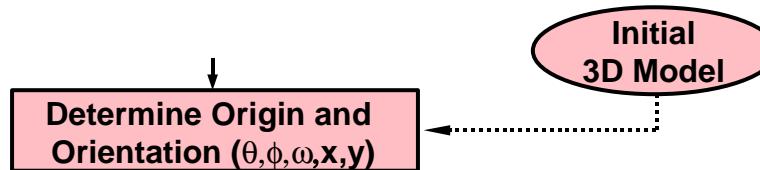
Common Lines

The (θ, ϕ, ω) that results in the lowest phase residual is selected as the best estimate for the particle view orientation

The ‘common lines’ procedure is similarly used to determine the particle phase origin (x, y)

Not to worry.....I'll spare you the details!!!

Icosahedral Virus 3D Reconstruction Scheme



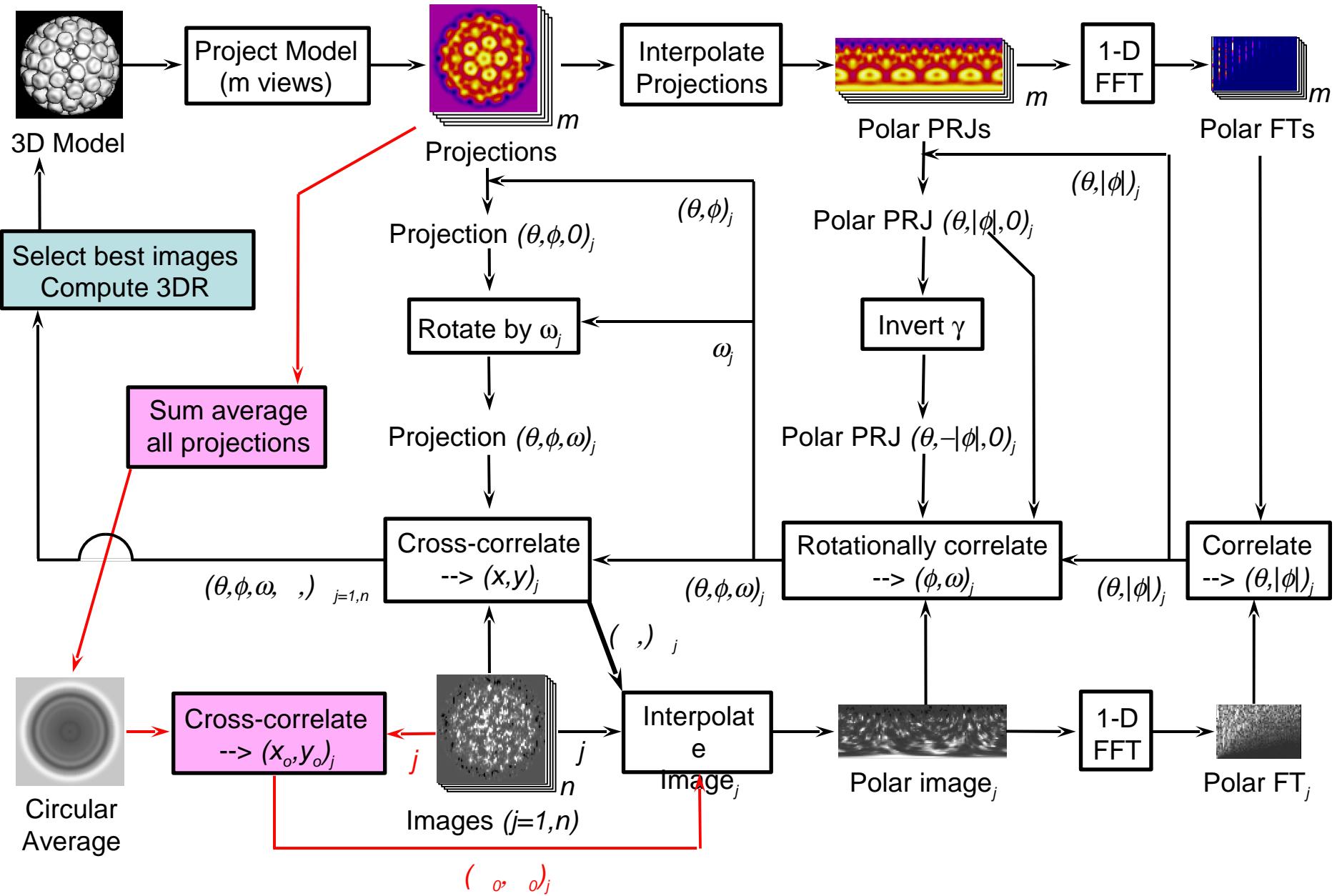
Recall: two methods to determine $(\theta, \phi, \omega, x, y)$:

1. Common lines
2. Model-based (template) matching

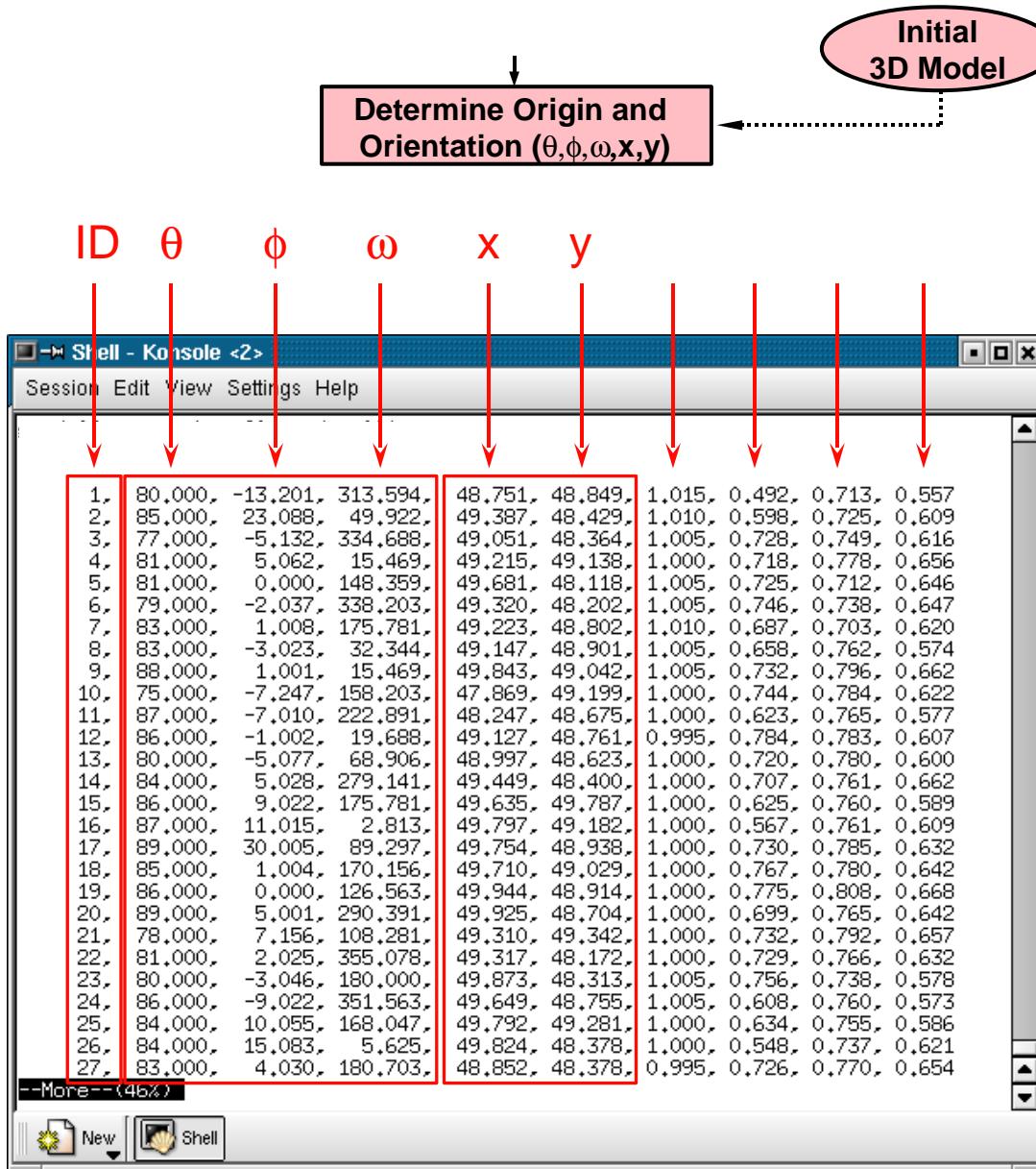
Bulk of structures now solved this way

Details discussed in practical session

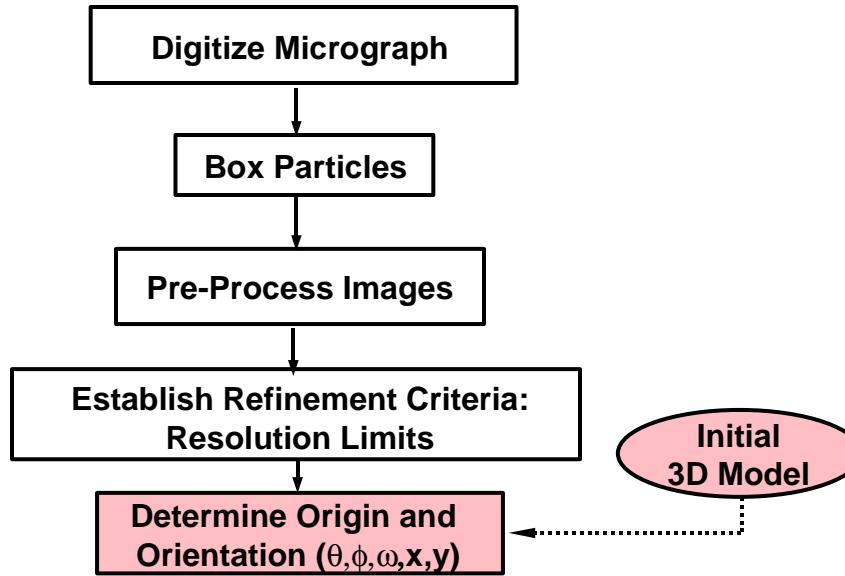
PFTSEARCH Program Flowchart



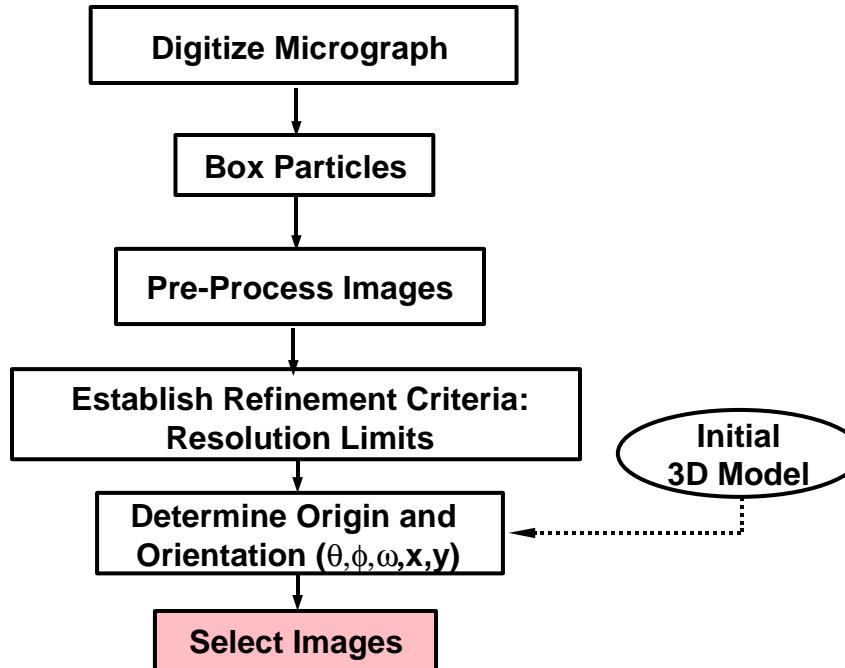
Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme

Select Images

Goal: weed out ‘bad’ particle images before computing 3D reconstruction

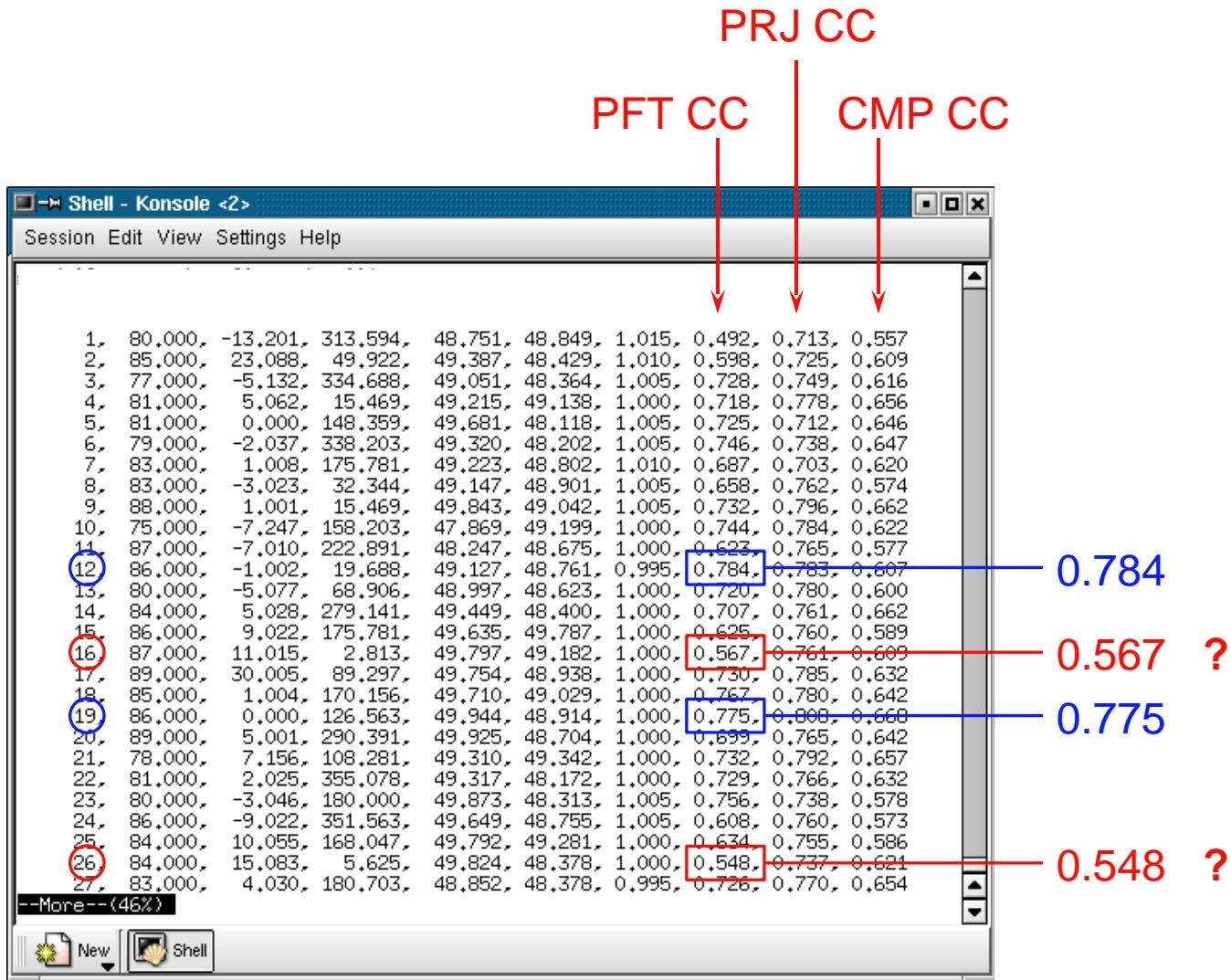
Icosahedral Virus 3D Reconstruction Scheme

Select Images

ID	θ	ϕ	ω	X	Y	
1,	80.000,	-13.201,	313.594,	48.751,	48.849,	1.015, 0.492, 0.713, 0.557
2,	85.000,	23.088,	49.922,	49.387,	48.429,	1.010, 0.598, 0.725, 0.609
3,	77.000,	-5.132,	334.688,	49.051,	48.364,	1.005, 0.728, 0.749, 0.616
4,	81.000,	5.062,	15.469,	49.215,	49.138,	1.000, 0.718, 0.778, 0.656
5,	81.000,	0.000,	148.359,	49.681,	48.118,	1.005, 0.725, 0.712, 0.646
6,	79.000,	-2.037,	338.203,	49.320,	48.202,	1.005, 0.746, 0.738, 0.647
7,	83.000,	1.008,	175.781,	49.223,	48.802,	1.010, 0.687, 0.703, 0.620
8,	83.000,	-3.023,	32.344,	49.147,	48.901,	1.005, 0.658, 0.762, 0.574
9,	88.000,	1.001,	15.469,	49.843,	49.042,	1.005, 0.732, 0.796, 0.662
10,	75.000,	-7.247,	158.203,	47.869,	49.199,	1.000, 0.744, 0.784, 0.622
11,	87.000,	-7.010,	222.891,	48.247,	48.675,	1.000, 0.623, 0.765, 0.577
12,	86.000,	-1.002,	19.688,	49.127,	48.761,	0.995, 0.784, 0.783, 0.607
13,	80.000,	-5.077,	68.906,	48.997,	48.623,	1.000, 0.720, 0.780, 0.600
14,	84.000,	5.028,	279.141,	49.449,	48.400,	1.000, 0.707, 0.761, 0.662
15,	86.000,	9.022,	175.781,	49.635,	49.787,	1.000, 0.625, 0.760, 0.589
16,	87.000,	11.015,	2.813,	49.797,	49.182,	1.000, 0.567, 0.761, 0.609
17,	89.000,	30.005,	89.297,	49.754,	48.938,	1.000, 0.730, 0.785, 0.632
18,	85.000,	1.004,	170.156,	49.710,	49.029,	1.000, 0.767, 0.780, 0.642
19,	86.000,	0.000,	126.563,	49.944,	48.914,	1.000, 0.775, 0.808, 0.668
20,	89.000,	5.001,	290.391,	49.925,	48.704,	1.000, 0.699, 0.765, 0.642
21,	78.000,	7.156,	108.281,	49.310,	49.342,	1.000, 0.732, 0.792, 0.657
22,	81.000,	2.025,	355.078,	49.317,	48.172,	1.000, 0.729, 0.766, 0.632
23,	80.000,	-3.046,	180.000,	49.873,	48.313,	1.005, 0.756, 0.738, 0.578
24,	86.000,	-9.022,	351.563,	49.649,	48.755,	1.005, 0.608, 0.760, 0.573
25,	84.000,	10.055,	168.047,	49.792,	49.281,	1.000, 0.634, 0.755, 0.586
26,	84.000,	15.083,	5.625,	49.824,	48.378,	1.000, 0.548, 0.737, 0.621
27,	83.000,	4.030,	180.703,	48.852,	48.378,	0.995, 0.726, 0.770, 0.654

Icosahedral Virus 3D Reconstruction Scheme

Select Images



Icosahedral Virus 3D Reconstruction Scheme

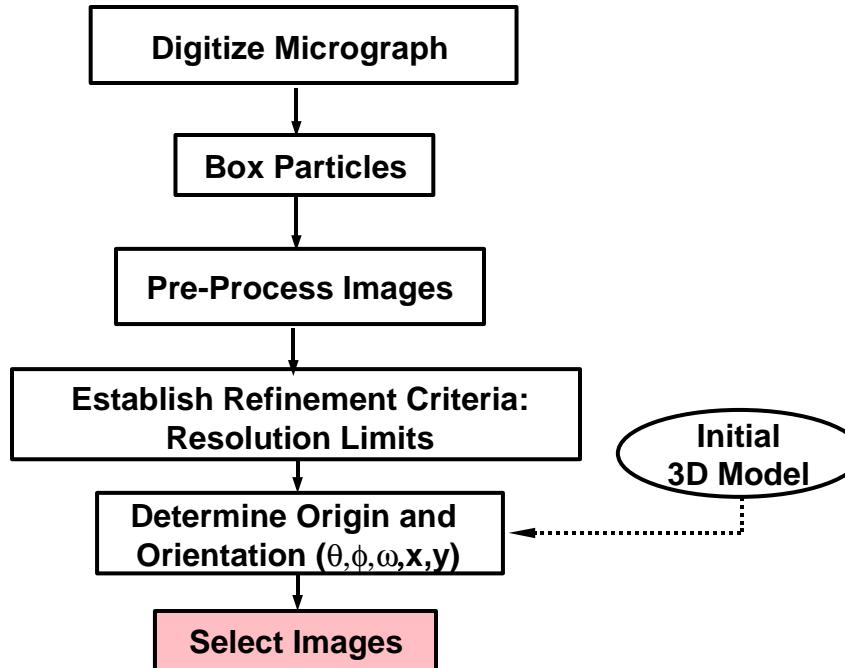
Select Images

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Session Edit View Settings Help
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1, 80.000, -13.201, 313.594, 48.751, 48.849, 1.015, 0.492, 0.713, 0.557
2, 85.000, 23.088, 49.922, 49.387, 48.429, 1.010, 0.598, 0.725, 0.609
3, 77.000, -5.132, 334.688, 49.051, 48.364, 1.005, 0.728, 0.749, 0.616
4, 81.000, 5.062, 15.469, 49.215, 49.138, 1.000, 0.718, 0.778, 0.656
5, 81.000, 0.000, 148.359, 49.681, 48.118, 1.005, 0.725, 0.712, 0.646
6, 79.000, -2.037, 338.203, 49.320, 48.202, 1.005, 0.746, 0.738, 0.647
7, 83.000, 1.008, 175.781, 49.223, 48.802, 1.010, 0.687, 0.703, 0.620
8, 83.000, -3.023, 32.344, 49.147, 48.901, 1.005, 0.658, 0.762, 0.574
9, 88.000, 1.001, 15.469, 49.843, 49.042, 1.005, 0.732, 0.796, 0.662
10, 75.000, -7.247, 158.203, 47.869, 49.199, 1.000, 0.744, 0.784, 0.622
11, 87.000, -7.010, 222.891, 48.247, 48.675, 1.000, 0.623, 0.765, 0.577
12, 86.000, -1.002, 19.688, 49.127, 48.761, 0.995, 0.784, 0.783, 0.607
13, 80.000, -5.077, 68.906, 48.997, 48.623, 1.000, 0.720, 0.780, 0.600
14, 84.000, 5.028, 279.141, 49.449, 48.400, 1.000, 0.707, 0.761, 0.662
15, 86.000, 9.022, 175.781, 49.635, 49.787, 1.000, 0.625, 0.760, 0.589
16, 87.000, 11.015, 2.813, 49.797, 49.182, 1.000, 0.567, 0.761, 0.609
17, 89.000, 30.005, 89.297, 49.754, 48.938, 1.000, 0.730, 0.785, 0.632
18, 85.000, 1.004, 170.156, 49.710, 49.029, 1.000, 0.767, 0.780, 0.642
19, 86.000, 0.000, 126.563, 49.944, 48.914, 1.000, 0.775, 0.808, 0.668
20, 89.000, 5.001, 290.391, 49.925, 48.704, 1.000, 0.699, 0.765, 0.642
21, 78.000, 7.156, 108.281, 49.310, 49.342, 1.000, 0.732, 0.792, 0.657
22, 81.000, 2.025, 355.078, 49.317, 48.172, 1.000, 0.729, 0.766, 0.632
23, 80.000, -3.046, 180.000, 49.873, 48.313, 1.005, 0.756, 0.738, 0.578
24, 86.000, -9.022, 351.563, 49.649, 48.755, 1.005, 0.608, 0.760, 0.573
25, 84.000, 10.055, 168.047, 49.792, 49.281, 1.000, 0.634, 0.755, 0.586
26, 84.000, 15.083, 5.625, 49.824, 48.378, 1.000, 0.548, 0.737, 0.621
27, 83.000, 4.030, 180.703, 48.852, 48.378, 0.995, 0.726, 0.770, 0.654
--More--(46%)
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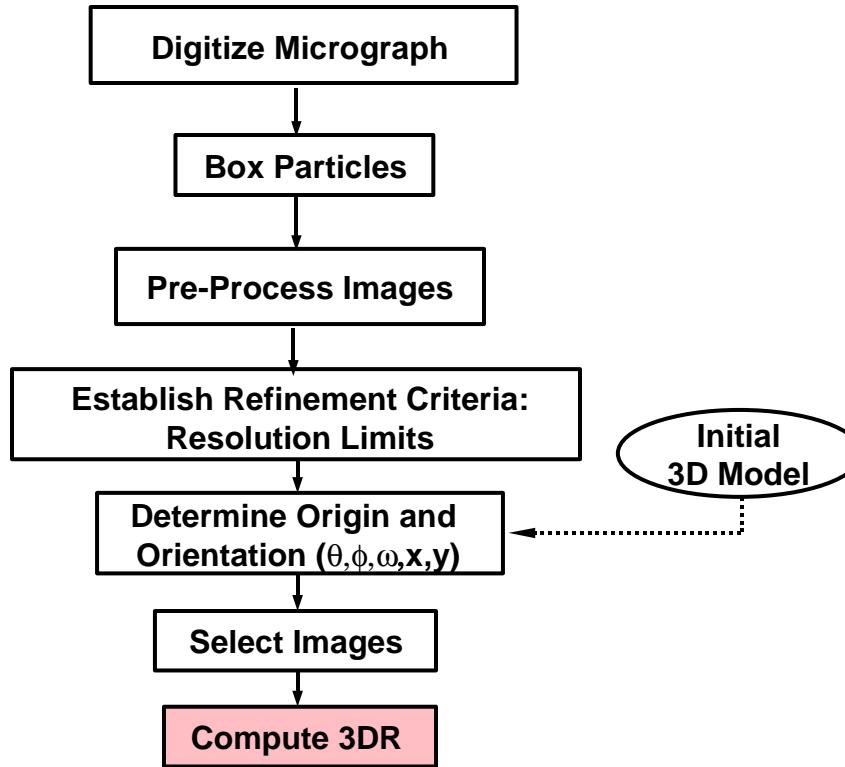
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Session Edit View Settings Help
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44, 80.000, 7.108, 239.063, 48.996, 49.075, 0.995, 0.690, 0.761, 0.623
45, 74.000, 1.040, 142.734, 49.824, 48.960, 0.990, 0.685, 0.718, 0.637
46, 81.000, 13.162, 242.578, 49.019, 49.032, 1.000, 0.533, 0.758, 0.558
47, 73.000, -1.046, 173.672, 48.797, 47.683, 1.000, 0.687, 0.744, 0.569
48, 71.000, -3.173, 296.016, 50.072, 48.370, 1.000, 0.717, 0.788, 0.614
49, 82.000, -6.059, 199.688, 49.642, 49.156, 1.000, 0.719, 0.764, 0.633
50, 73.000, 2.091, 170.859, 49.110, 48.884, 1.000, 0.681, 0.741, 0.589
51, 84.000, 20.110, 215.156, 49.076, 48.673, 1.000, 0.576, 0.764, 0.608
52, 79.000, 14.262, 21.094, 49.088, 49.107, 1.005, 0.536, 0.745, 0.560
53, 89.000, -5.001, 187.031, 48.970, 49.204, 1.005, 0.602, 0.744, 0.551
54, 79.000, 6.112, 227.109, 49.223, 48.719, 1.000, 0.721, 0.755, 0.636
55, 88.000, 21.013, 162.422, 48.765, 49.285, 0.995, 0.557, 0.749, 0.580
56, 84.000, -3.017, 251.016, 49.831, 50.002, 0.995, 0.745, 0.776, 0.616
57, 80.000, -2.031, 213.047, 47.831, 48.686, 0.995, 0.722, 0.744, 0.590
58, 72.000, -3.154, 295.313, 48.862, 47.839, 0.995, 0.680, 0.741, 0.546
59, 83.000, -1.008, 102.656, 48.957, 48.904, 1.005, 0.713, 0.767, 0.575
60, 89.000, -6.001, 73.828, 48.802, 48.736, 1.010, 0.680, 0.693, 0.544
=====
Compute average MAG factor and coefficients. N = 120
=====
Average Std. Dev.
MAG Factor 1.000 0.005
PFT Coefficient 0.679 0.075
PRJ Coefficient 0.756 0.023
CMP Coefficient 0.609 0.038
PFT finished.
*****
gandalf #
```

PFT Coefficient 0.679 ± 0.075

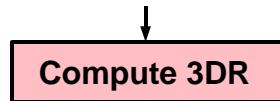
Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme



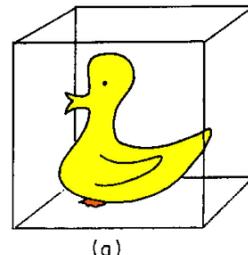
Icosahedral Virus 3D Reconstruction Scheme



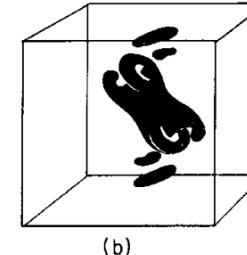
Goal: combine only “good” particle images
to compute a 3D density map

Icosahedral Virus 3D Reconstruction Scheme

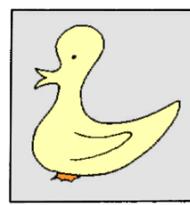
In theory



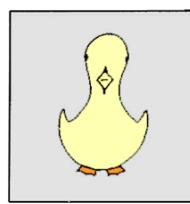
Three dimensional Fourier transform
↔
Inverse three dimensional Fourier transform



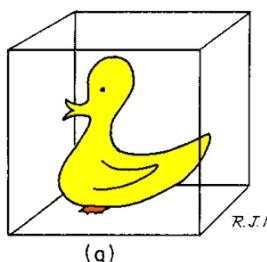
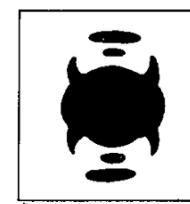
In practice



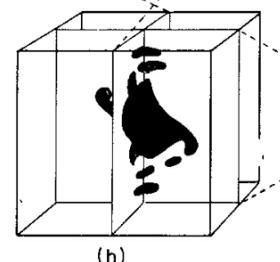
Two dimensional Fourier transform



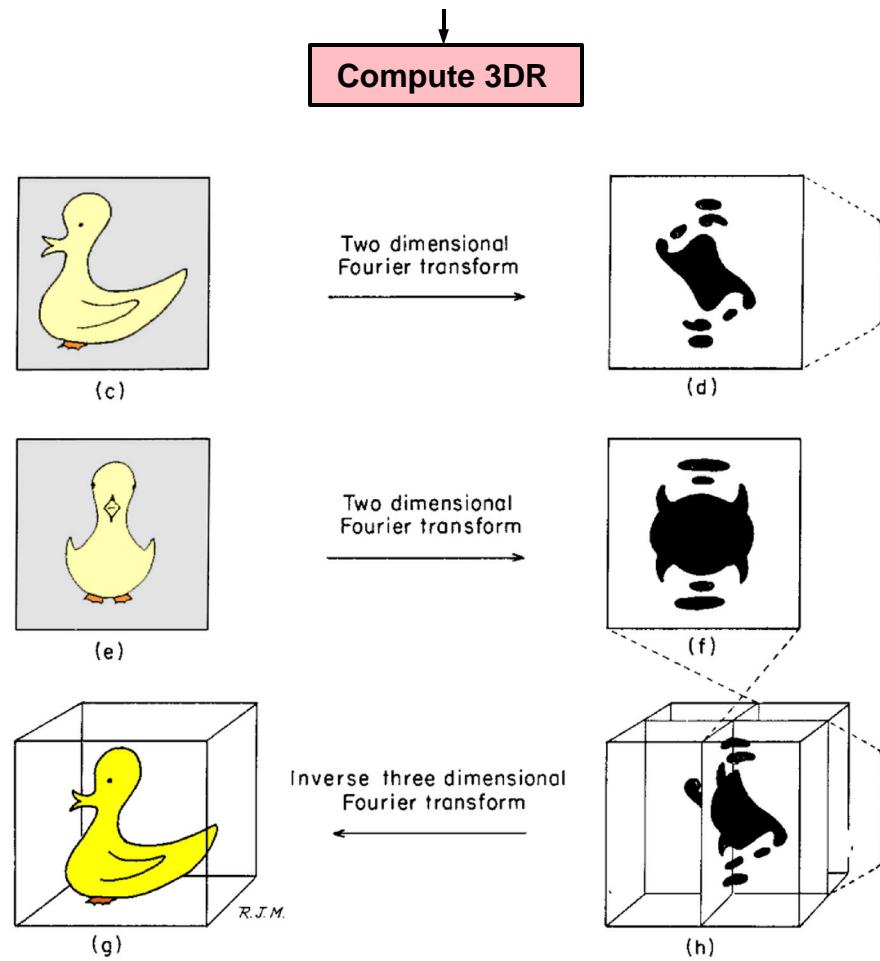
Two dimensional Fourier transform



Inverse three dimensional Fourier transform



Icosahedral Virus 3D Reconstruction Scheme



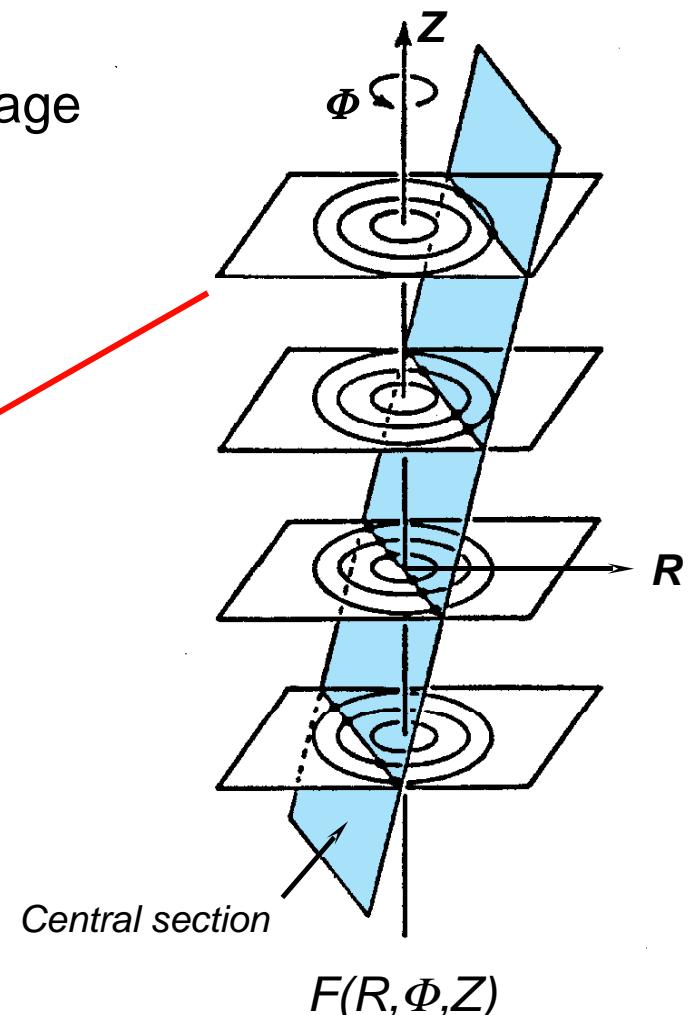
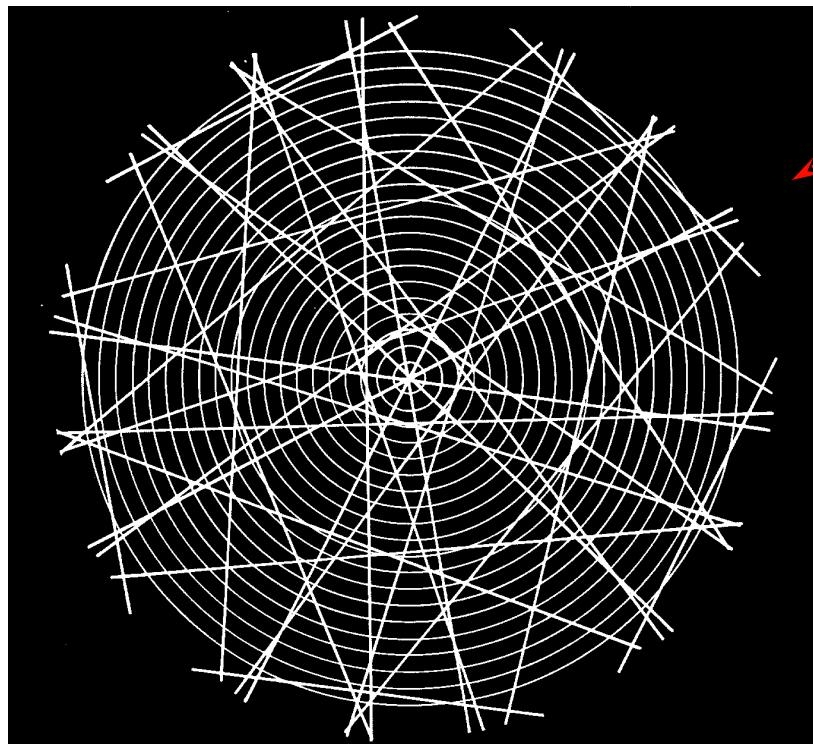
Overall scheme: $\rho \leftarrow g \leftarrow G \leftarrow F$

Icosahedral Virus 3D Reconstruction Scheme

Compute 3DR

Steps:

1. Compute 2D FFT of each particle image
2. Combine all 2D FFTs to build up 3D Fourier-Bessel transform



Icosahedral Virus 3D Reconstruction Scheme

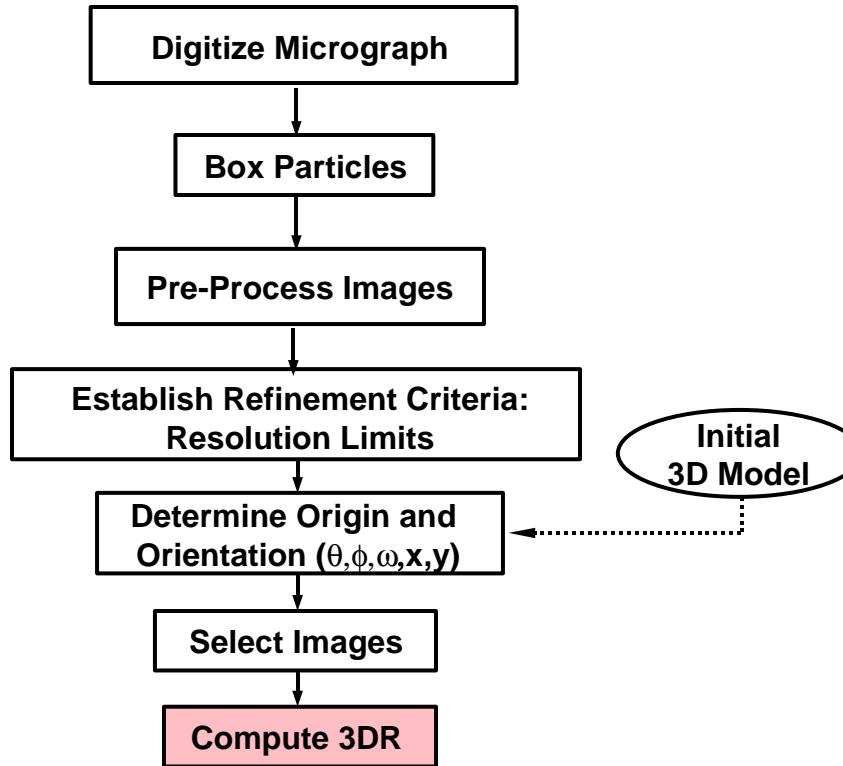
↓
Compute 3DR

$\rho \leftarrow g \leftarrow G \leftarrow F$

Steps:

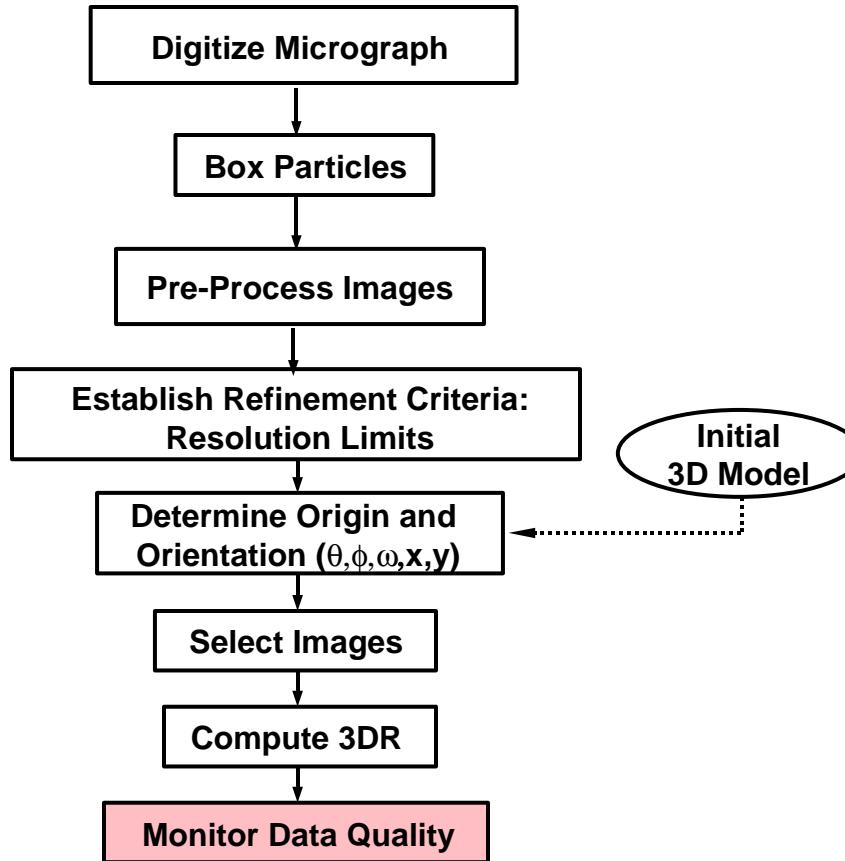
1. Compute 2D FFT of each particle image
2. Combine all 2D FFTs to build up 3D Fourier-Bessel transform
3. Compute G_n 's on each annulus $G = (B B)^{-1} B F$
4. Compute g_n 's from G_n 's (Fourier-Bessel transform)
5. Compute polar density map ($\rho(r,\phi,z)$) from g_n 's
6. Convert from polar to Cartesian map ($\rho(r,\phi,z) \rightarrow \rho(x,y,z)$)

Icosahedral Virus 3D Reconstruction Scheme

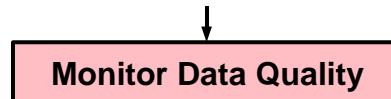


Option: correct for CTF effects in particle FFTs before FFTs are merged to form the 3D FFT

Icosahedral Virus 3D Reconstruction Scheme

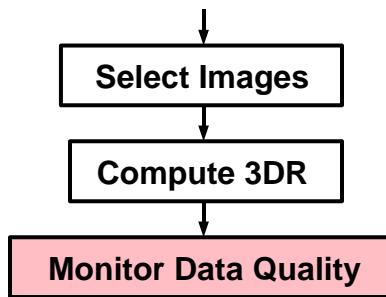


Icosahedral Virus 3D Reconstruction Scheme

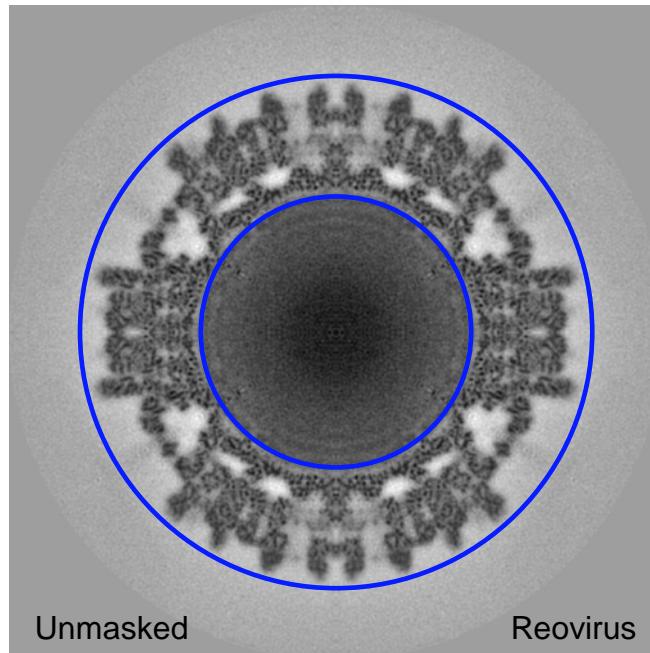
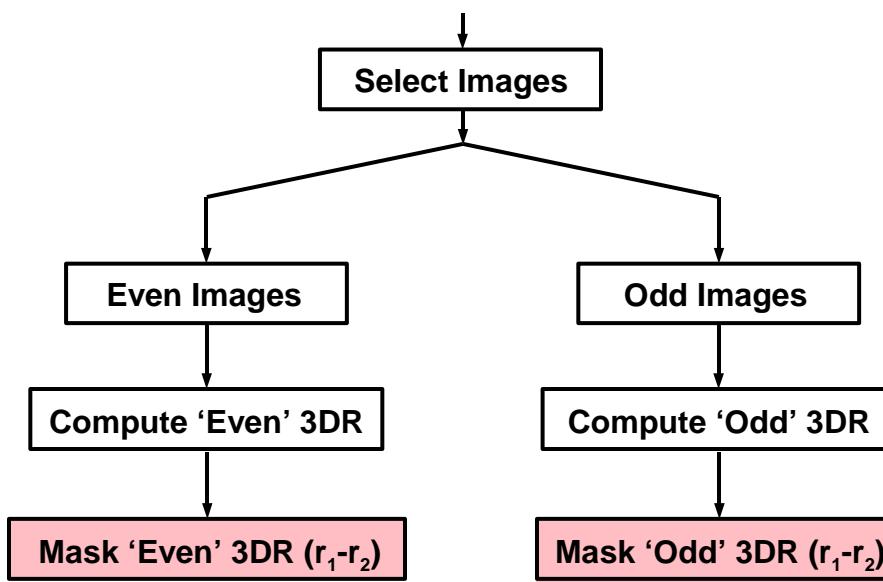


Goal: assess resolution of 3D density map
to determine what to do next

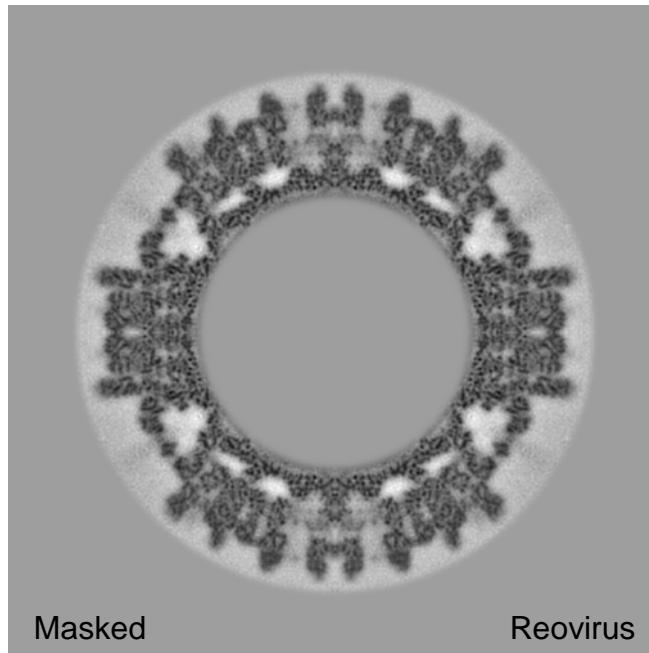
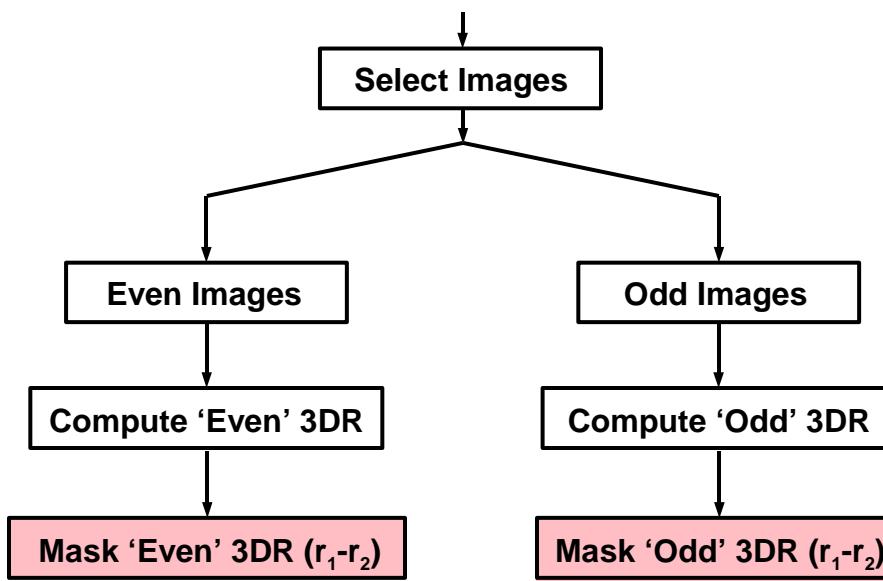
Icosahedral Virus 3D Reconstruction Scheme



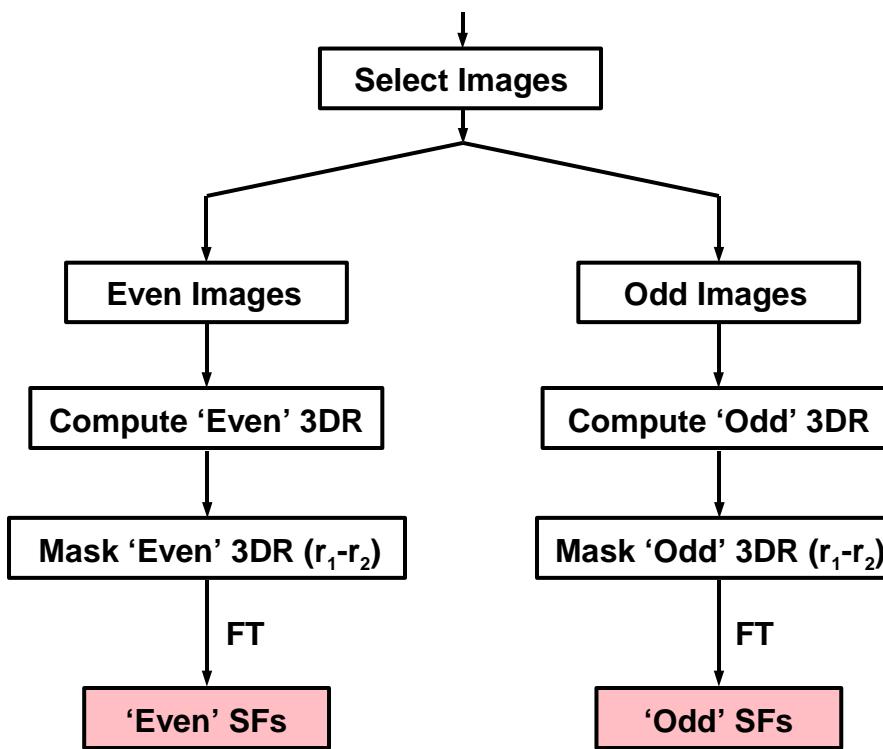
Icosahedral Virus 3D Reconstruction Scheme



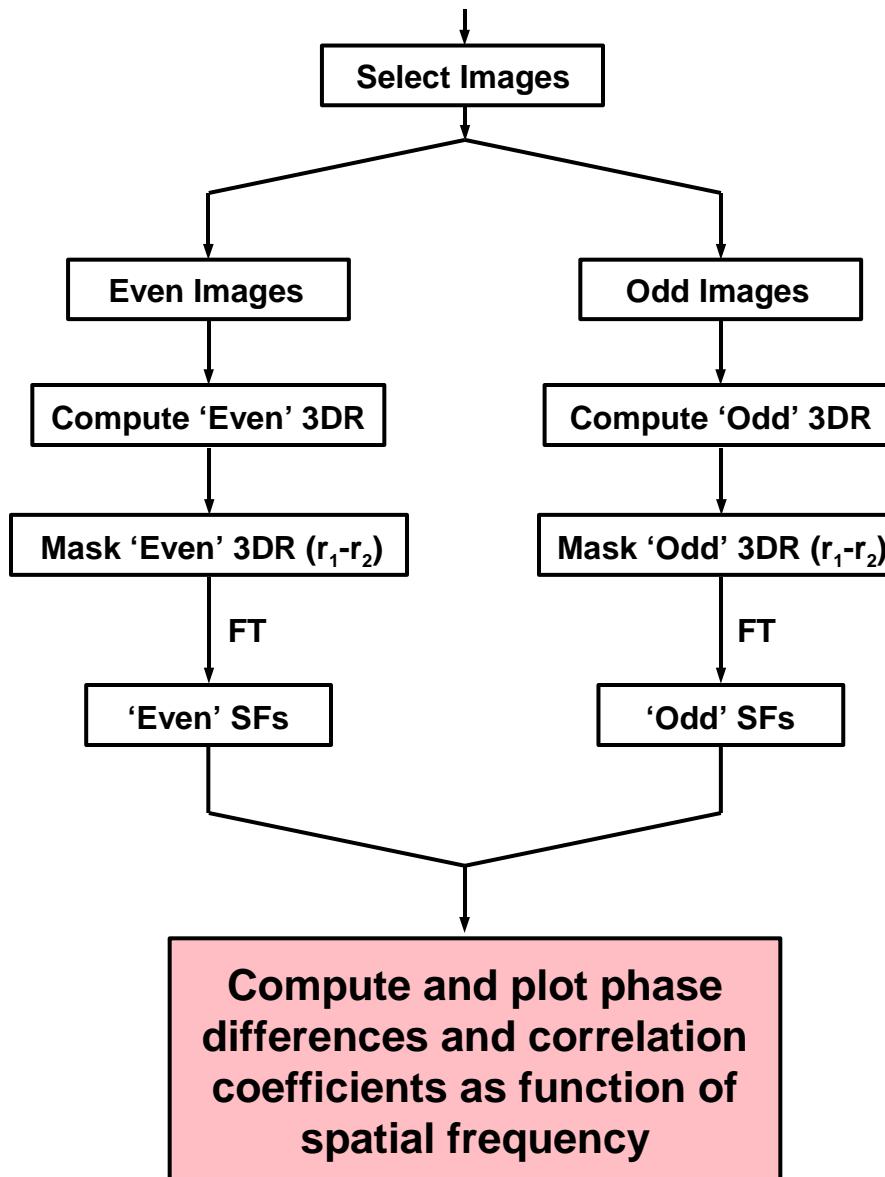
Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme

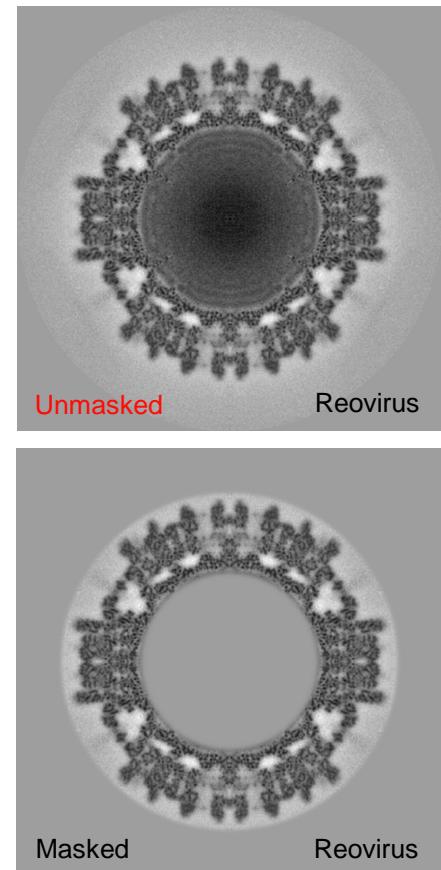
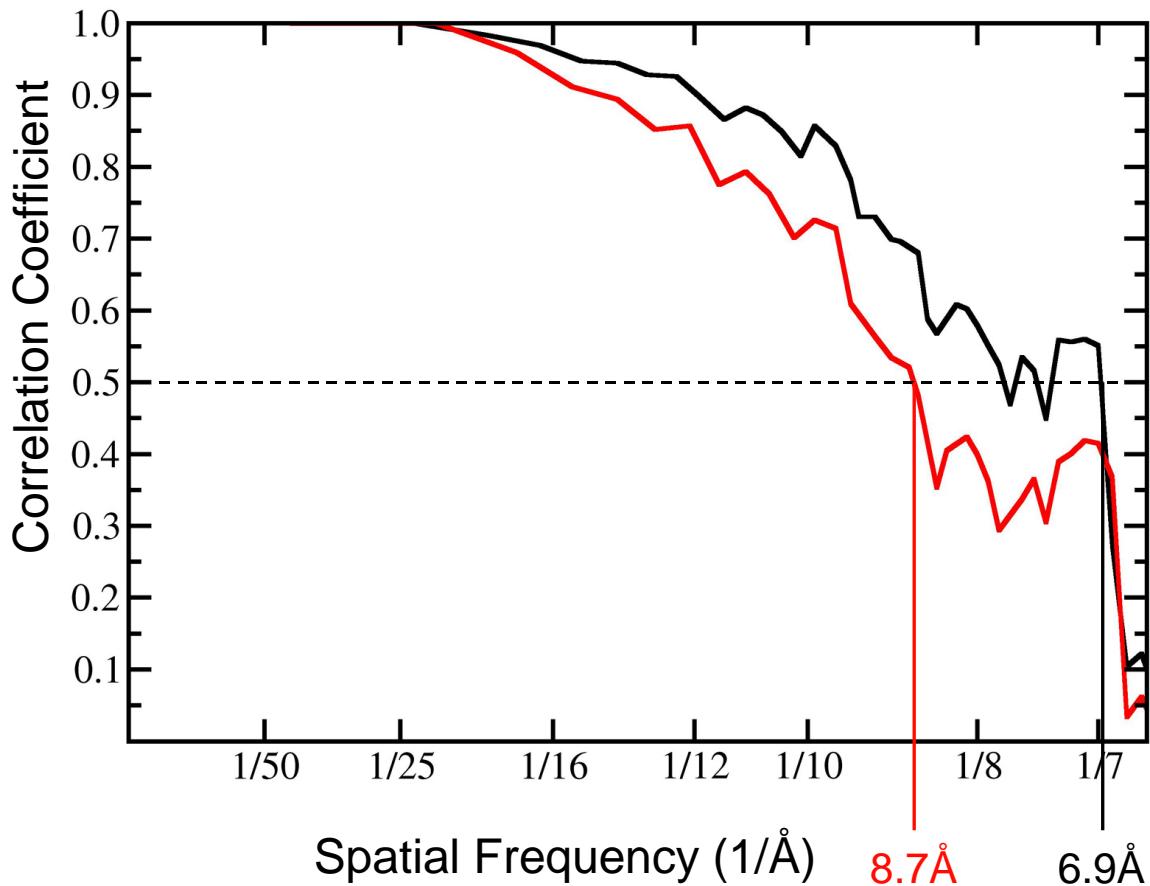


Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme

↓
Monitor Data Quality



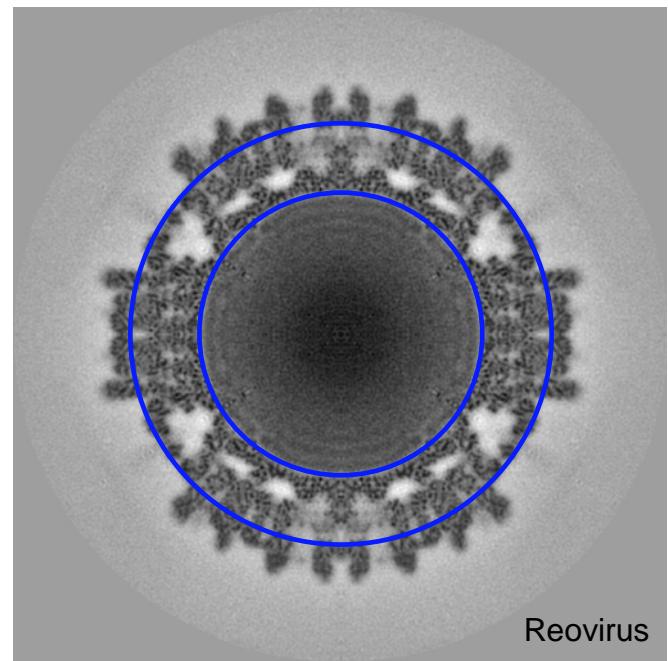
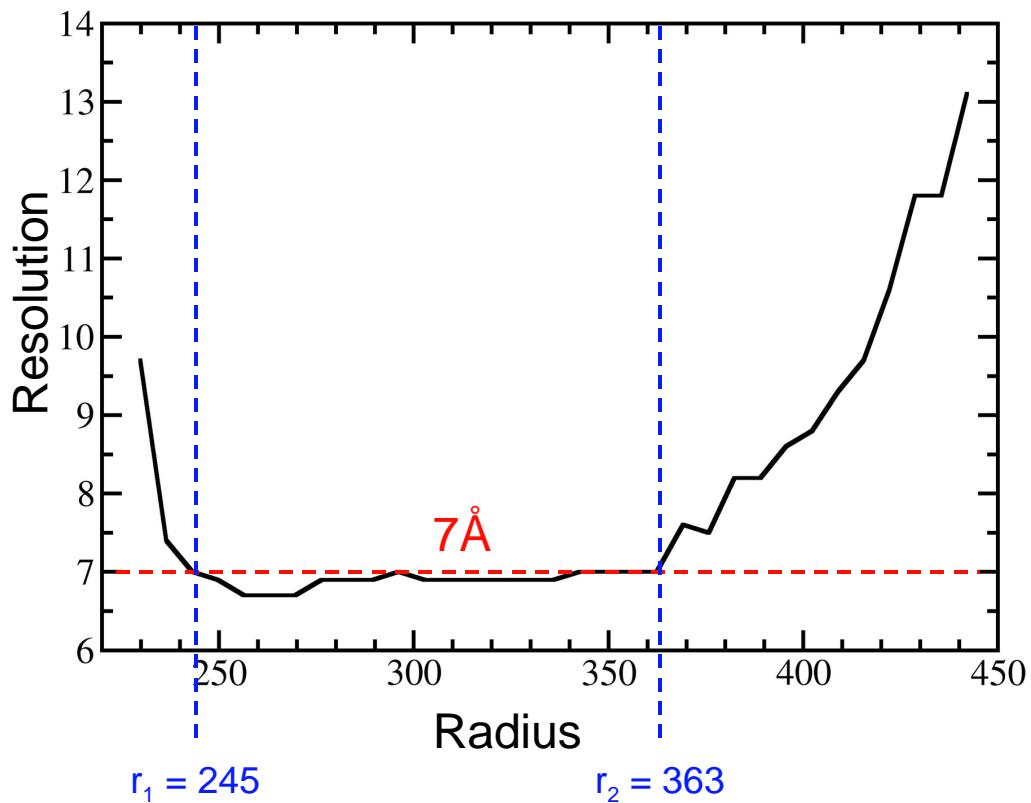
Icosahedral Virus 3D Reconstruction Scheme

↓
Monitor Data Quality

Note: quality of 3D density map is not identical
everywhere in the map

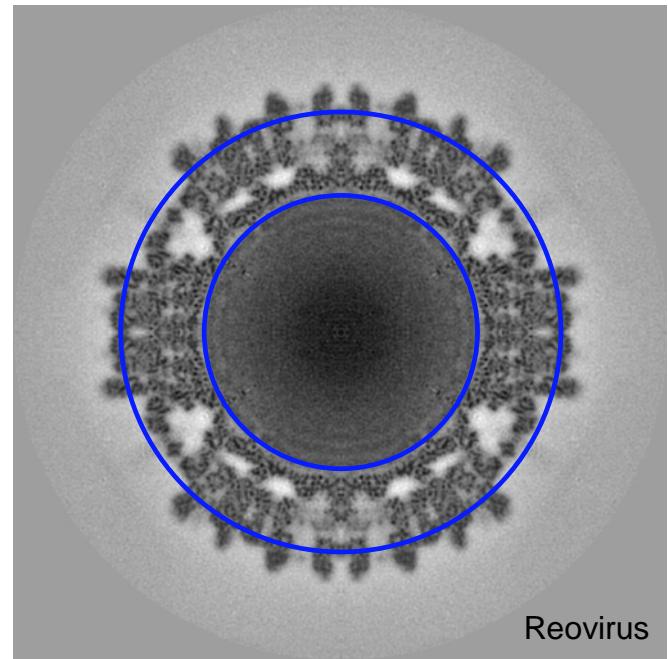
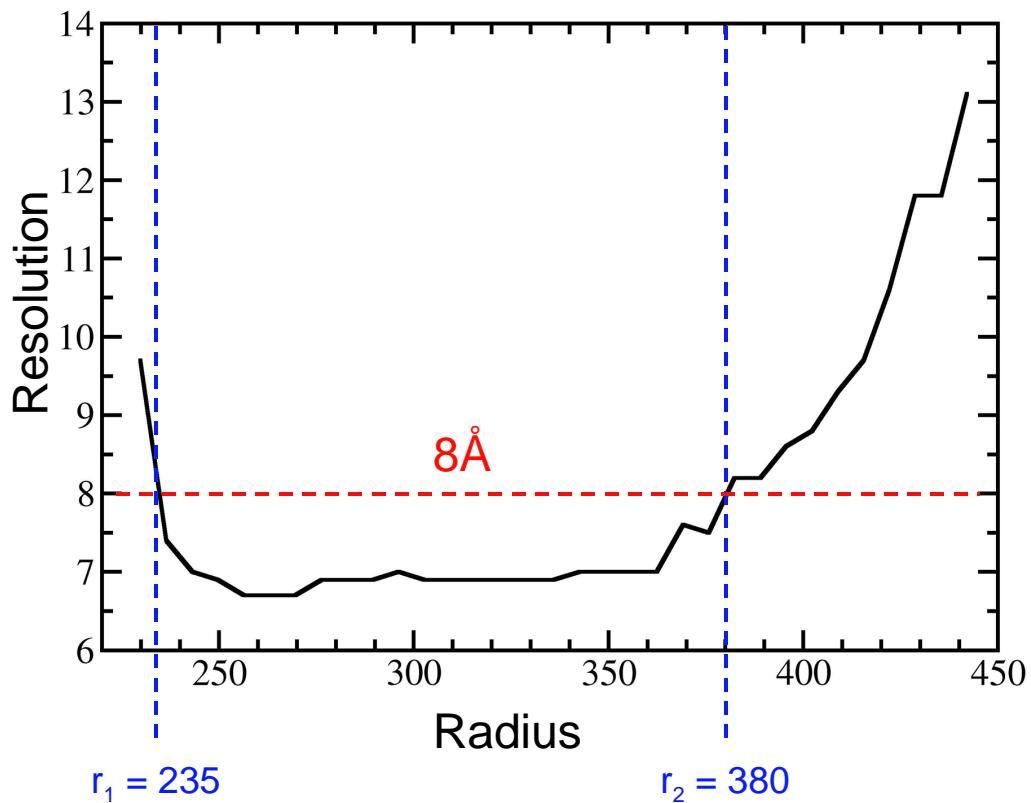
Icosahedral Virus 3D Reconstruction Scheme

Monitor Data Quality



Icosahedral Virus 3D Reconstruction Scheme

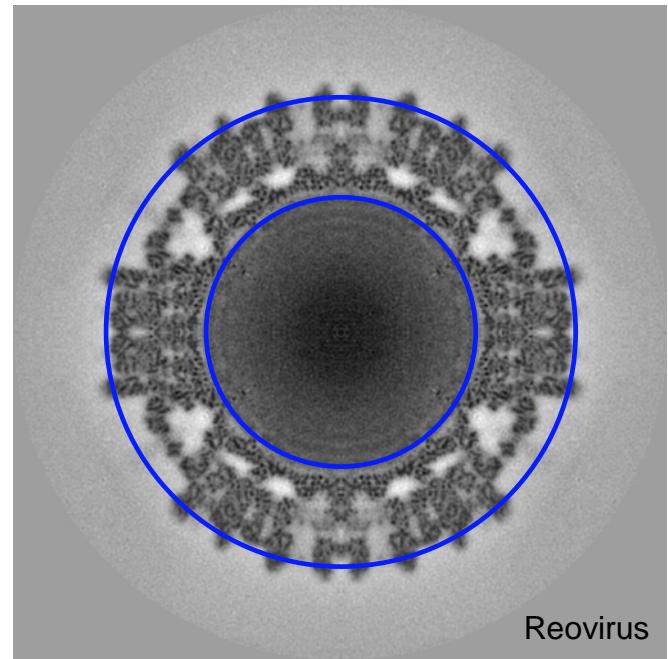
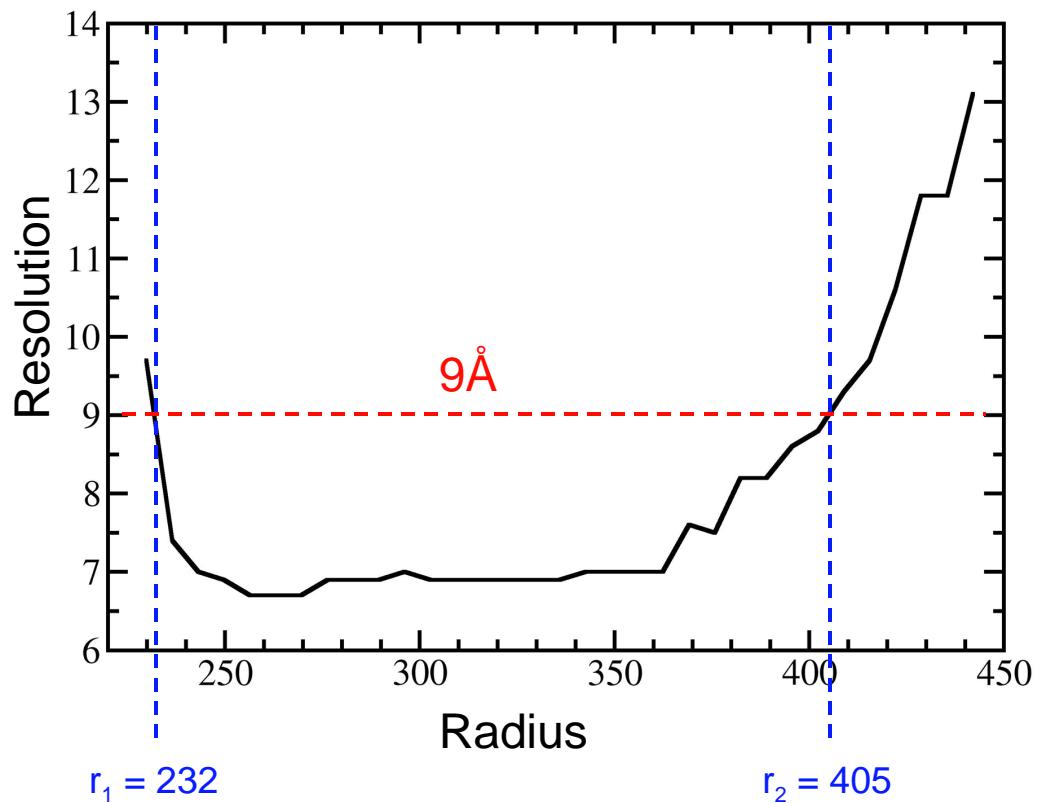
Monitor Data Quality



Reovirus

Icosahedral Virus 3D Reconstruction Scheme

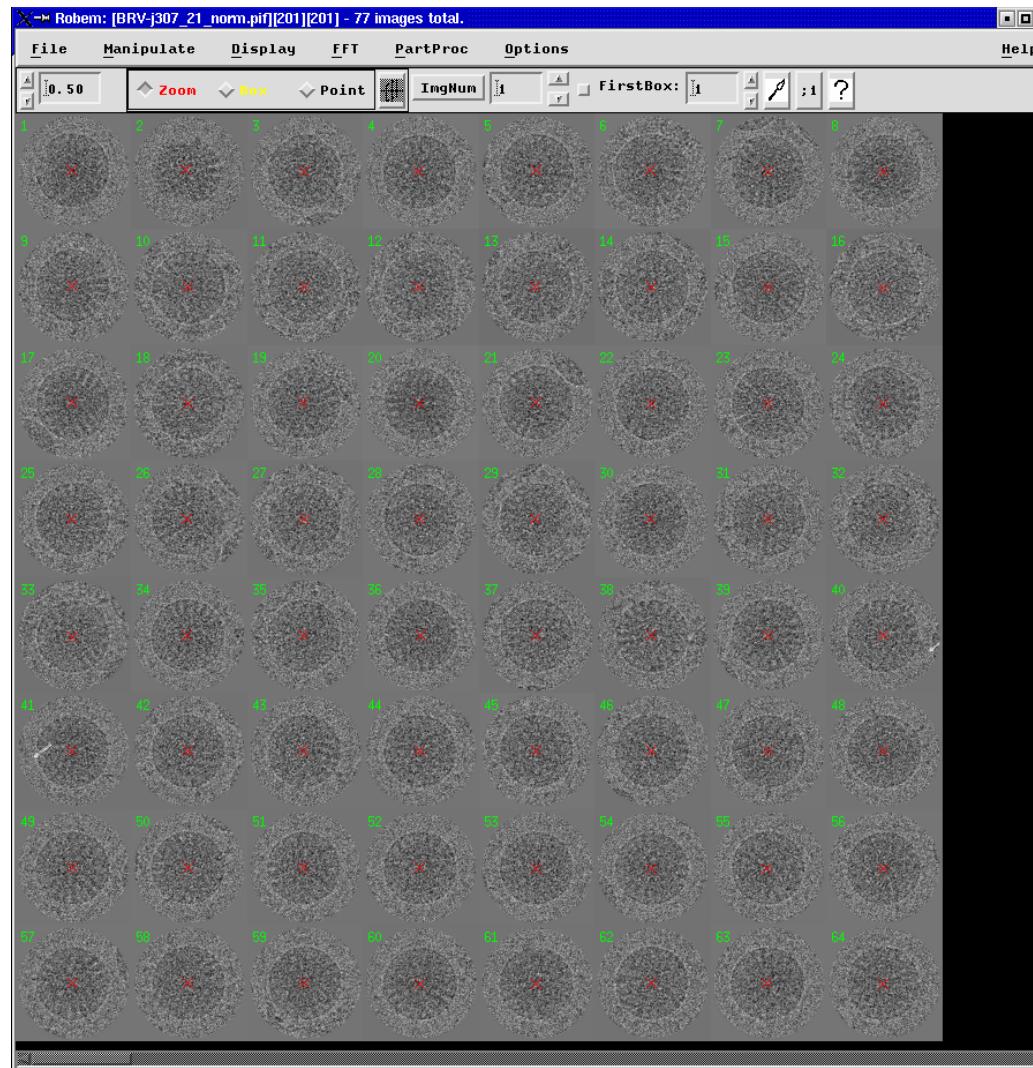
Monitor Data Quality



Icosahedral Virus 3D Reconstruction Scheme



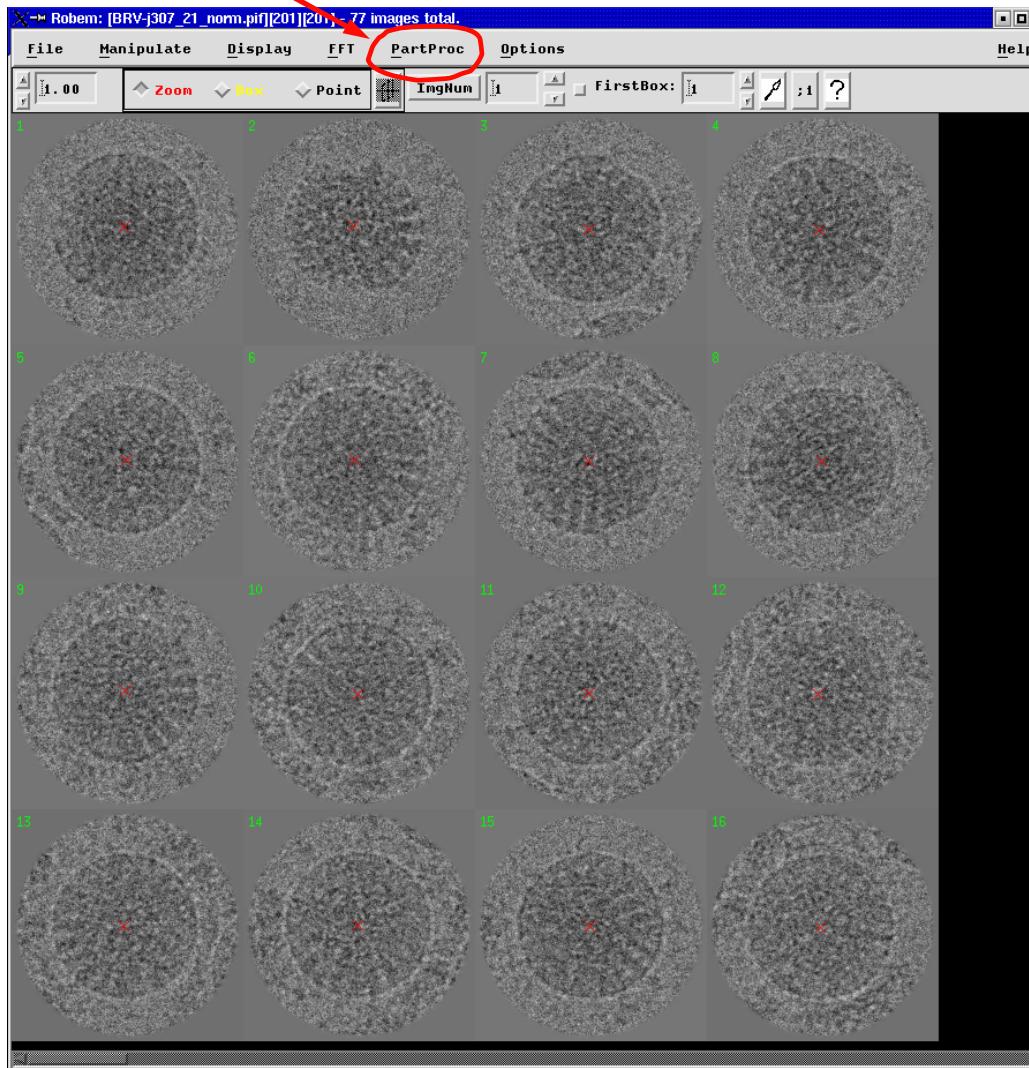
Monitor Data Quality



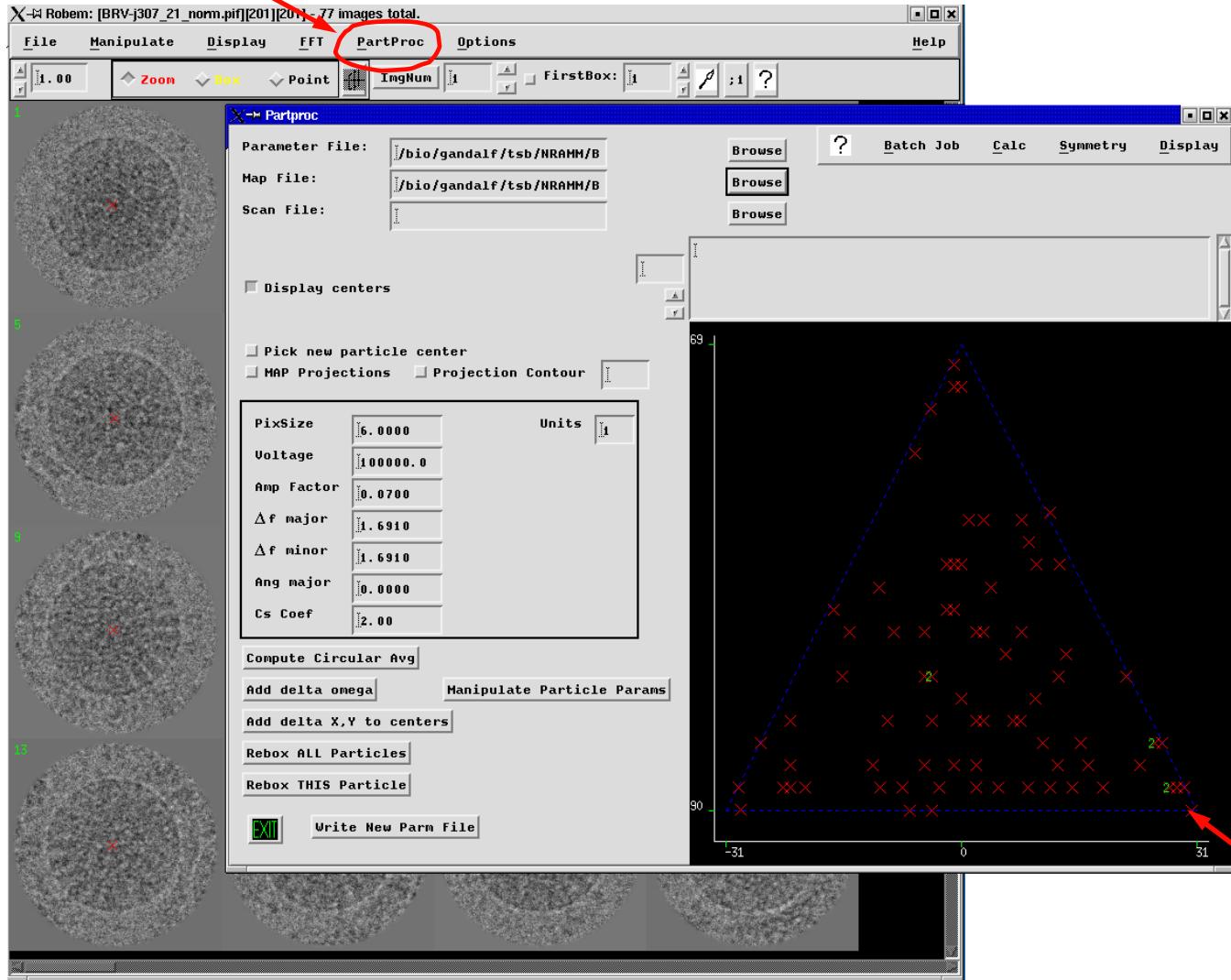
Icosahedral Virus 3D Reconstruction Scheme



Monitor Data Quality



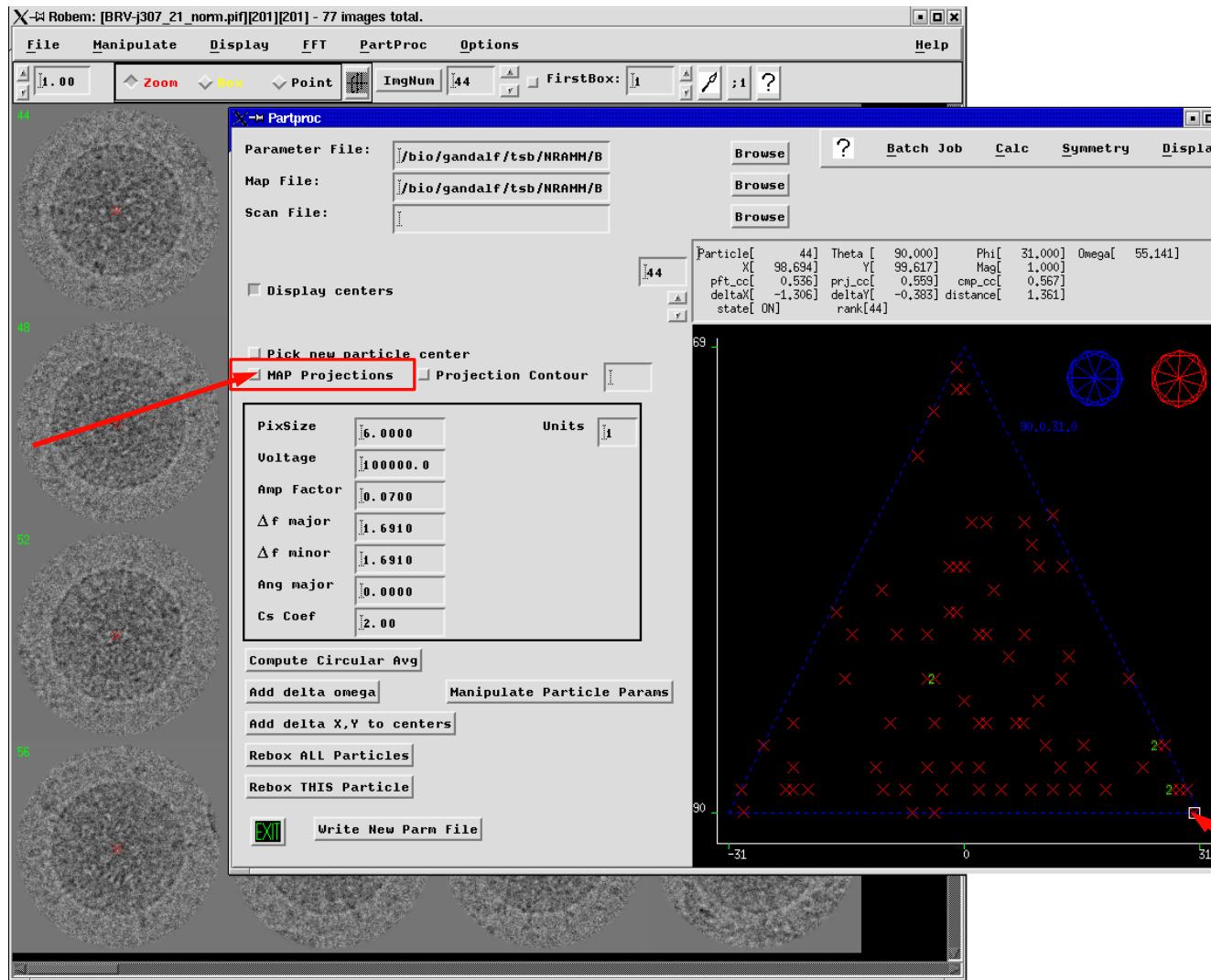
Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme



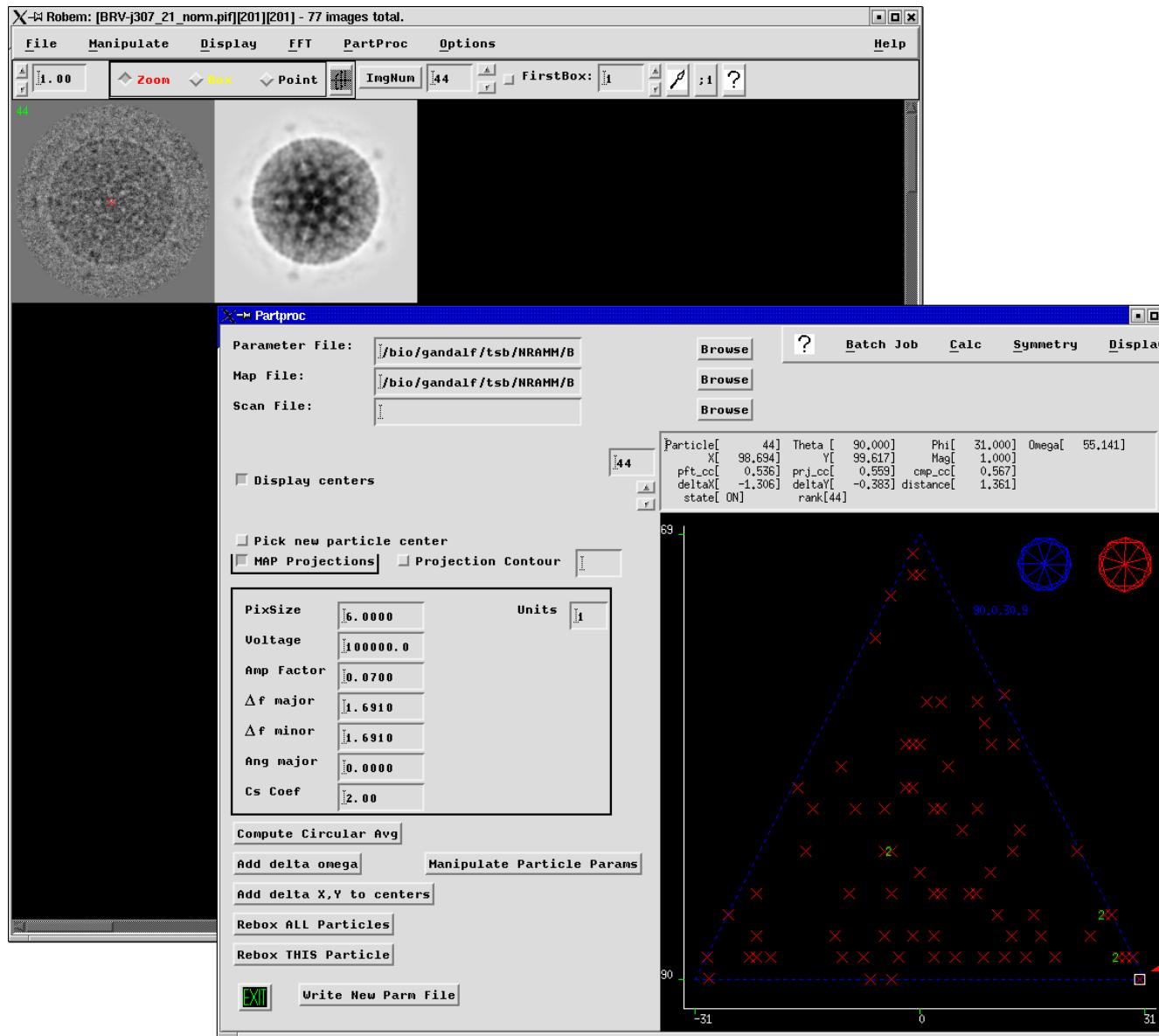
Monitor Data Quality



Icosahedral Virus 3D Reconstruction Scheme



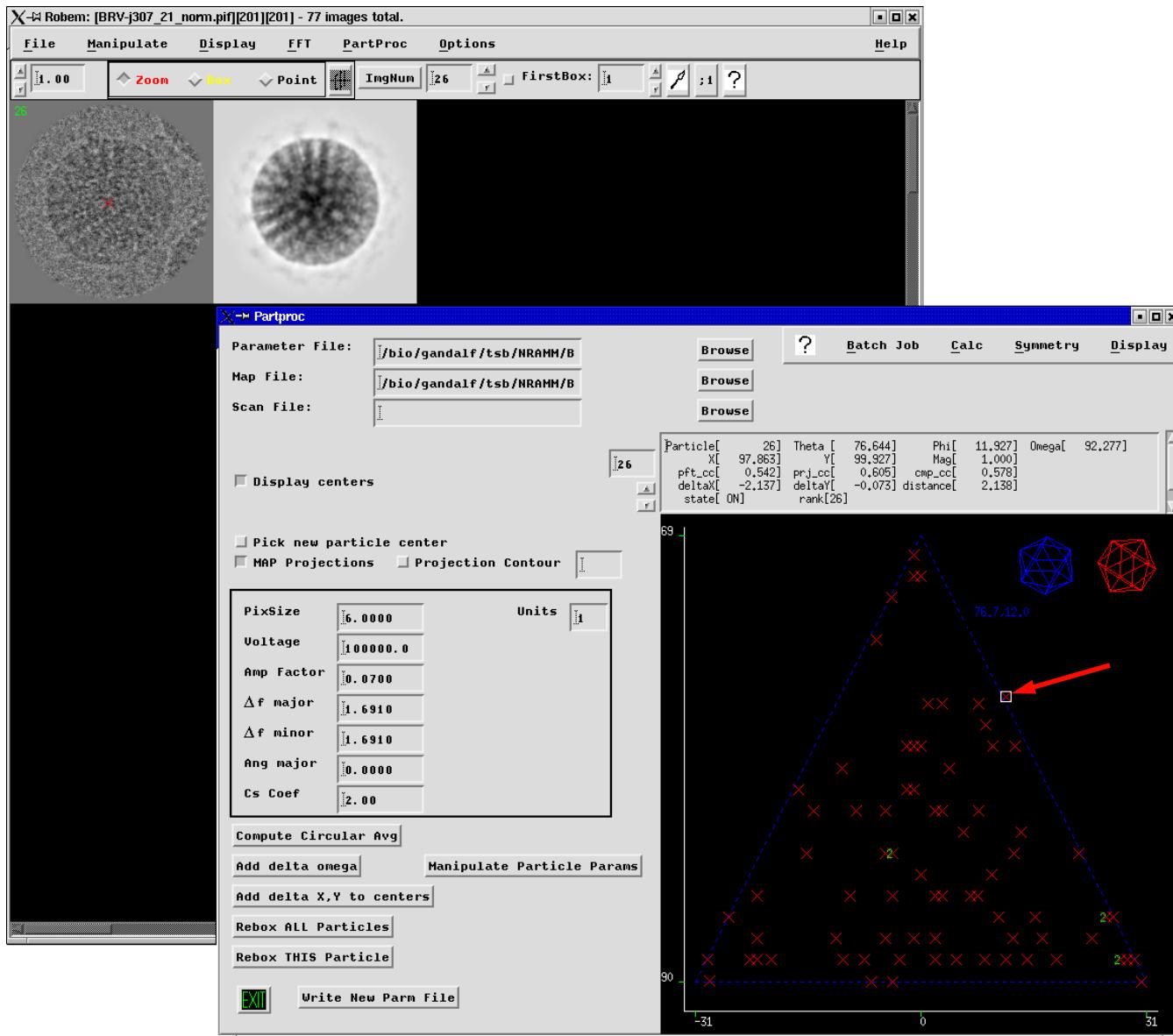
Monitor Data Quality



Icosahedral Virus 3D Reconstruction Scheme



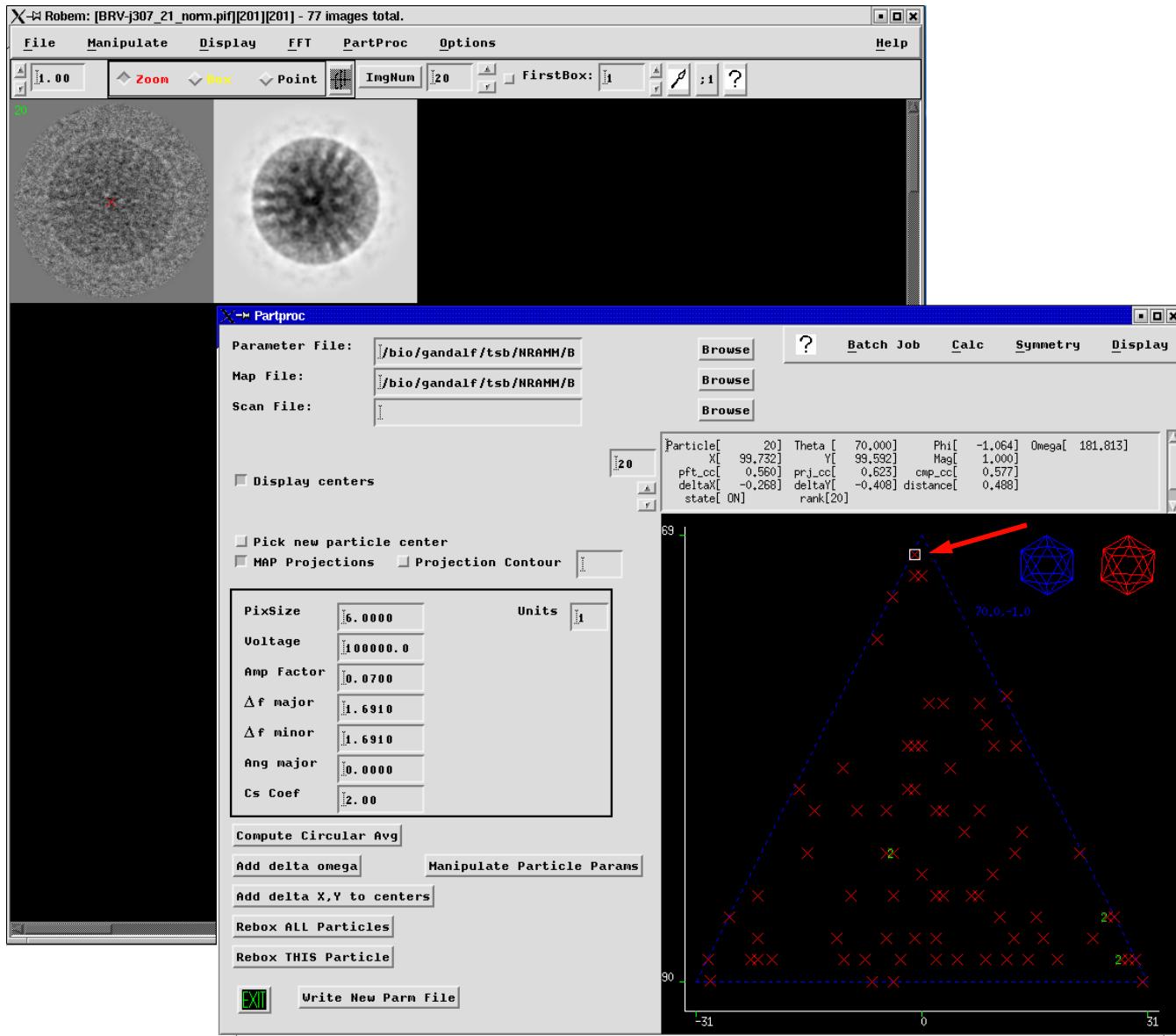
Monitor Data Quality



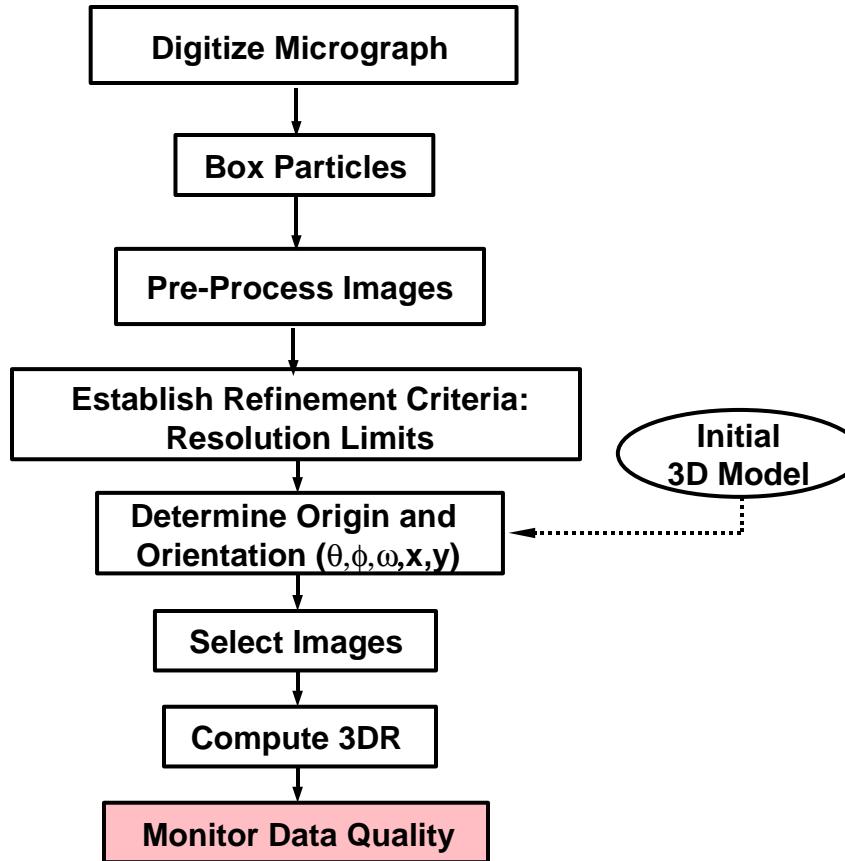
Icosahedral Virus 3D Reconstruction Scheme



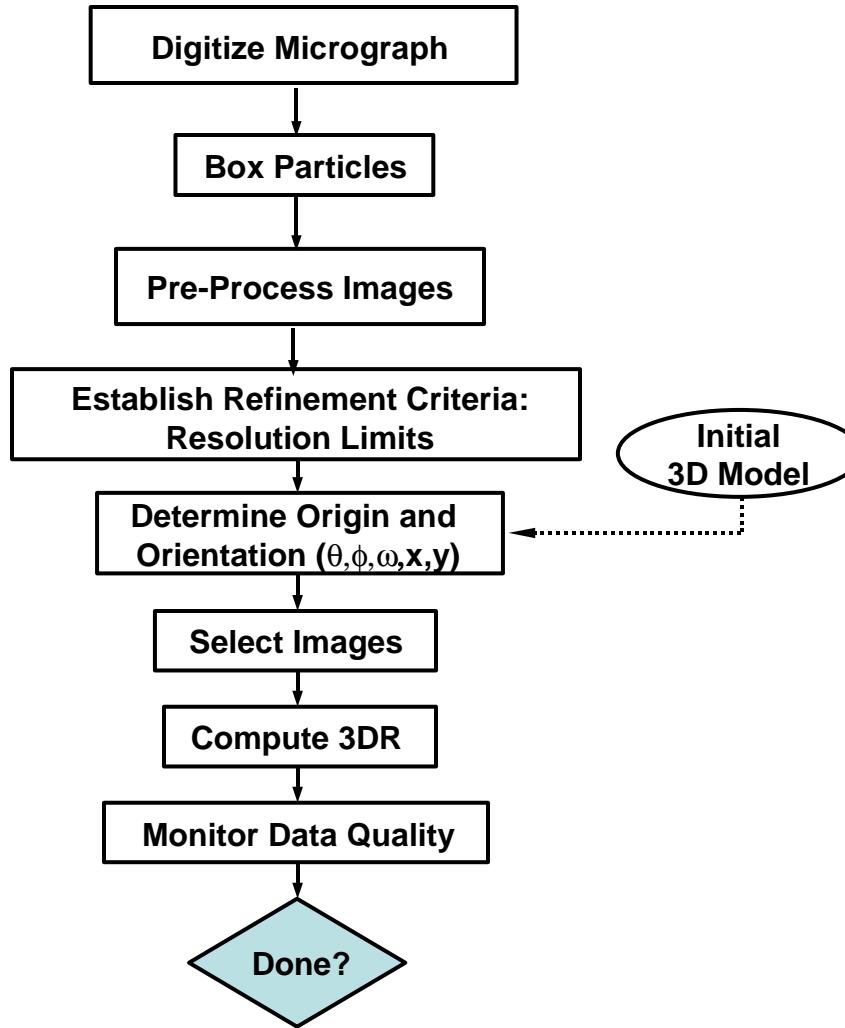
Monitor Data Quality



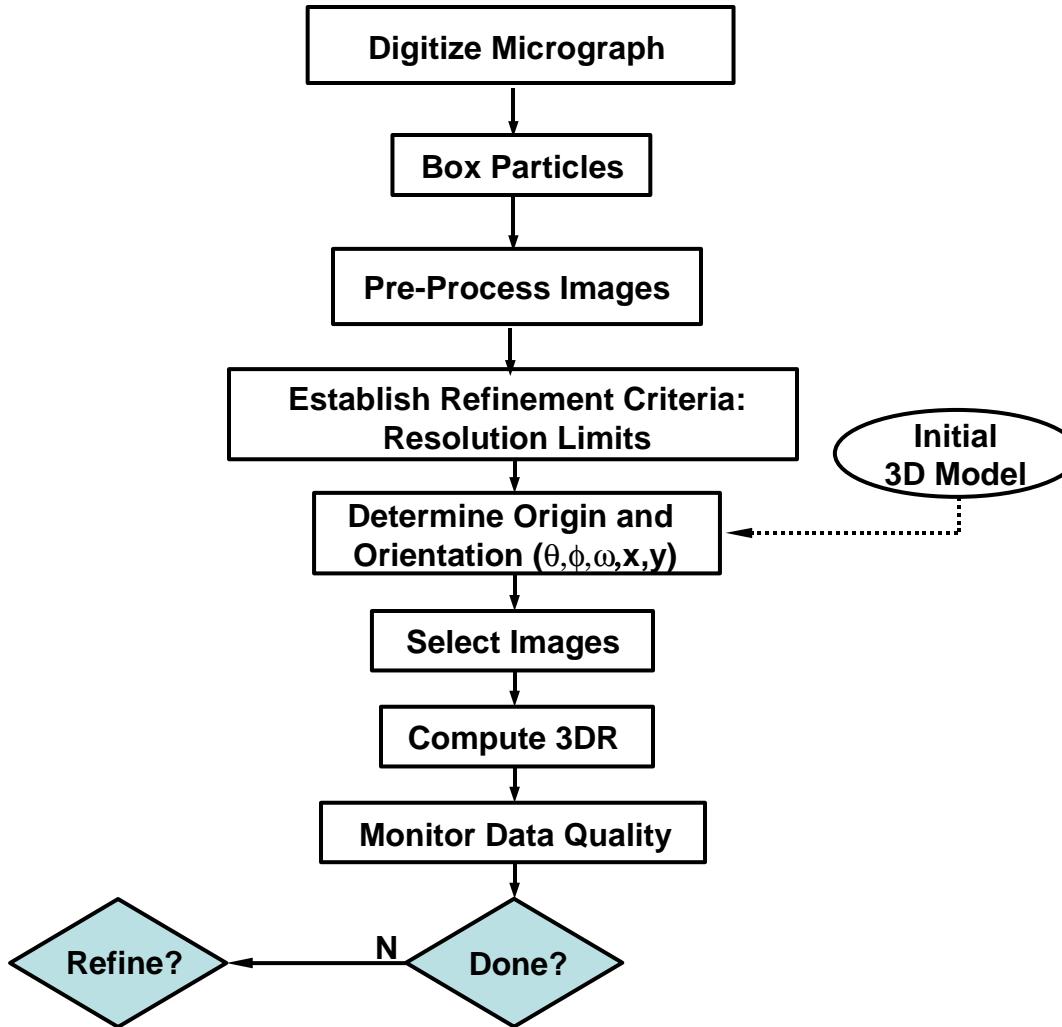
Icosahedral Virus 3D Reconstruction Scheme



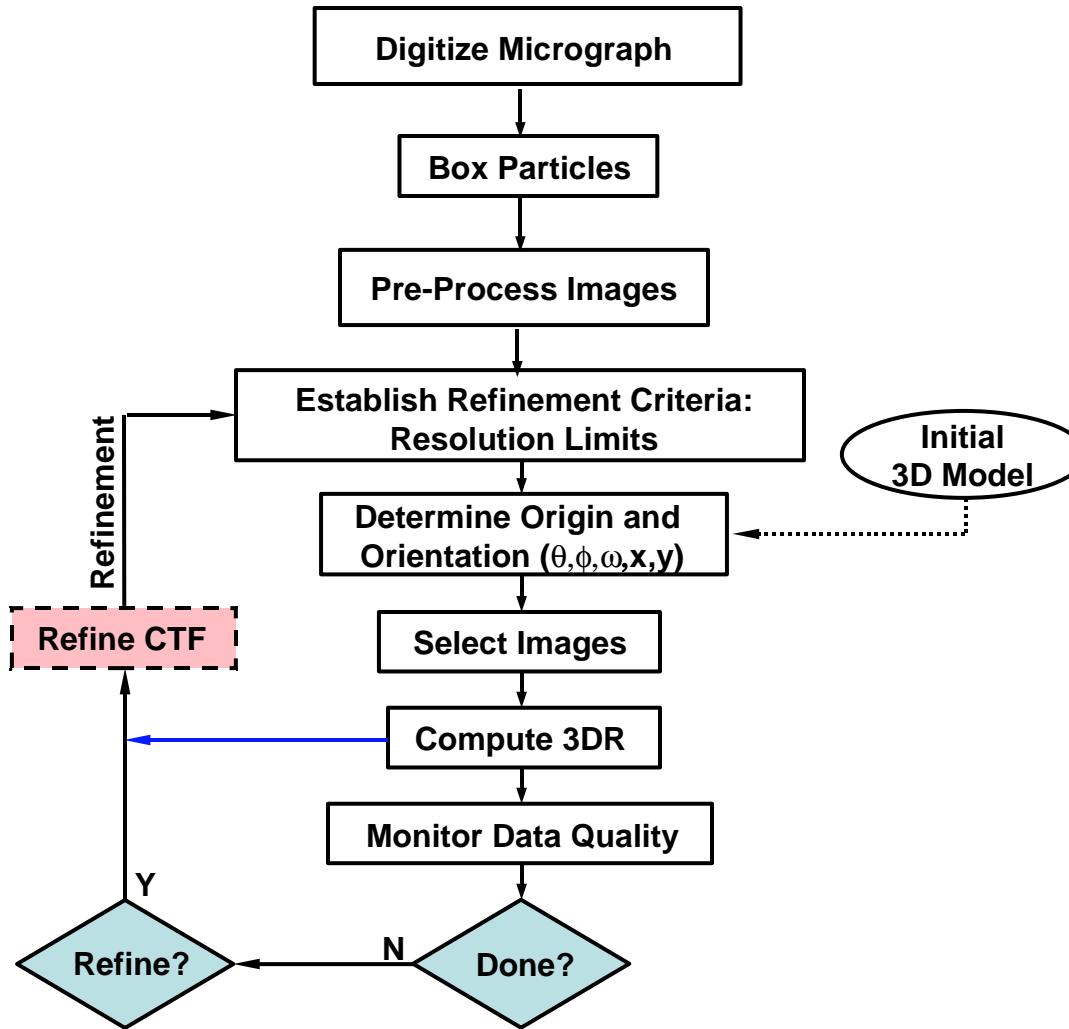
Icosahedral Virus 3D Reconstruction Scheme



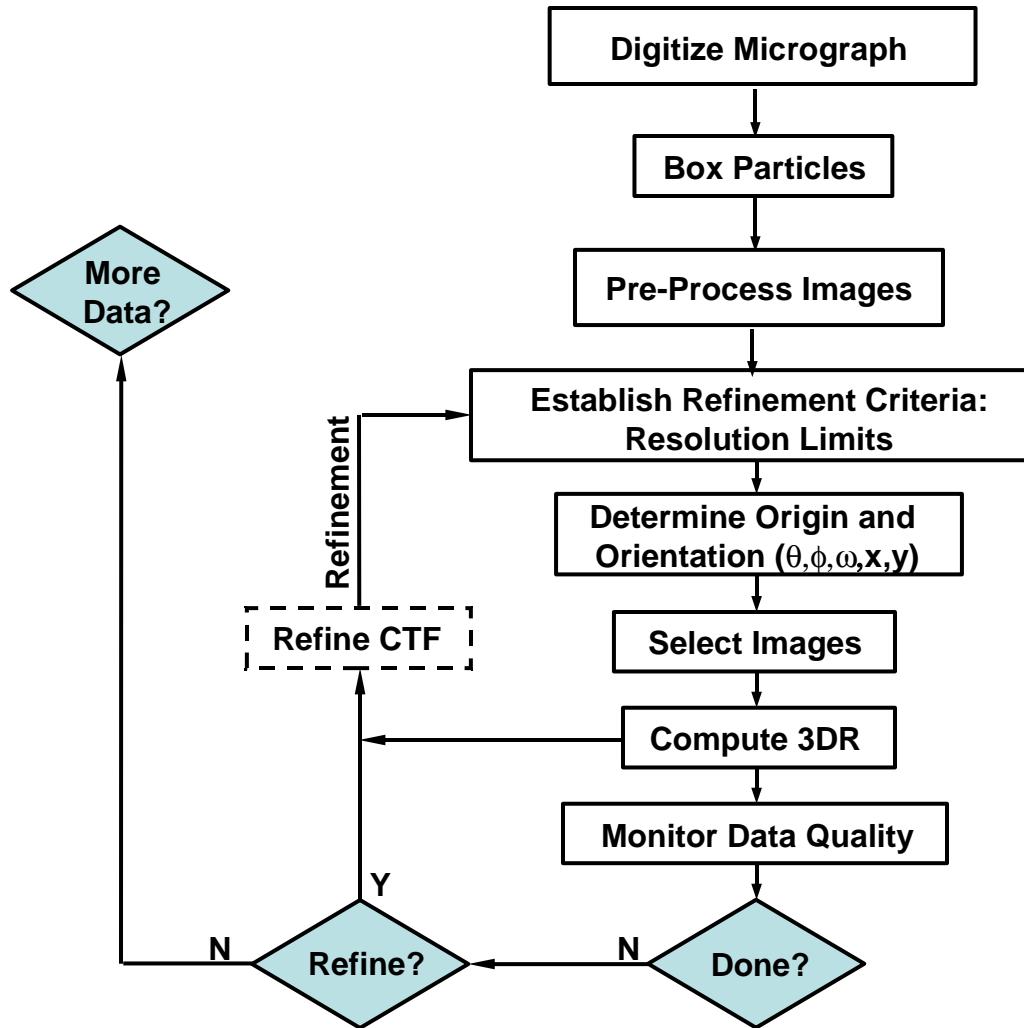
Icosahedral Virus 3D Reconstruction Scheme



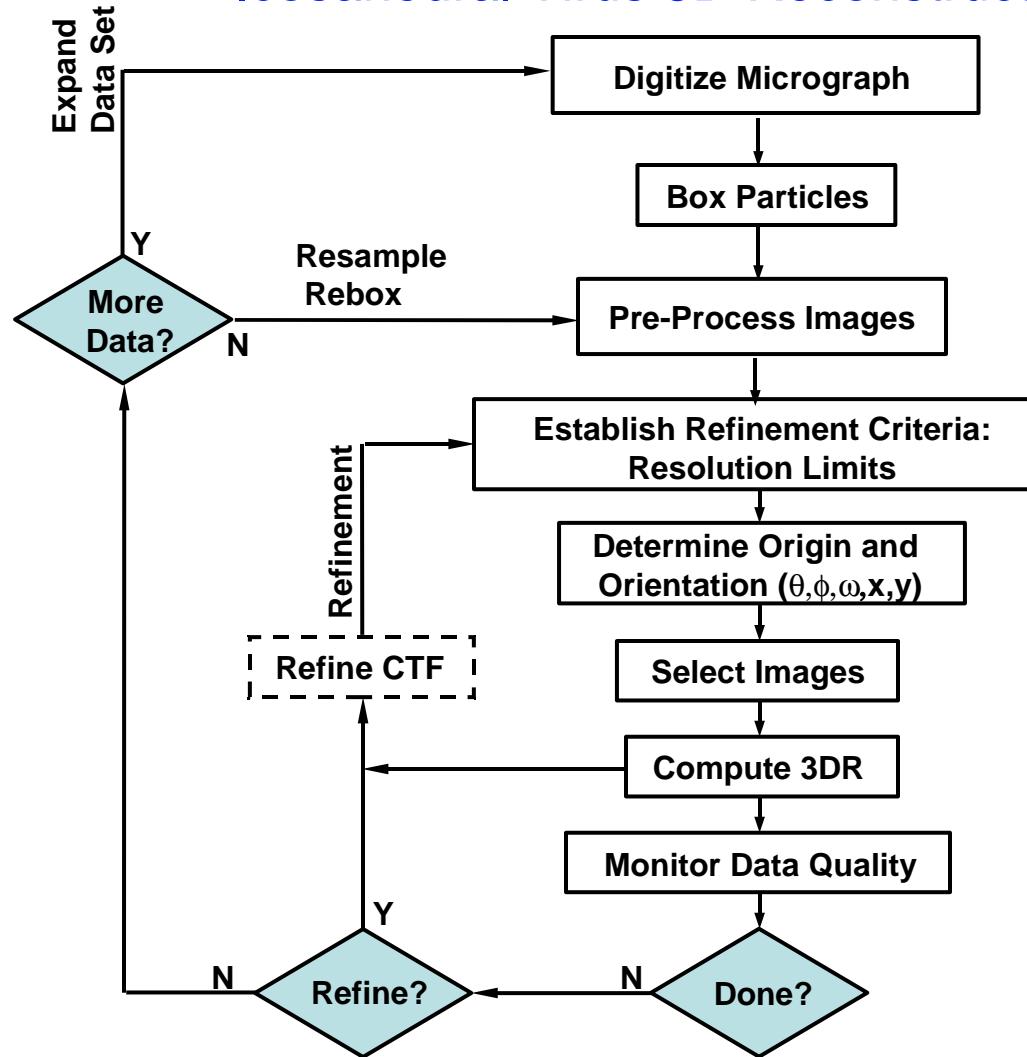
Icosahedral Virus 3D Reconstruction Scheme



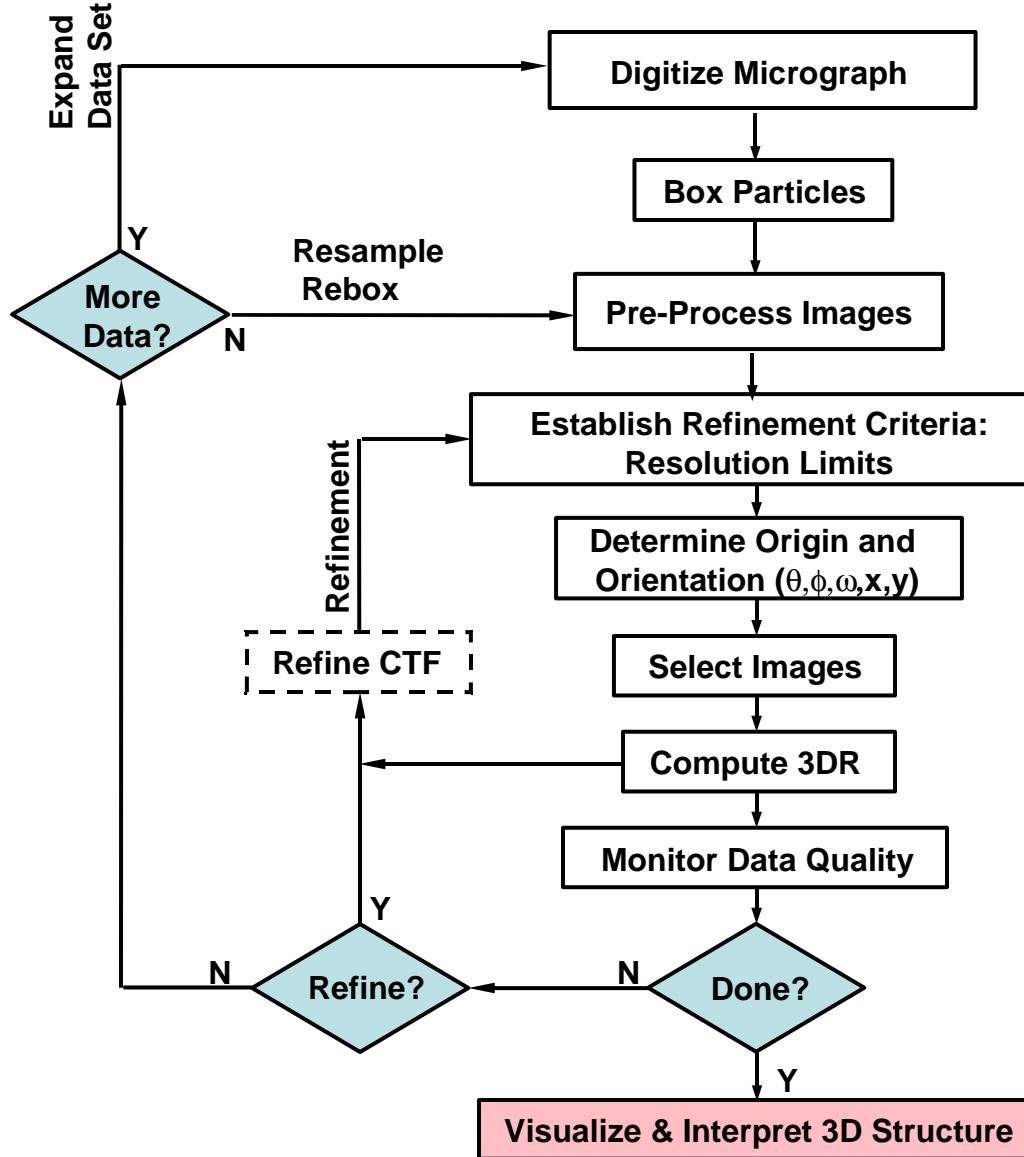
Icosahedral Virus 3D Reconstruction Scheme



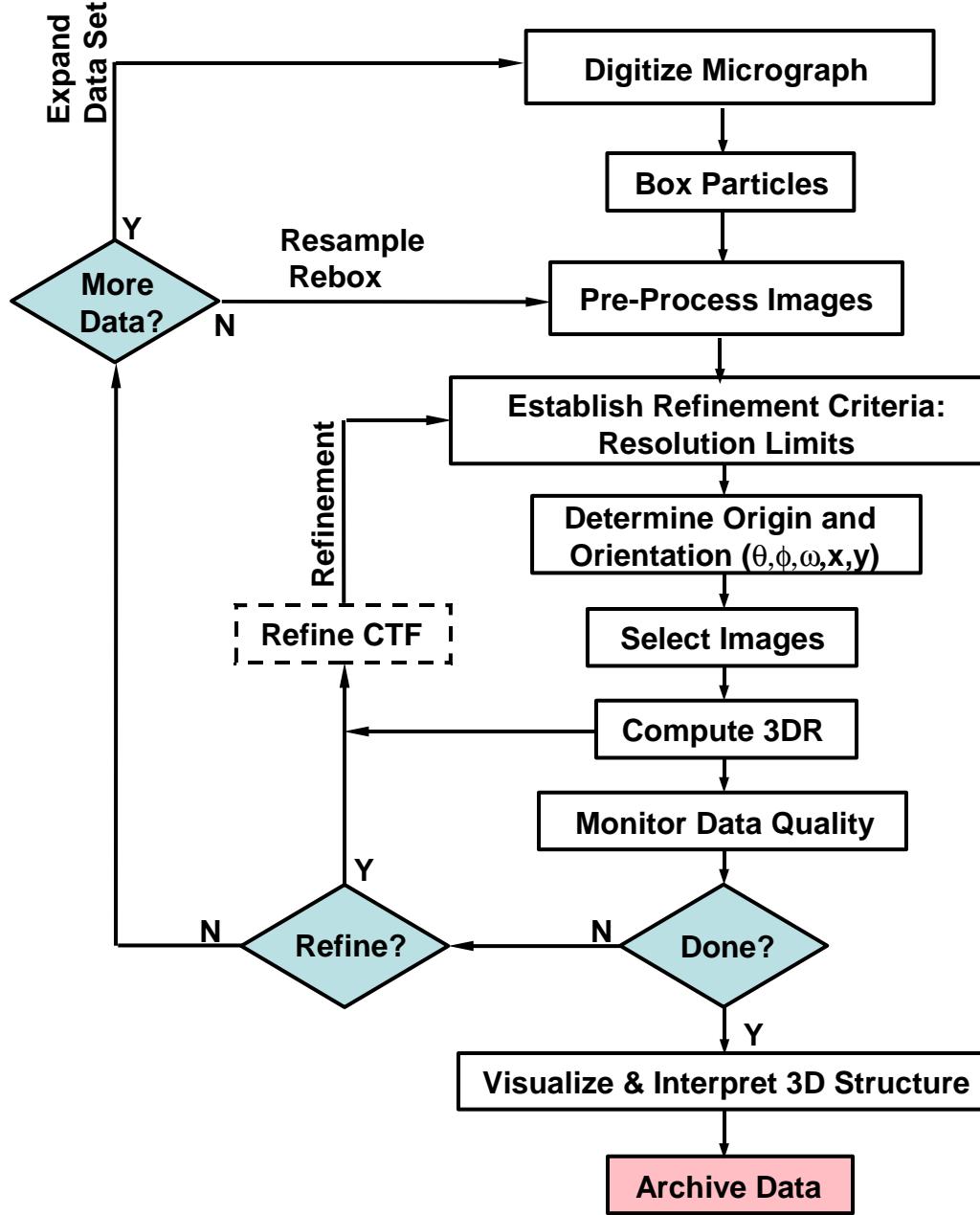
Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme



Icosahedral Virus 3D Reconstruction Scheme



3D Reconstruction of Icosahedral Particles

Outline

- Background

- References; examples; etc.

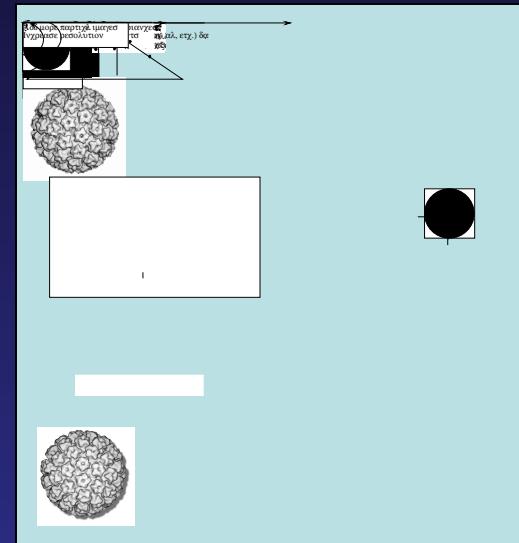
- Symmetry

- Icosahedral (532) point group symmetry
 - Triangulation symmetry

- “Typical” procedure (flow chart)

- Digitization and boxing
 - Image preprocessing / CTF estimation
 - Initial particle orientation/origin search
 - Orientation/origin refinement
 - 3D reconstruction with CTF corrections
 - Validation (resolution assessment)

- Current and future strategies



3D Reconstruction of Icosahedral Particles

Outline

- Background
 - References; examples; etc.
- Symmetry
 - Icosahedral (532) point group symmetry
 - Triangulation symmetry
- “Typical” procedure (flow chart)
 - Digitization and boxing
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 - Orientation/origin refinement
 - 3D reconstruction with CTF corrections
 - Validation (resolution assessment)
- Current and future strategies

3D Reconstruction of Icosahedral Particles

Current and Future Strategies

- Parallelization and new algorithms

- “Parallel” versions of EM3DR, PFTSEARCH, OOR
- EM3DR ---> P3DR
- OOR -----> PO²R

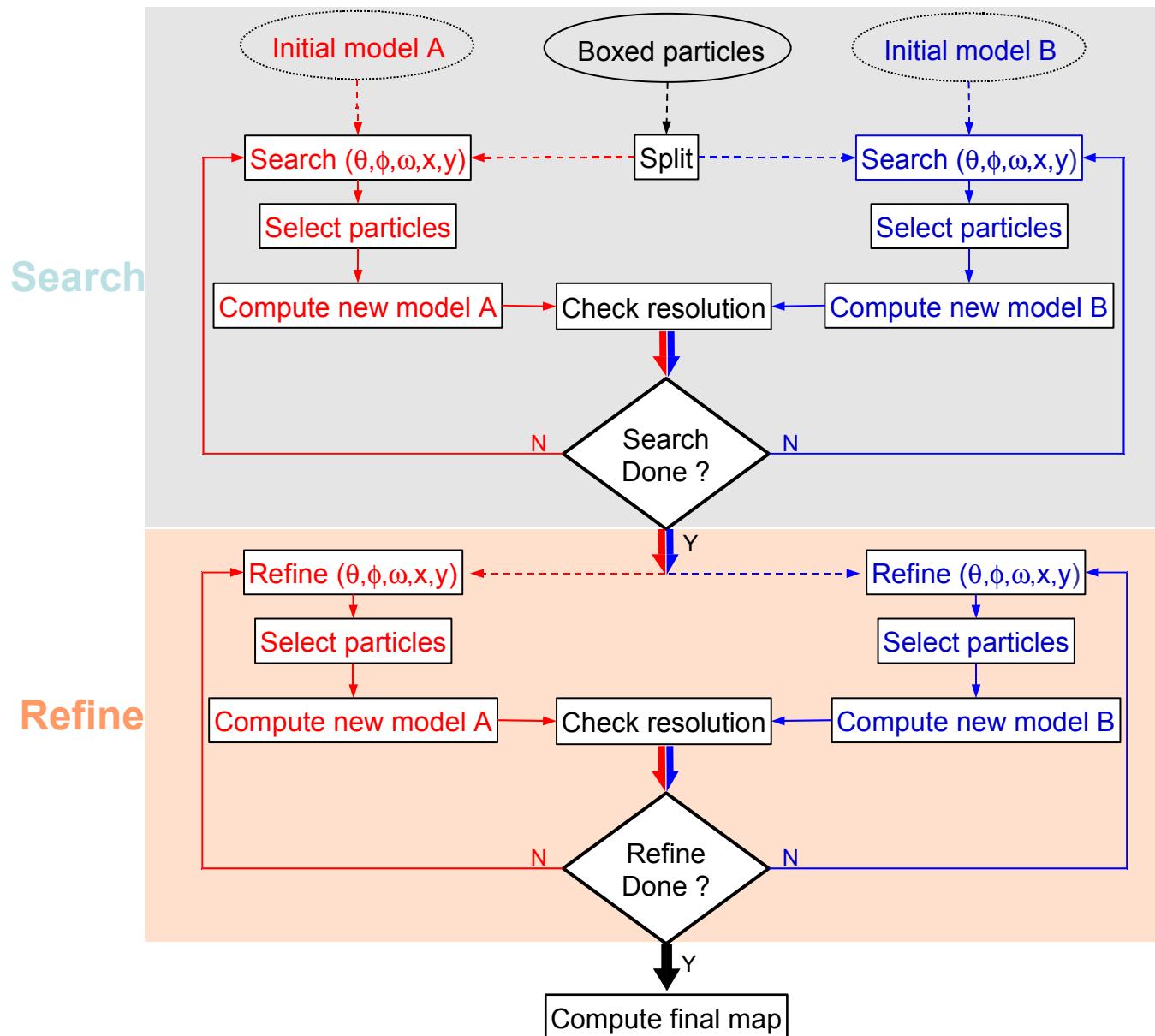
- Automation

- Semi-auto boxing (RobEM)
- Automated origin/orientation refinement (AUTO3DEM)

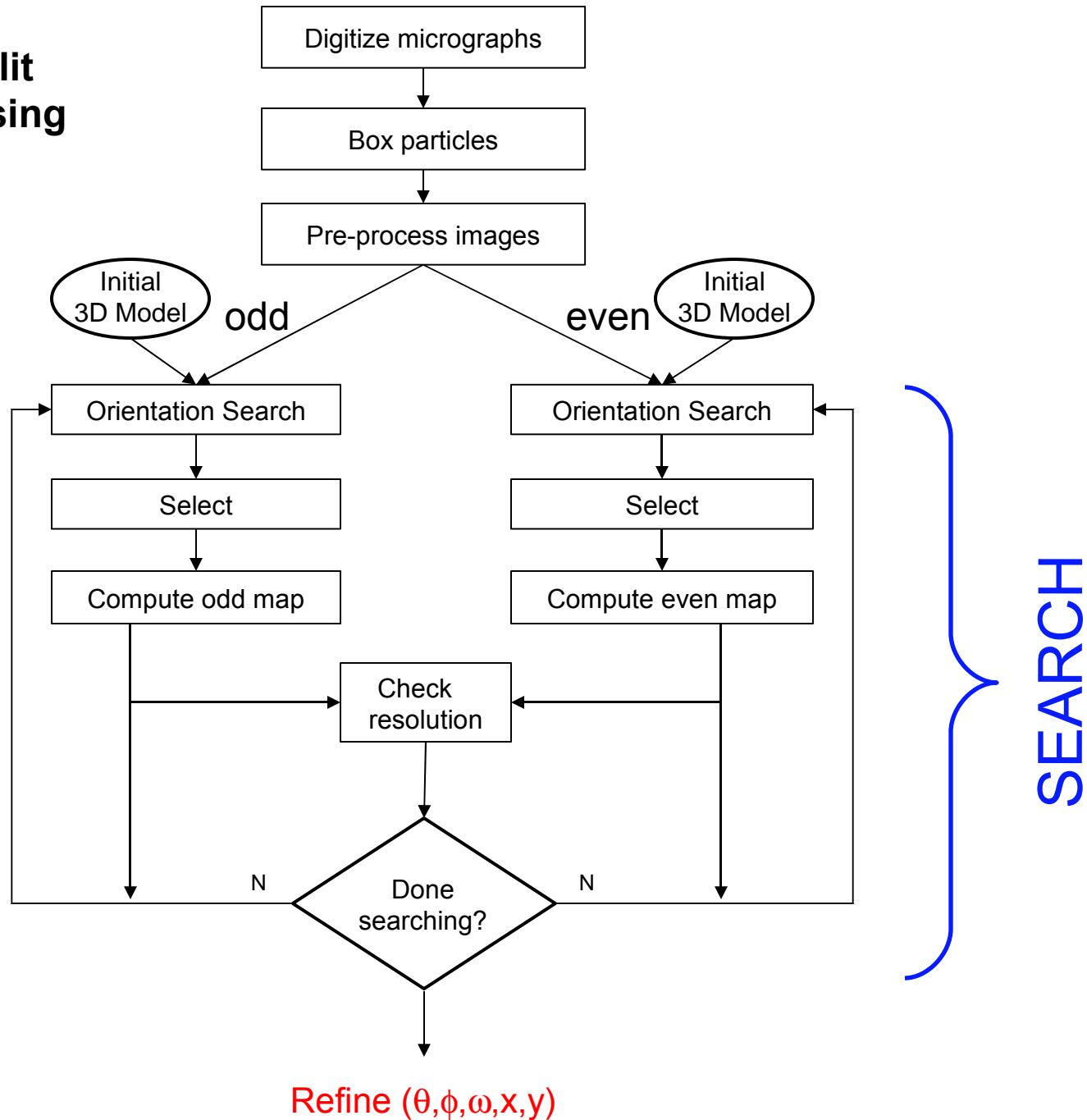
- Split data set processing

- Divide image data at very beginning and refine ‘even’ and ‘odd’ data independently.
- Minimizes (eliminates ?) bias in resolution assessment
- Combine independent reconstructions to obtain ‘final’ 3DR with highest S/N

Structure Determination Flow Chart



Data Flow for Split Data Set Processing



3D Reconstruction of Icosahedral Particles

Current and Future Strategies

- Data selection

Trying to improve resolution by substantially increasing the number of images averaged *ad infinitum* may prove less beneficial than simply applying more rigorous quality control measures to weed out ‘bad’ data.

Borgnia, M. J., D. Shi, P. Zhang and J. L. Milne (2004) Visualization of α -helical features in a density map constructed using 9 molecular images of the 1.8 MDa icosahedral core of pyruvate dehydrogenase. *J. Struct. Biol.* 147:136-145.

